

# A Mechanics Simulation of the Influence of Reinforcement Corrosion on RC Beam Behaviour

by

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### ABSTRACT

Corrosion influences both of the serviceability limit state and the ultimate limit state of the reinforced concrete structures. The mass loss of reinforcement caused by corrosion not only reduces cross sectional area of the reinforcement but also the bond between the steel reinforcement and surrounding concrete. By reducing the bond between the reinforcement and surrounding concrete, at serviceability limit state, corrosion may lead to an increase crack width and deflection, while at the ultimate limit state it may lead to reinforcement debonding. Hence, knowledge of the influence of corrosion on the bond between reinforcement and concrete is required to evaluate structural behaviour and extend the life span of the reinforced concrete structures.

This thesis first investigates the influence of corrosion on bond properties yielding a new bond-slip material model which has been developed from the analysis of a large data base of 377 individual test results obtained from published experimental results. From the resulting bond-slip model it is shown the debonding of reinforcement may occur at relatively low levels of corrosion and that the influence of corrosion on bond is more significant corrosion for large bar diameters.

Having developed a material model illustrating how corrosion influences the bond-slip relationship, the impact of corrosion on reinforced concrete beams is considered. Firstly the performance of beams at the ultimate limit state is considered through the development of a numerical segmental analysis technique to simulate member behaviour prior to and post debonding. Importantly this model shows that although debonding of reinforcement may occur at a relatively low level of corrosion, it does not always negatively impact member strength or ductility.

The impact of reinforcement corrosion at the serviceability limit state is then considered through the extension of the segmental approach to incorporate not only the influence of bond but also concrete creep and shrinkage. The resulting model couples concrete creep and shrinkage with reinforcement corrosion and predicts the influence of each on crack width and member deflection. Significantly it is shown that reinforcement corrosion can be much more easily monitored through measurement of crack widths over time rather than through consideration of member deflection and the approach proposed may be used to provide guidance on the variation in reinforcement corrosion along a span.

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### LIST OF PUBLICATIONS

Feng, Q, Visintin, P and Oehlers, DJ (2016) Deterioration of bond–slip due to corrosion of steel reinforcement in reinforced concrete. Magazine of Concrete Research, 68(15): 768-781.

Feng, Q, Visintin, P and Oehlers, D (2016) Quantifying through bond mechanics the effect of steel bar corrosion on the flexural capacity of RC beams. Submitted to Proceedings of the Institution of Civil Engineers-Structures and Buildings.

Feng, Q, Visintin, P and Oehlers, D (2016) A mechanics prediction of reinforcement corrosion in RC beams through the measurement of crack widths. Submitted to Structural Concrete.

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### INTRODUCTION

This thesis collects one published paper and 2 submitted papers to show (i) how bond-slip relationship between concrete and reinforcement changes with corrosion; (ii) how corrosion influences the serviceability and ultimate limit states of reinforced concrete structures; (iii) how to monitor the level of reinforcement corrosion.

The first chapter develops a material model to predict the bond-slip relationship between corroded reinforcement and concrete. A large database of existing test data is collected and the influence of concrete compressive strength, concrete cover and reinforcing bar diameter is investigated. Importantly, based on partial interaction theory, this paper quantifies the level of corrosion required to cause the reinforcement to debond and shows that relatively low levels of corrosion lead to debonding of reinforcement prior to yielding. Examples of analysis with different bar diameters are presented and it is shown from mechanics that reinforcement of larger diameters is more susceptible to the debonding induced by corrosion.

Having quantified the corrosion required to cause debonding of reinforcement in chapter 1, chapter 2 develops analytical procedures to calculate the flexural capacity and ductility of members with corroded reinforcement. Significantly the analysis procedures developed consider behaviour prior to dobonding of corroded reinforcement as well as analysis after debonding occurs by treating the unbonded reinforcement in a similar way to unbonded post-tensioned tendons. Importantly, the results of the analysis indicate that, despite the existence of debonding, members may still have significant capacity and ductility due to deformation compatibility between the reinforcement and concrete. This chapter tells reader that debonding caused by corrosion may not be a catastrophic problem in terms of beam strength and ductility.

Chapter 2 affords a model to analyse the problems caused by corrosion in ultimate limit states while Chapter 3 provides a monitoring way to quantify the corrosion effects in serviceability limit states. As is widely known, concrete creep and shrinkage have significant impact at the serviceability limit state of reinforced concrete leading to increased deflection and crack widths. In this chapter is shown how the additional time dependent action of reinforcement corrosion can be coupled with concrete creep and shrinkage. Significantly, this chapter provides a methodology for predicting variation in corrosion along the span of a member by monitoring crack widths over time.

### CHAPTER 1

### Manuscript

Feng, Q, Visintin, P and Oehlers, DJ (2016) Deterioration of bond–slip due to corrosion of steel reinforcement in reinforced concrete. Magazine of Concrete Research, 68(15): 768-781.

## Statement of Authorship

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Name of Principal Author (Candidate)	Qian Feng
Contribution to the Paper	Performed analysis on data base building and data processing, interpreted data and wrote manuscript.
Overall percentage (%)	75%
Certification:	This paper reports on original research I conducted during the period of my Higher Degree by Research candidature and is not subject to any obligations or contractual agreements with a third partv that would constrain its inclusion in this thesis. I am the primary author of this paper.
Signature	Date 19/08/2016

#### **Co-Author Contributions**

By signing the Statement of Authorship, each author certifies that:

- i. the candidate's stated contribution to the publication is accurate (as detailed above);
- ii. permission is granted for the candidate in include the publication in the thesis; and
- iii. the sum of all co-author contributions is equal to 100% less the candidate's stated contribution.

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Name of Co-Author	Deric Oehlers				
Contribution to the Paper	Supervised development of work, helped edit manuscript and helped check details.				
-					
Signature		Date	19/08/2016		

Please cut and paste additional co-author panels here as required.

#### Deterioration of bond-slip due to corrosion of steel reinforcement in RC

Qian Feng, Phillip Visintin and Deric John Oehlers

#### Abstract

Corrosion of steel reinforcement in RC members is a common occurrence and a major concern as it can significantly affect both the serviceability and ultimate limit states. In order to simulate the effects of corrosion through mechanics, it is necessary to quantify the effects of corrosion on the material bond-slip properties, which is the subject of this paper. A large data base of 377 data points, is used to quantify the effect of corrosion on the bond-strength and on the bond-slip in a form that can be used in numerical analyses. This research concentrates on the changes in bond-strength and bond-slip due to corrosion and hence the changes relative to the uncorroded properties because these are already well quantified. Furthermore, it does not consider the clamping action of stirrups encasing the reinforcement. As an illustration of the application of these bond properties of corroded steel reinforcement, they are used in a mechanics analysis to show that large diameter bars are much more susceptible to the effects of corrosion than small diameter bars.

Keywords: bond-slip; bond-strength; steel reinforcement; corrosion; debonding.

