



ANNULAR JETS

by

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TABLE OF CONTENTS

	<u>Page</u>
SUMMARY	i.
SIGNED STATEMENT	ii.
ACKNOWLEDGEMENTS	iii.
INTRODUCTION	1.
<u>CHAPTER 1. ANNULAR NOZZLES</u>	4.
1. Introduction	4.
2. Equations for Initial Slope	6.
3. Separation of Variables Equations	8.
4. Numerical Procedure	10.
5. Computing Kappa	14.
6. Numerical Results	15.
7. Large β Limit	17.
8. Offset Pipes	18.
9. Conclusion	19.
<u>CHAPTER 2. ANNULAR JETS WITH SURFACE TENSION</u>	21.
1. Introduction	21.
2. Equations for Thick, Slender Annular Jets	23.
3. Solution of the Boundary Value Problem	25.
4. Computed Results and Discussion	28.
5. Thin-Slender Annular Jets	37.
6. Solutions for Thin-Slender Annular Jets	39.
7. Thin Annular Sheets of Water	41.
8. Equations for a Thin Jet	43.
9. The Dynamic Equations	49.
10. Conclusions	53.

<u>CHAPTER 3.</u>	<u>STABILITY OF ANNULAR COLUMNS OF WATER</u>	55.
1.	Introduction	55.
2.	Temporal Instability of an Annular Column	55.
3.	Equations of Motion	57.
4.	Kinematic Boundary Conditions	57.
5.	Dynamic Boundary Conditions	58.
6.	The Dispersion Relations	60.
7.	Results	62.
8.	Small β Limit	69.
9.	Thin Jet Limits	71.
10.	Intermediate Modes	71.
	 BIBLIOGRAPHY	 74.

SUMMARY

In this thesis annular jets, falling vertically (when gravity is included), are considered. Thus in any horizontal plane the jet lies between two concentric circles. The three main jet parameters examined are surface tension, jet thickness and a pressure difference across the annulus. Various types of dynamic behaviour are also considered, including formation of jets from nozzles and stability of jets.

Techniques are developed where the behaviour of such jets may be described mathematically, and solutions for a wide spectrum of jet parameters presented.

SIGNED STATEMENT

I hereby declare that this thesis contains no material which has been accepted for the award of any other degree or diploma in any University and, to the best of my knowledge, it contains no material previously published by any other person, except where due reference is made in the text of the thesis.

...

M. S. BORGAS.

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