#### Notation

A<sub>r</sub> = cross-sectional area of reinforcing bar allowing for reduction in area due to corrosion C = % corrosion; % loss of mass due to corrosion C<sub>pk</sub> = C at peak  $\tau_{max}$ C<sub>tran</sub> = C at transition from yield to P<sub>IC</sub> C<sub>1-2</sub> = C at transition from Stage 1 to Stage 2 where k<sub>t</sub> = 0 C<sub>2-3</sub> = C at transition from Stage 2 to Stage 3 c = reinforcing bar cover d<sub>b</sub> = reinforcing bar diameter E<sub>r</sub> = modulus of reinforcing bar f<sub>c</sub> = concrete cylinder strength f<sub>y</sub> = yield strength of reinforcing bar K<sub>s</sub> = slope of τ/δ descending branch

 $K_{s1} = K_s$  divided by  $\tau_{max0}$  $K_{2D}$  = slope of Stage 2 Descending branch  $k_{t}$  =  $\tau_{max}/\tau_{max0}$  $(k_t)_{pk}$  = maximum or peak value of  $k_t$  $k_{t-1A} = k_t$  in Stage 1 Ascending branch  $k_{t-2D}$  =  $k_t$  in Stage 2 Descending branch  $(k_{t-2D})_{exp}$  = experimental value of  $k_{t-2D}$  $(k_{t-2D})_{the}$  = theoretical value of  $k_{t-2D}$  from Eq. 5  $k_{t-3} = k_t$  in Stage 3 branch L<sub>emb</sub> = reinforcement embedment length  $L_{per}$  = perimeter of uncorroded reinforcing bar;  $\pi d_b$  $P_{IC}$  = intermediate crack debonding resistance  $P_{yld}$  = yield strength of reinforcing bar;  $A_r f_y$  $P_{yld0} = P_{yld}$  of uncorroded bar  $\alpha$  = exponent of ascending  $\tau/\delta$  model  $\delta$  = interface bond slip  $\delta_{\text{max}} = \delta$  at zero shear  $\delta_1 = \delta$  at  $\tau_{max}$  $\tau$  = interface bond shear; shear stress  $\tau_{max}$  = maximum shear stress; bond-strength  $\tau_{max0} = \tau_{max}$  at zero corrosion  $\tau/\delta$  = bond-slip variation

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#### 1. Introduction

The bond between the reinforcement and adjacent concrete in RC members affects the flexural behaviour at both the serviceability and ultimate limit states, as well as the shear capacity. Needless to say, the deterioration of this bond due to corrosion of the steel reinforcement can cause both increased deflections and reduced strengths and consequently lead to failure. Thus there is a clear need for accurately predicting the deteriorated bond-slip for use in mechanics models that use the bond-slip properties directly to simulate the flexural and shear capacity of beams (Visintin et al. 2012; Zhang et al. 2014) as well as the long term deflection (Visintin et al. 2013). Hence although not the purpose of this paper, with an improved definition of the change in bond properties due to corrosion these models can assist in predicting the performance of a structure deteriorated by reinforcement corrosion.

There is already a very large number of publications experimentally investigating or empirically quantifying: (1) the deterioration due to corrosion of the bond-strength (Johnston and Cox 1940;

Peattie and Pope 1956; Kemp et al 1968; Chapman and Shah 1987; Al-Sulaimani et al 1990; Maslehuddin et al 1990; Giuriani et al 1991; Cabrera and Ghoddoussi 1992; Almusallam et al 1996; Ihekwaba et al 1996; Fu and Chung 1997; Amleh and Mirza 1999; Auyeung et al 2000; Jin and Zhao 2001; Lee et al 2002; Lundgren 2002; Al-Negheimish and Al-Zaid 2004; Fang et al 2004; Amleh and Ghosh 2006; Cairns et al 2006; Fang et al 2006; Ouglova et al 2008; Kobayashi et al 2010; Shang et al 2011; Yalciner et al 2012; Fischer and Ožbolt 2013), that is the maximum interface shear  $\tau_{max}$  that can be resisted after corrosion; (2) the change in the bond-slip  $(\tau/\delta)$  characteristics due to corrosion, that is the relationship between the interface shear stress  $\tau$  and interface slip  $\delta$  with corrosion (Al-Sulaimani et al 1990; Almusallam et al 1996; Lee et al 2002). Additionally there exist a number of studies deriving semi-empirical approaches for predicting the bond-strength  $\tau_{max}$  as a function of corrosion. These models are derived through regression analyses of varying complexity and typically take a linear (Cabrera 1996), non-linear (Jin and Zhao 2001; Chung et al 2008) or exponential (Lee et al 2002; Bhargava et al 2007; Yalciner et al 2012) form. As with most empirical models they are generally accurate within the bounds of the experimental population from which they were derived. However, they are less accurate or inaccurate beyond these bounds and importantly and in general, existing models are derived from limited data sets.

In this study, the very large amount of published data referenced above has been scrutinised to extract that which gives sufficient information for the extraction of the changes in the bond properties due to corrosion. This refined data is then used to derive expressions for the changes in the bond-strength and bond-slip due to corrosion and which are compared with published values. It should be emphasised here that the purpose of this work is not to provide the practitioner with guidance on predicting the level of corrosion, but rather once the level of corrosion in a structure is determined to provide guidance on how the bond is affected. The outcomes of this research can be used directly in numerical simulations. However as just one example of their application, they are used in published partial-interaction mechanics analyses to quantify the debonding resistance of corroded reinforcement; such that it can be shown that there exists a transition whereby failure is no longer initiated by yielding of the reinforcement but rather debonding. Full details of all the papers considered, the reasons for eliminating papers and the results of all the statistical regression analyses are given elsewhere (Feng 2014).

#### 2. Data bases

#### 2.1 Idealisation of bond models

The variation of the bond-slip  $(\tau/\delta)$  is idealised as in Fig. 1. In theory any ascending branch can be used. For convenience the following model is used (CEB-FIP 1993)

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$$\tau = \tau_{max} (\frac{\delta}{\delta_1})^{\alpha} \tag{1}$$

in which the maximum shear stress or bond-strength  $\tau_{max}$  occurs at a slip  $\delta_1$  and in which  $\alpha$  can be taken as 0.4 (CEB-FIP 1993). The slope of the descending branch in Fig. 1 is defined as K<sub>s</sub> and the slip at zero shear  $\delta_{max}$ .



Figure 2 Idealised bond-strength variation with corrosion

The variation of the bond-strength ( $\tau_{max}$ ) with the percentage mass loss due to corrosion (C) is idealised as the tri-linear variation in Fig. 2 where k<sub>t</sub> is the bond-strength  $\tau_{max}$  as a proportion of the bond-strength with zero corrosion  $\tau_{max0}$  (Mirza and Houde 1979; Howe 1979; Eligehausen et al 1982; CEB-FIP 1993 Wu and Zhao 2012). It should be noted that in this work the different forms of corrosion are not distinguished and it is assumed that corrosion quantified as a percentage of mass loss is uniform along the reinforcing bar. Within Stage 1, which is bounded by the peak bondstrength which occurs at a corrosion level C<sub>pk</sub>, corrosion enhances the bond strength and thus a conservative design would be to ignore this benefit. Stage 2 is associated with a rapid reduction in the bond-strength below  $\tau_{max0}$ . The transition from Stage 1 to Stage 2 occurs at a corrosion percentage C<sub>1-2</sub>. Stage 3 is associated with very low bond-strengths that only reduce gradually. The transition from Stage 2 to Stage 3 occurs at a corrosion percentage of C<sub>2-3</sub>.

It is a question of quantifying each linear variation of the tri-linear variation in Fig. 2. The first linear variation is the ascending branch in Stage 1 and will be referred to as 'Stage 1 Ascending'. Only a small part of the second linear variation occurs in Stage 1 so it will be referred to as 'Stage 2 Descending'. The third linear variation will be referred to as 'Stage 3'.

#### 2.2 Limitations to test data

To allow the bond properties in Figs. 1 and 2 to be quantified, it was necessary to restrict the data base to tests in which there was enough information from which these bond properties could be extracted. Hence test data that did not conform with the following requirements or limitations were not used in the statistical analyses.

- 1. Limited to deformed or ribbed reinforcing bars.
- 2. Accelerated corrosion was achieved by inducing corrosion following the encasement of the bar in concrete, that is, tests in which bars were pre-corroded have been excluded.
- 3. The level of corrosion is calculated as the proportion of the mass loss as opposed to exposure time or the severity of the environment.
- Pull-tests had short embedment lengths. Such that the average bond stress was close to the actual bond stress. This was confirmed through partial-interaction tension-stiffening analyses (Haskett et al. 2008; Knight et al. 2013; Feng 2014).
- 5. The ribbed bars were not entrapped by stirrups as the presence of stirrups is an additional anchor or confinement that should be dealt with as an alternative bond such as a mechanical anchor.
- The concrete strength (f<sub>c</sub>), concrete cover (c) and bar diameter (d<sub>b</sub>) had been stated as these were considered important parameters.
- 7. The bond-strength at zero corrosion  $\tau_{max0}$  had been measured within the series of tests. This was considered important as the aim of this research is to determine the change due to corrosion from this reference point.
- 8. When dealing with Stage 2 in Fig. 2, only test series in which there was sufficient test data to quantify the slope of the descending branch were included.

Full details of all the data collected and the reasons for omitting specific data are given elsewhere (Feng 2014). However in general most test data was excluded in the present study due to insufficient

information to be able to determine the corrosion level as a function of mass loss. Additionally, tests were excluded if the bonded length, according to a tension stiffening analysis (Haskett et al. 2008), was found to be of a length such that the average bond stress could not be taken as the actual bond stress.

#### 2.3 Bond-strength corrosion data base

Based on the requirements in Section 2.2, the data sets for the bond-strength are listed in Table 1. It can be seen that there are 15 data sets from 7 publications. Furthermore there is a wide range in the variables:  $f_c$  varied from 22 to 60 MPa; cover c from 8 to 70 mm; bar diameter  $d_b$  from 10 to 20 mm; and the embedment length  $L_{emb}$  from 40 to 208 mm.

Data sets	References	f <sub>c</sub> (MPa)	c (mm)	d <sub>b</sub> (mm)	L <sub>emb</sub> (mm)
M1	Almusallam et al. (1996)	30	64	12	102
M2	Al-Sulaimani et al. (1990)	30	70	10	40
M3	Al-Sulaimani et al. (1990)	30	68	14	56
M4	Al-Sulaimani et al. (1990)	30	65	20	80
M5	Yalciner et al. (2012)	23	8	14	50
M6	Yalciner et al. (2012)	23	23	14	50
M7	Yalciner et al. (2012)	23	38	14	50
M8	Yalciner et al. (2012)	51	8	14	50
M9	Yalciner et al. (2012)	51	23	14	50
M10	Yalciner et al. (2012)	51	38	14	50
M11	Fang et al. (2006)	52	60	20	80
M12	Jin and Zhao (2001)	22	44	12	80
M13	Cabrera and Ghoddoussi (1992)	56	69	12	48
M14	Amleh and Ghosh (2006)	60	25	20	208
M15	Amleh and Ghosh (2006)	50	25	20	208

#### Table 1 Bond-strength data sets

The individual data points from the papers in Table 1 are given in Table A in the Appendix. There are a total of 196 results in which: there is always within a series a bond-strength at 0% corrosion that is  $\tau_{max0}$  as this is the datum by which all other values are compared; the percentage corrosion C reached 80%;  $\tau_{max}$  ranged between 0.67 MPa and 30.7 MPa; and k<sub>t</sub> between 0.088 and 1.54. The

bond-strengths  $\tau_{max}$  in Table A are divided by their respective strengths at zero corrosion, that is at C equal to 0%, to determine  $k_t$ . Hence

$$\tau_{\max} = k_t \tau_{\max 0} \tag{2}$$

which are plotted in Fig. 3 as the square points.



Figure 3 Variation of bond-strength with corrosion

#### 2.4 Bond-slip corrosion data base

Based on the limitations in Section 2.2, the data base in Table 2 of 21 bond-slip curves from 3 publications was collected. The individual load-slip curves are shown as unbroken lines in Fig. 4. From each data set in Fig. 4, the maximum shear stress  $\tau_{max}$  and the slip  $\delta_1$  at  $\tau_{max}$  is listed in Table 3.

Furthermore from a linear regression analysis of the falling branches (Feng 2014) of each data set which is plotted as the 'Regression' line in Fig. 4 was extracted the slope of the falling branches  $K_s$  and these are also listed in Table 3.

Data	ta Reference		$f_c$	с	d <sub>b</sub>	т.
Set	Kelefellee	C	(MPa)	(mm)	(mm)	Lemb
N1	Almusallam et al. (1996)	0	30	63.5	12	102
N2	Almusallam et al. (1996)	3.6	30	63.5	12	102
N3	Almusallam et al. (1996)	4	30	63.5	12	102
N4	Almusallam et al. (1996)	4.78	30	63.5	12	102
N5	Almusallam et al. (1996)	5.09	30	63.5	12	102
N6	Almusallam et al. (1996)	7	30	63.5	12	102
N7	Almusallam et al. (1996)	15.7	30	63.5	12	102
N8	Almusallam et al. (1996)	20.5	30	63.5	12	102
N9	Almusallam et al. (1996)	32.5	30	63.5	12	102
N10	Al-Sulaimani et al. (1990)	0	30	70	10	40
N11	Al-Sulaimani et al. (1990)	0.87	30	70	10	40
N12	Al-Sulaimani et al. (1990)	1.5	30	70	10	40
N13	Al-Sulaimani et al. (1990)	4.27	30	70	10	40
N14	Al-Sulaimani et al. (1990)	6.7	30	70	10	40
N15	Al-Sulaimani et al. (1990)	7.8	30	70	10	40
N16	Al-Sulaimani et al. (1990)	1.62	30	68	14	56
N17	Al-Sulaimani et al. (1990)	2.75	30	68	14	56
N18	Al-Sulaimani et al. (1990)	5.45	30	68	14	56
N19	Lee et al (2002)	0	24.7	39	13	78
N20	Lee et al (2002)	3.2	24.7	39	13	78
N21	Lee et al (2002)	16.8	24.7	39	13	78

Table 2 Bond-slip data sets

#### 3. Bond-strength corrosion model

It is now a question of quantifying the variation of the bond-strength parameter  $k_t$  in Fig. 2 that is  $\tau_{max}$  as a proportion of  $\tau_{max0}$ .

#### 3.1 Stage 2 Descending

First consider the falling branch in Fig. 2 that is between the percentage corrosions  $C_{pk}$  and  $C_{2-3}$ . From Fig. 3, it can be seen that the seven data sets M1-M4, M6, M12 and M13 have comparatively clearly defined falling branches. The falling branch in each of these sets of data points was subjected to a linear regression analysis from which was extracted and tabulated in Table 4: the individual slopes  $K_{2D}$ ; and the percentage corrosion  $C_{1-2}$  at  $k_t$  equal to one, that is when  $\tau_{max}$  equalled that of the uncorroded specimen  $\tau_{max0}$  that is  $C_{1-2}$  in Fig. 2. Also listed is the non-dimensional cover parameter  $c/d_b$  and the concrete strength  $f_c$ .



Figure 4 Variations of bond-slip

Data	C	$\tau_{max}$	$\delta_1$	Ks	Ks <sub>-1</sub>
Set	C	(MPa)	(mm)	$(N/mm^3)$	$(mm^{-1})$
N1	0	15.7	0.643	-2.231	-2.527
N2	3.6	17.2	0.400	-3.325	-2.527
N3	4	18.4	0.250	-3.781	-2.527
N4	4.78	16.2	0.064	-3.365	-2.527
N5	5.09	13.6	0.071	-3.651	-2.527
N6	7	4.6	0.029	-1.969	-2.527
N7	15.7	3.0	0.125	-0.257	-2.527
N8	20.5	2.8	0.071	-0.767	-2.527
N9	32.5	2.6	0.010	-2.706	-2.527
N10	0	15.8	0.167	-1.223	-2.540
N11	0.87	24.5	0.133	-3.192	-2.540
N12	1.5	22.5	0.183	-3.779	-2.540
N13	4.27	14.5	0.183	-1.440	-2.540
N14	6.7	7.75	0.242	-3.292	-2.540
N15	7.8	4.13	0.258	-3.364	-2.540
N16	1.62	18.8	0.151	-5.332	-
N17	2.75	15.3	0.146	-5.453	-
N18	5.45	5.0	0.188	-8.268	-
N19	0	6.22	0.291	-0.682	-1.000
N20	3.2	4.21	0.053	-8.356	-1.000
N21	16.8	1.50	0.019	-2.137	-1.000

Table 3 Bond-slip properties

Table 4: Stage 2 Descending statistical results

Data set	c/d <sub>b</sub>	f <sub>c</sub> (MPa)	C <sub>1-2</sub>	K <sub>2D</sub>
M1	5.29	30	4.30	-0.265
M2	7.00	30	3.82	-0.186
M3	4.86	30	2.51	-0.199
M4	3.25	30	1.69	-0.195
M6	1.64	23	2.63	-0.270
M12	3.67	22	3.15	-0.108
M13	5.75	56	3.00	-0.073

A linear regression analysis of the results in Table 4 Feng (2014) showed that neither C<sub>1-2</sub> nor K<sub>2D</sub> were dependent on f<sub>c</sub>. This is probably because the ordinate k<sub>t</sub> in Fig. 2 is a function of  $\tau_{max0}$  which itself is a function of f<sub>c</sub> that is any dependency on f<sub>c</sub> is already allowed for in  $\tau_{max0}$ . However, the linear regression analyses Feng (2014) did show a strong dependency on c/d<sub>b</sub> and the regressions are given below

$$C_{1-2} = 0.288 \times \frac{c}{d_b} + 1.72 \tag{3}$$

$$K_{2D} = 0.0137 \times \frac{c}{d_b} - 0.247 \tag{4}$$

from which can be derived the following linear variation of the Stage 2 Descending branch.

$$k_{t-2D} = \left(0.0137 \frac{c}{d_b} - 0.247\right) C + 1.42 + 0.0475 \frac{c}{d_b} - 3.94 \times 10^{-3} \left(\frac{c}{d_b}\right)^2$$
(5)

The variation of  $k_{t-2D}$  from Equation 5 has been plotted in Fig. 3 as the 'Model' between  $C_{pk}$  and  $C_{1-2}$  for all the data sets and shows reasonably good correlation throughout. For only the data sets in Table 4, dividing the experimental values  $(k_{t-SD})_{exp}$  by the theoretical values  $(k_{t-2D})_{the}$  from Eq. 5 showed very good correlation up to a corrosion level of 6% (Feng 2014). Hence Eq. 5 should be limited to corrosion levels less than 6%; for this range the mean of  $(k_{t-2D})_{exp}/(k_{t-2D})_{the}$  is 0.974 and the coefficient of variation 0.156.

#### 3.2 Stage 1 Ascending

Consider the rising branch in Stage 1 in Fig. 2. The statistical analyses have been restricted to the data base in Section 3.1 which is listed in the first column in Table 5.

	Stage 1 Ascending (k <sub>t-1A</sub> =)	Stage 2 Descending (k <sub>t-2D</sub> =)	(k <sub>t</sub> ) <sub>pk</sub>	C <sub>pk</sub>	C <sub>1-2</sub>	$\frac{C_{pk}}{C_{1-2}}$
M1	0.0458 <i>C</i> + 0.987	-0.265C + 2.14	1.16	3.71	4.30	0.862
M2	0.68C + 1.02	-0.186C + 1.71	1.56	0.780	3.82	0.209
M3	0.374C + 1.02	-0.199 <i>C</i> + 1.5	1.33	0.838	2.51	0.333
M4	0.459 <i>C</i> + 1.02	-0.195C + 1.33	1.24	0.474	1.69	0.280
M6	0.26C + 1	-0.27C + 1.71	1.35	1.34	2.63	0.509
M12	0.36C + 1	-0.108C + 1.34	1.26	0.727	3.15	0.231
M13	0.207 <i>C</i> + 0.994	-0.0733C + 1.22	1.16	0.806	3.00	0.269

Table 5 Bond-strength Stage 1 statistical results

The results of a linear regression analysis of the ascending branches of each data set are listed in Column 2 in Table 5, where, as would be expected the constant is close to unity. The descending branch in Column 3 is from a linear regression analysis of the data for that specific data set and not from Eq. 5. The intercept between the equations in Columns 2 and 3 is the maximum or peak bond-strength  $(k_t)_{pk}$  in Column 4 which occurs at the corrosion level  $C_{pk}$  in Column 5. Substituting  $k_{t-2D} = 1$  into Column 3 gives  $C_{1-2}$  in Column 6. Dividing  $C_{pk}$  in Column 5 by  $C_{1-2}$  in Column 6 gives Column 7.

The result for M1 in the Column 7 can be considered to be an outlier when compared with the remaining values which have a mean of 0.305. Rounding down to 0.3 gives

$$C_{pk} = 0.3C_{1-2}$$
 (6)

which can be substituted into Eq. 5 to derive  $(k_t)_{pk}$  for  $C_{pk}$ . A linear variation from this point  $(C_{pk}; (k_t)_{pk})$  to the intercept on the ordinate (0,1) in Fig. 2 gives the following linear ascending branch in Stage 1

$$k_{t-1A} = \left(-0.0320 \frac{c}{d_b} + 0.576\right) C + 1 \tag{7}$$

For data sets in Table 5, a comparison of the experimental data points with the theoretical predictions of Eqs. 5 and 7, that is  $(k_t)_{exp}/(k_t)_{the}$ , gave a mean of 0.97 and coefficient of variation of 0.16; these are listed in the second column in Table 6. Equations 5 and 7 are plotted for all the data sets in Fig. 3 with reasonable correlation.

	Proposed model	Bhargava et al. (2007)	Cabrera (1996)	Chung et al (2008)	Lee et al (2002)
Mean	0.97	1.12	1.14	1.17	1.12
COV	0.16	0.22	0.24	0.22	0.25
Confidence intervals	0.72 - 1.22	0.71 - 1.54	0.68 - 1.60	0.74 - 1.59	0.66 - 1.58

Table 6 Comparison of experimental and theoretical bond strengths

#### 3.3 Stage 3

It can be seen in Fig. 3 that the transition from Stage 2 to Stage 3 is difficult to pinpoint as any scatter in the Stage 2 results may make the results appear to be Stage 3. To overcome this, only corrosion levels greater than 10% were used to quantify Stage 3 as shown in Fig. 5.



Figure 5 Stage 3 Descending

The linear regression is given by

$$k_{t-3} = -0.0016C + 0.224 \tag{8}$$

where the intercepts between Stages 2 and 3 occur at

$$C_{2-3} = \frac{-1.20 - 0.0475 \frac{c}{d_b} + 3.94 \times 10^{-3} \left(\frac{c}{d_b}\right)^2}{0.0137 \frac{c}{d_b} - 0.245}$$
(9)

which is plotted for all the data sets in Fig. 3.

3.4 Comparison with published models

The published models referenced in Table 6 apply to any strength of concrete, are based on mass loss due to corrosion and have been written in terms of  $k_t$  in Column 2 in Table 7. They have been compared with the Stage 2 data sets in Table 5; the statistical analysis of  $(k_t)_{exp}/(k_t)_{the}$  are summarised in Table 6 where it can be seen that the new model has reduced the scatter.

References	
Cabrera (1996)	$k_t = \frac{\tau_{max}}{\tau_{max0}} = \frac{23.5 - 1.31C}{23.5}$
Bhargava et al. (2007)	$k_t = 1.0$ , for $C \le 1.5\%$

	$k_t = 1.192e^{-0.117C}$ , for $C > 1.5\%$
Lee, Noguchi and Tomosawa (2002)	If $f_c \leq 21$ MPa:
	$k_t = \frac{\tau_{max}}{\tau_{max0}} = 1$ , for $C < \frac{\ln \left(\frac{(0.34f_C - 1.93)}{5.21}\right)}{-0.0561} \%$
	$k_t = \frac{\tau_{max}}{\tau_{max0}} = \frac{5.21e^{-0.0561C}}{0.34f_c - 1.93}, \text{ for } C \ge \frac{\ln\left(\frac{(0.34f_c - 1.93)}{5.21}\right)}{-0.0561}\%$
	If $f_c > 21$ MPa:
	$k_t = \frac{\tau_{max} - 5.21e^{-0.0561C}}{\tau_{max0} - 5.21}$
Chung, Kim and Yi (2008)	$k_t = 1$ , for C $\le 2.0\%$
	$k_t = \frac{24.7C^{-0.55}}{16.87}$ , for $C > 2.0\%$

#### 4. Bond-slip corrosion model

Having quantified in Section 3 the bond-strength  $\tau_{max}$  in the bond-slip variation in Fig. 1, all that is now required is  $\delta_1$  and K<sub>s</sub>; these have already been extracted from the data sets in Fig. 4 and are listed in Table 3. To mirror the research approach in Section 3, the ordinate in Fig. 4 has been normalised by dividing by  $\tau_{max0}$ , which are the corresponding values in Table 3 at zero C. This adjustment to K<sub>s</sub> in Table 3 is listed as K<sub>s1</sub>; there are no values for N16-N18 as  $\tau_{max0}$  had not been measured experimentally. A plot of K<sub>s1</sub> against  $\tau_{max}/\tau_{max0}$  showed no correlation and, furthermore, that the points for N20 and N21 could be considered as outliers (Feng 2014). Ignoring the outliers, the average value for K<sub>s1</sub> was -0.161 so that the slope K<sub>s</sub> can be taken as the following in which the units are in N and mm.

$$k_s = -0.161 \times \tau_{max0} \tag{10}$$

A statistical analysis of  $\delta_1$  in Table 3 had an average value of 0.175 mm, showed large scatters and was unable to find a correlation (Feng 2014). It can be seen in Fig. 4 that the slip  $\delta_1$  at the maximum shear  $\tau_{max}$  is very small compared with the slips associated with the falling branches and hence the measurement of these slips are prone to experimental error. It will be shown in the following section that although more research data is required to accurately quantify  $\delta_1$  is not an important parameter so that the average value can be taken, that is

$$\delta_1 = 0.175 \ mm \tag{11}$$

Also shown in the following section, an important parameter for debonding is the slip limit  $\delta_{max}$  in Fig. 1. It can be seen in Fig. 1 that  $\delta_{max}$  depends on both  $\delta_1$  and K<sub>s</sub>. Hence using Eqs. 10 and 11

$$\delta_{max} = 0.175 - \frac{\tau_{max0}k_t}{k_s} \tag{12}$$

where the units are in mm. The theoretical bond-slips from the above analyses are plotted as 'Model' in Fig. 4. A comparison with the experimental values in Fig. 4 that is the unbroken line shows that apart from N7 and N8 there appears to be good correlation.

#### 5. Debonding of corroded reinforcing bars

The effect of corrosion on the degradation of the bond-slip properties has been quantified above. These properties can be used in numerical simulations such as finite element analyses or segmental analyses (Visintin et al. 2013; Zhang et al. 2014; Knight et al. 2014). However just as an example of its application as opposed to a detailed study, let us now consider the effect of the degradation of the bond-slip on the strength of the steel reinforcing bar.

The strength of a steel reinforcing bar is the lesser of either its yield capacity

$$P_{yld} = A_r f_y \tag{13}$$

or its resistance to debonding, that is its partial-interaction intermediate crack (IC) debonding resistance (Seracino et al. 2007; Haskett et al. 2008; Haskett et al. 2009; Muhamad et al. 2012; Visintin et al. 2012) of which one form (Haskett et al. 2009) is given by

$$P_{IC} = \sqrt{\tau_{max} \delta_{max}} \sqrt{L_{per} E_r A_r}$$
(14)

in which:  $A_r$  is the cross-sectional area of the bar allowing for loss of area due to corrosion;  $f_y$  is the yield capacity of the reinforcing bar;  $E_r$  is the modulus of the reinforcing bar; and  $L_{per}$  is the circumference of the reinforcing bar prior to corrosion that is  $\pi d_b$ . It can be seen in Eq. 14 that  $P_{IC}$  is proportional to the product  $\tau_{max} \delta_{max}$ .

To illustrate the effect of corrosion on P<sub>yld</sub> and P<sub>IC</sub>, consider reinforcing bars in RC members in which: the cover c is 40 mm; yield strength  $f_y = 500$  MPa; bar modulus  $E_r = 200$  GPa; and a concrete strength  $f_c = 40$  MPa for which the peak bond stress for unconfined concrete was taken as  $\tau_{max0} = 6.32$  MPa (CEB-FIP 1993). The variations of the bond-slip properties for a 16 mm diameter bar are shown in Fig. 6 where the ascending branches are also shown as linear. For the uncorroded case that is C = 0:  $\tau_{max} = 6.32$  MPa;  $\delta_{max} = 6.39$  mm; and  $\delta_1 = 0.175$  mm. It can be seen in Fig. 6 that  $\delta_1$  is at least one order of magnitude smaller than  $\delta_{max}$ . Hence any error in the estimation of  $\delta_1$  as discussed previously has only a very minor effect on the overall bond-slip. It can also be seen in Fig. 6 that the area under each bond-slip, that is  $\tau_{max} \delta_{max}/2$ , which is proportional to  $P_{IC}$  as in Eq. 14, rapidly diminishes with corrosion, that is the debonding resistance  $P_{IC}$  rapidly diminishes with corrosion.



Figure 6 Variation of bond-slip with corrosion for 16 mm diameter bar

The variation of bond-slip with bar diameter at 6% corrosion is shown in Fig. 7. It can be seen that the areas under the plots  $\tau_{max} \delta_{max}/2$  diminishes rapidly with increase in bar diameter such that large diameter bars are much more susceptible to debonding due to corrosion than small diameter bars.



Figure 7 Variation of bond-slip with bar diameter



Figure 8 Debonded resistance

The effect of corrosion on the yield capacity from Eq. 13 and on the IC debonding resistance from Eq. 14 are plotted in Fig. 8. At zero corrosion, C = 0,  $P_{IC}$  is much larger that the yield capacity  $P_{yld}$  ranging from about twice as much for large diameter bars to 4<sup>3</sup>/<sub>4</sub> times for small diameter bars. Corrosion causes a small reduction in  $P_{yld}$  but a large reduction in  $P_{IC}$ . Where  $P_{IC} > P_{yld}$ , yielding limits the strength. Where  $P_{IC} < P_{yld}$  debonding limits the strength. For large corrosions the 10 mm bars are only slightly below their yield capacity but for 40 mm bars they are about half. Hence large diameter bars are more likely to debond than small diameter bars and their debonding resistance is much less than their yield capacity.

The transition from yielding to IC debonding in Fig. 8 is shown in Fig. 9 where it can be seen that smaller diameter bars can resist higher corrosion levels than large diameter bars. This behaviour, which has also been noted by Fischer and Ožbolt (2013), arises because both the bond stress slip relationship and the partial interaction mechanics of IC debonding are dependent on the bar diameter.


Figure 9 Transition from yield to debonding

The transition in Fig. 9 is given by the following equation

$$C_{tran} = 100 - 200 \sqrt{\frac{E_r \delta_{max} \tau_{max}}{d_b f_y^2}}$$
(15)

which has been developed by equating the IC debonding resistance given by Eq. 14 with the reduced yield capacity of a corroded bar, and in which  $\tau_{max}$  and  $\delta_{max}$  can be determined from Eq. 2 and Eq. 12 respectively.

#### 6. Conclusions

A model for determining the change in the bond-slip properties  $(\tau/\delta)$  of ribbed steel reinforcement due to corrosion has been developed. As this model quantifies the change, it can be used with existing published or code bond-slip models for uncorroded steel reinforcement to estimate the change due to various degrees of corrosion. As the model is based on the change in bond-slip, it was found that the only parameter that needs to be considered is the cover as a proportion of the bar diameter  $(c/d_b)$ . The beneficial effect of early corrosion on the bond-strength  $(\tau_{max})$  has been quantified, as well as the ensuing rapid reduction in bond-strength followed by a very small region with slow deterioration of the bond. The quantified bond-strength of corroded reinforcement is then used in a bond-slip model where it is shown that the slip capacity  $(\delta_{max})$  is also reduced with corrosion. The research is completed with a study of the changes in  $\tau_{max}$  and  $\delta_{max}$  for different diameter bars and for different levels of corrosion. It is then shown through published partialinteraction mechanics how the parameter  $\tau_{max}\delta_{max}$  can be used to quantify reinforcement debonding and how large diameter bars are prone to large reductions in strength compared with smaller diameter bars.

# 7. Appendix

Data sets	Data points	С	$\tau_{max}$ (MPa)	k <sub>t</sub>
	M1_1	0.000	15.8	1.00
	M1_2	2.22	16.4	1.04
	M1_3	2.67	17.9	1.13
	M1_4	3.44	18.4	1.16
	M1_5	3.89	17.1	1.08
	M1_6	4.56	16.4	1.04
	M1_7	5.00	13.6	0.86
	M1_8	5.56	10.7	0.68
M1	M1_9	6.67	5.00	0.32
	M1_10	7.50	4.49	0.28
	M1_11	11.7	3.37	0.21
	M1_12	15.6	3.17	0.20
	M1_13	20.0	2.97	0.19
	M1_14	31.9	2.60	0.17
	M1_15	49.4	2.20	0.14
	M1_16	61.7	1.97	0.13
	M1_17	80.0	1.69	0.11
	M2_1	0.00	15.1	0.97
	M2_2	0.00	15.70	1.01
	M2_3	0.00	15.1	0.97
	M2_4	0.30	20.4	1.32
	M2_5	0.50	21.9	1.41
	M2_6	0.87	23.9	1.54
	M2_7	1.50	22.3	1.44
	M2_8	1.83	21.2	1.37
MO	M2_9	2.66	19.1	1.23
IVI2	M2_10	3.25	17.7	1.14
	M2_11	4.27	14.5	0.94
	M2_12	4.52	14.4	0.93
	M2_13	4.81	10.9	0.70
	M2_14	6.67	9.70	0.63
	M2_15	6.70	7.10	0.46
	M2_16	7.15	3.70	0.24
	M2_17	7.80	2.60	0.17
	M2_18	8.75	3.10	0.20
M3	M3_1	0.00	16.3	1.02

# Table A: Bond-strength individual data points

	M3_2	0.00	15.2	0.95
	M3_3	0.00	16.5	1.03
	M3_4	0.30	19.1	1.19
	M3_5	0.76	21.0	1.31
	M3_6	0.90	21.1	1.32
	M3 7	1.22	19.0	1.19
	M3 8	1.36	20.4	1.28
	M3_9	1.62	18.7	1.17
	M3_10	2.75	15.5	0.97
	M3_11	2.89	16.0	1.00
	M3_12	3.00	14.6	0.91
	M3_13	3.33	13.2	0.83
	M3_14	3.33	13.4	0.84
	M3_15	4.29	10.7	0.67
	M3_16	5.15	7.90	0.49
	M3_17	5.45	4.80	0.30
	M3_18	6.50	4.10	0.26
	M4_1	0.00	15.0	0.97
	M4_2	0.00	16.1	1.04
	M4_3	0.00	15.4	0.99
	M4_4	0.30	19.1	1.23
	M4_5	0.50	19.4	1.25
	M4_6	0.65	19.7	1.27
	M4_7	0.78	18.3	1.18
	M4_8	1.16	17.6	1.14
M4	M4_9	1.67	13.7	0.88
1714	M4_10	1.86	15.7	1.01
	M4_11	2.00	14.4	0.93
	M4_12	2.69	11.8	0.76
	M4_13	2.87	11.4	0.74
	M4_14	3.08	11.6	0.75
	M4_15	3.13	11.7	0.76
	M4_16	3.60	9.60	0.62
	M4_17	4.25	8.00	0.52
	M4_18	4.35	8.00	0.52
	M5_1	0.00	9.10	0.99
	M5_2	0.00	9.40	1.02
	M5_3	0.00	9.20	1.00
	M5_4	2.47	11.2	1.21
M5	M5_5	2.72	11.7	1.27
-	M5_6	4.09	13.0	1.41
	M5_7	4.10	13.0	1.41
	M5_8	4.32	12.2	1.32
	M5_9	4.33	12.2	1.32
Γ	M5_10	6.51	3.20	0.35

	M5_11	8.90	3.70	0.40
	M5_12	8.90	3.00	0.33
	M5_13	14.5	2.10	0.23
	M5_14	14.7	2.00	0.22
	M5_15	18.8	4.30	0.47
	M6_1	0.00	14.0	1.06
	M6_2	0.00	12.3	0.93
	M6_3	0.00	13.5	1.02
	M6_4	1.37	18.0	1.36
	M6_5	1.40	17.9	1.35
	M6_6	1.60	17.0	1.28
	M6_7	1.69	16.9	1.27
M6	M6_8	3.45	9.60	0.72
	M6_9	3.57	8.90	0.67
	M6_10	5.36	3.70	0.28
	M6_11	5.56	3.30	0.25
	M6_12	6.40	5.50	0.41
	M6_13	6.87	6.50	0.49
	M6_14	16.7	2.13	0.16
	M6_15	17.3	1.80	0.14
	M7_1	0.00	12.1	0.82
	M7_2	0.00	17.3	1.17
	M7_3	0.00	15.0	1.01
	M7_4	0.66	18.9	1.28
	M7_5	0.68	17.9	1.21
	M7_6	0.68	18.0	1.22
	M7_7	0.69	19.1	1.29
M7	M7_8	0.84	18.3	1.24
	M7_9	0.88	18.2	1.23
	M7_10	1.60	13.7	0.93
	M7_11	1.69	13.4	0.91
	M7_12	2.66	12.4	0.84
	M7_13	3.81	1.30	0.09
	M7_14	3.81	1.30	0.09
	M7_15	6.27	3.20	0.22
	M8_1	0.00	19.6	0.99
	M8_2	0.00	20.0	1.01
	M8_3	0.77	22.3	1.13
	4	0.80	22.4	1.13
M8	M8_5	0.90	21.7	1.10
	M8_6	0.94	21.5	1.09
	M8_7	1.33	18.5	0.93
	M8_8	3.30	7.50	0.38
	M8_9	3.41	6.80	0.34
	M8_10	4.47	6.30	0.32

	M8_11	7.48	3.50	0.18
	M8_12	7.56	3.50	0.18
	M8_13	8.95	3.00	0.15
	M9_1	0.00	20.9	1.00
	M9_2	0.00	21.7	1.03
	M9_3	0.00	21.0	1.00
	M9_4	0.00	20.4	0.97
	M9_5	0.65	23.8	1.13
	M9_6	0.77	23.5	1.12
MO	M9_7	0.77	23.4	1.11
1119	M9_8	1.70	14.0	0.67
	M9_9	1.72	13.8	0.66
	M9_10	4.45	4.20	0.20
	M9_11	4.86	1.70	0.08
	M9_12	5.14	6.20	0.30
	M9_13	5.46	2.40	0.11
	M9_14	9.90	5.90	0.28
	M10_1	0.00	27.3	0.98
	M10_2	0.00	27.7	1.00
	M10_3	0.00	28.3	1.02
	M10_4	0.31	31.5	1.14
M10	M10_5	0.39	30.7	1.11
IVIIO	M10_6	2.69	7.43	0.27
	M10_7	3.08	6.10	0.22
	M10_8	4.12	3.81	0.14
	M10_9	4.39	3.24	0.12
	M10_10	4.71	2.86	0.10
	M11_1	0.00	21.8	1.00
M11	M11_2	4.00	11.9	0.55
	M11_3	6.10	6.00	0.28
	M12_1	0.00	8.74	1.00
	M12_2	0.12	8.92	1.02
	M12_3	0.16	9.48	1.09
	M12_4	0.24	7.36	0.84
	M12_5	0.32	8.45	0.97
	M12_6	0.43	8.39	0.96
	M12_7	0.62	10.6	1.21
M12	M12_8	0.81	11.3	1.30
	M12_9	1.66	9.72	1.11
	M12_10	4.64	7.50	0.86
	M12_11	5.97	5.68	0.65
	12	8.70	4.45	0.51
	13	8.60	3.75	0.43
	M12_14	9.95	2.54	0.29
	M12_15	9.99	1.40	0.16

	M13_1	0.00	18.5	0.95
	M13_2	0.00	19.4	1.00
	M13_3	0.00	20.3	1.05
	M13_4	0.31	20.3	1.05
	M13_5	0.56	20.3	1.05
	M13_6	0.71	23.2	1.19
	M13_7	1.09	22.6	1.16
	M13_8	2.28	20.4	1.05
	M13_9	2.48	19.6	1.01
M13	M13_10	4.46	17.2	0.89
	M13_11	4.87	16.2	0.84
	M13_12	6.41	14.3	0.74
	M13_13	6.80	14.3	0.74
	M13_14	7.95	12.4	0.64
	M13_15	8.16	12.4	0.64
	M13_16	9.35	10.6	0.55
	M13_17	10.0	12.4	0.64
	M13_18	11.6	8.68	0.45
	M13_19	12.1	4.87	0.25
	M14_1	0.00	5.10	1.00
M14	M14_2	3.50	3.00	0.59
	M14_3	9.50	1.30	0.26
	M15_1	0.00	3.11	1.00
M15	M15_2	2.50	2.39	0.77
	M15_3	9.50	0.67	0.22

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# CHAPTER 2

# Manuscript

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By signing the Statement of Authorship, each author certifies that:

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#### Quantifying through bond mechanics the effect of steel bar corrosion on the flexural capacity of

#### **RC beams**

Feng, Q., Visintin, P., Oehlers, D.J.

#### Abstract

Steel reinforcing bar corrosion is a major concern in reinforced concrete (RC) structures. Two problems have to be tackled: determining the rate of corrosion which is a material property; and secondly, determining the effect of corrosion on the behaviour of the RC structure not just at serviceability but also at the ultimate limit state which is a mechanics problem. This paper deals with the latter at the ultimate limit state, that is, the quantification through mechanics of the effect of a known amount of corrosion on the flexural capacity of RC beams with corroded longitudinal steel reinforcement. A partial interaction numerical procedure is described for quantifying the effect of corrosion at the ultimate limit state. The procedure quantifies: the flexural capacity and ductility prior to debonding that is whilst the corroded bars are still acting as reinforcement; the onset of debonding; and the flexural capacity and ductility after debonding whilst the corroded bars are acting as tendons. Hence the partial interaction numerical model can be used in design to quantify the effect of gradual corrosion on RC structures and also in assessment to quantify the effect of known corrosion within an existing member. It is shown through mechanics that the onset of debonding through the deterioration of the bond through corrosion is not necessarily a major or catastrophic problem as the RC beam can still have significant strength and ductility both of which are quantifiable. Furthermore, it is shown that corrosion has to occur in critical regions and over large critical lengths, also quantifiable, to significantly affect the behaviour at the ultimate limit state.

**Keywords:** reinforced concrete; beams; steel corrosion; durability; debonding; flexural strength; and flexural ductility.

#### Notation

- b = width of prism
- c = cover to reinforcing bar
- C(x%) = x% corrosion by mass
- d = diameter of bar

 $d_{NA}$  = depth from compression face to neutral axis

d<sub>tend</sub> = distance from neutral of debonded bar acting as a tendon

- E<sub>c</sub> = elastic modulus of concrete
- E<sub>s</sub> = elastic modulus of steel reinforcement
- E<sub>sh</sub> = strain hardening modulus of steel reinforcement
- (EA)<sub>r</sub> = axial rigidity of corroded reinforcement
- FI = full interaction i.e. no interface slip
- FRP = fibre reinforced polymer
- f<sub>c</sub> = concrete compressive cylinder strength
- fy = yield strength of steel reinforcement
- h = depth of prism
- IC = intermediate crack
- K = crack opening stiffness
- $K_t = K$  of top layer of tension reinforcing bars
- $K_{x\%} = K$  of bar with x% corrosion
- L = half span of simply supported beam
- $L_{crt}$  = bond length required to develop  $P_{IC}$
- L<sub>db</sub> = debonded length of reinforcing bar
- $L_{def}$  = half length of segment over which Euler-Bernoulli deformation occurs
- $L_{FI}$  = length over which there is no interface slip i.e. full interaction
- $L_{\mbox{\scriptsize per}}$  = perimeter length of uncorroded reinforcing bar
- $L_{PI}$  = length over which there is interface slap that is partial interaction
- L<sub>wdg</sub> = length of softening wedge
- M = moment
- M<sub>asc</sub> = moment at which the concrete ascending branch is fully developed; moment at the onset
  - of hinge formation

M<sub>des</sub> = moment at which the concrete descending branch is fully developed; moment when hinge is

fully formed

M<sub>fail</sub> = maximum stable moment after which the moment capacity reduces rapidly

 $M_{IC}$  = moment at which  $P_{IC}$  is first achieved

M<sub>max</sub> = maximum moment of the moment distribution applied to beam

P = force; force profile; force in reinforcing bar

- $P_{cc}$  = force in concrete in compression
- P<sub>IC</sub> = IC debonding resistance of reinforcing bar; maximum force in bar that can be developed by

bond stresses alone

 $P_{IC-x\%} = P_{IC}$  of bar with x% corrosion

- P<sub>rc</sub> = force in reinforcement in compression
- P<sub>rtt</sub> = force in reinforcement in tension at top layer
- P<sub>rtb</sub> = force in reinforcement in tension in bottom layer
- $P_{vld}$  = P to cause yield in reinforcing bar

 $P_{yld-x\%} = P_{yld}$  with x% corrosion

 $P_{yld-0} = P_{yld}$  with zero percentage corrosion

PI = partial interaction i.e. interface slip

RC = reinforced concrete

S<sub>cr</sub> = crack spacing

S<sub>cr-pr</sub> = primary crack spacing

 $w_{cr}$  = crack width at level of reinforcing bar

- $\alpha$  = angle of sliding wedge
- $\chi$  = curvature

 $\chi_{asc}$  = curvature at  $M_{asc}$ 

 $\chi_{des}$  = curvature at  $M_{des}$ 

 $\chi_{\text{fail}}$  = curvature at  $M_{\text{fail}}$ 

 $\chi_{yld}$  = curvature at M<sub>yld</sub>

 $\Delta = \delta$  at crack face

- $\Delta_b = \Delta$  of bottom layer of tension reinforcement;  $2\Delta_b$  is the crack width at level of bottom layer of tension reinforcement
- $\Delta_t = \Delta$  of top layer of tension reinforcement;  $2\Delta_t$  is the crack width at level of top layer of tension reinforcement
- $\delta$  = bond slip; deformation profile; longitudinal deformation in a beam

 $\delta_{\text{1}}$  =  $\,\delta$  at  $\delta_{\text{max}}$ 

- $\delta_{\text{anch}}$  = slip of anchorage; slip of mechanical anchorage;  $\delta_{\text{max}}$  when only bond stress
- $\delta_{\text{ext}}$  = extension of reinforcing bar due to debonded region;  $\epsilon_{\text{IC}} \mathsf{L}_{\text{db}}$
- $\delta_{\text{max}}$  =  $\delta$  when  $\tau$  tends to zero with increasing slip
- $\delta_{\text{max-0}} = \delta_{\text{max}}$  of uncorroded bar
- $\delta_{max-x\%} = \delta_{max}$  at x% corrosion
- $\delta_{\text{rb}}\,$  = total deformation of reinforcing bar along L\_db;  $\,\delta_{\text{max}}$  +  $\epsilon_{\text{IC}}\text{L}_{\text{db}}$
- $\delta_{\text{RC}}$  = total deformation of RC member along L<sub>db</sub> at the level of the debonded bar that is d<sub>tend</sub> from

neutral axis

- $\epsilon$  = strain; strain profile
- $\epsilon_{IC}$  = strain when force in bar is P<sub>IC</sub>; P<sub>IC</sub>/(EA)<sub>r</sub>
- $\epsilon_{\text{pk}}$  = train at peak concrete stress  $f_{\text{c}}$

 $\epsilon_{\text{RC}}$  = strain in RC member at level of the debonded reinforcement

- $\epsilon_{\text{u}}$  = maximum softening strain when stress tends to zero
- $\epsilon_{u\text{-model}}$  =  $\epsilon_u$  for  $L_{def}$  of segment being analysed
- $\boldsymbol{\theta}$  = rotation of a single cack face
- $\theta_T$  = total rotation of segment imposed by Euler Bernoulli deformation;

 $\sigma$  = stress profile

 $\sigma_c$  = possible concrete stress profile  $\tau$  = bond shear stress  $\tau_{x\%}$  = bond shear stress at x% corrosion  $\tau_{max}$  = maximum bond shear strength  $\tau_{max-x\%}$  =  $\tau_{max}$  at percentage corrosion  $\tau_{max-0}$  =  $\tau_{max}$  of uncorroded bar

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- Figure 3: Member debonding mechanism
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- Table 1: Beam results with varying corrosion
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#### Introduction

Steel reinforcement corrosion is the principal form of deterioration in RC structures. Corrosion influences the longitudinal reinforcement in two ways: firstly the loss of area associated with corrosion leads to a reduction in the total force that can be carried; and secondly the products of corrosion exert stresses within the surrounding concrete leading to more extensive cracking and weakening of the bond between the reinforcement and the surrounding concrete (Al-Sulaimani et al., 1990; Almusallam 2001; Bhargava et al., 2007; Stanish et al., 1999). This latter reduction in bond leads to a loss of serviceability as it causes increased crack widths and a reduction in tension stiffening and, therefore, increased deflections. Moreover, the reduction in bond may lead to local or global debonding of the reinforcement (Haskett et al., 2008) thus limiting strength and ductility at the ultimate limit state which is the subject of this paper. While much experimental research exists particularly on the repair of corroded structures (Bertolini et al., 2013; Broomfield 2002; Lee et al., 2000; Miyagawa 1991), there is significantly less theoretical research, and thus guidance to practitioners, regarding the prediction through mechanics of the residual strength of members with corroded reinforcing bars (Castel et al., 2000; Coronelli and Gambarova 2004; Jin and Zhao 2001; Mangat, P S and Elgarf, M S 1999) particularly after partial debonding of the longitudinal bars (Eyre and Nokhasteh 1992; Yuan and Marosszeky 1991).

In previous research utilising published test results (Al-Sulaimani et al., 1990; Almusallam et al., 1996a; Amleh and Ghosh 2006; Cabrera and Ghoddoussi 1992; Fang et al., 2006; Jin and Zhao 2001; Lee et al., 2002; Yalciner et al., 2012), Feng et al. (2016b) developed a new local bond-stress/slip ( $\tau/\delta$ ) relationship to describe the change in bond between corroded longitudinal bars and the surrounding concrete as illustrated in Figure 1 where: in the ordinate  $\tau_c$  is the interface shear stress between the bar and adjacent concrete for reinforcement with *C*% corrosion by mass;  $\tau_{max-0}$  is the maximum bond shear stress of an uncorroded bar that is with 0% corrosion; and in the abscissa  $\delta$  is the slip between the longitudinal bar and adjacent concrete. The results of this research (Al-Sulaimani et al., 1990; Almusallam et al., 1996a; Amleh and Ghosh 2006; Cabrera and Ghoddoussi 1992; Fang et al., 2006; Jin and Zhao 2001; Lee et al., 2002; Yalciner et al., 2012) are summarised in Appendix 1.

The bond-slip O-A-B in Figure 1 is for the uncorroded longitudinal bar, that is C(0%), which can be determined through pull tests (Eligehausen et al., 1982) or from codes (CEB-FIP Model Code 1990: Design Code 1994). The maximum shear stress  $\tau_{max-0}$  occurs at a slip of  $\delta_1$ . The maximum slip capacity is  $\delta_{max-0}$  and for slips greater than  $\delta_{max-0}$ , the bond stress  $\tau_{0\%}$  is zero. In regions of an RC beam where the bond slip is greater than  $\delta_{max-0}$ , the bars will be referred to as unbonded or debonded such that the bars now acts as a tendon anchored at their ends in bonded regions. In regions of the beam where the slip is less than  $\delta_{max-0}$  but greater than zero, the bars will be referred to as bonded and act

as reinforcement and because there is interface slip these regions will also be referred to as partial interaction (PI) regions. Finally in regions of the beam where there is no interface slip that is  $\delta$  is zero, the bars are also acting as reinforcement and these regions will be referred to as full interaction (FI) regions.



Figure 1 Change in interface bond/slip  $(\tau/\delta)$  due to corrosion

The corrosion level C(x%) in Figure 1 signifies the percentage loss of mass due to corrosion. At very low corrosion levels this can be beneficial (Al-Sulaimani et al., 1990; Almusallam et al., 1996a; Berto et al., 2008). This is illustrated at the 1% corrosion O-D-E where the maximum bond shear capacity  $\tau_{max-1\%}$  is greater than  $\tau_{max-0}$  and the slip capacity  $\delta_{max-1\%}$  is greater than  $\delta_{max-0}$ . After which, corrosion reduces both the interface shear capacity  $\tau_{max}$  and slip capacity  $\delta_{max}$  as shown for the 4% and C(x%)corrosion levels for O-F-G and O-H-I respectively.

From the bond-slip properties due to corrosion as illustrated in Figure 1, Feng et al. (2016b) used partial interaction (PI) intermediate crack (IC) debonding mechanics (Oehlers et al., 2015) to quantify the IC debonding resistance of a bar with x% corrosion,  $P_{IC-x\%}$ ; this occurs when the bond-slip properties in Figure 1 are fully developed such that the maximum slip is that for x% corrosion that is  $\delta_{max-x\%}$ . The bar force  $P_{IC-x\%}$  is the maximum force that the interface bond for x% corrosion in Figure 1 can apply to the bar as any further attempt to increase the force in the bar will simply cause greater slip without an increase in force (Haskett et al., 2008; Oehlers and Seracino 2004). The force in the bar is also limited by the yield capacity of the reinforcement  $P_{y/d-x\%}$ , that is the yield stress times the cross-sectional area of the bar less the area lost through corrosion such that  $P_{y/d-0}$  is the yield capacity prior to corrosion.

The variation in the strength of the corroded reinforcement is illustrated in Figure 2. The ordinate is either:  $P_{IC-x\%}/P_{yld-0}$  that is the maximum force in the steel reinforcing bar as limited by the IC debonding strength at x% corrosion  $P_{IC-x\%}$  as a proportion of the yield capacity prior to corrosion  $P_{yld-0}$  that is at C = 0% corrosion; or  $P_{yld-x\%}/P_{yld-0}$  that is the maximum force in the steel reinforcing bar as limited by a sa limited by the yield strength  $P_{yld-x\%}$  as a proportion of  $P_{yld-0}$ .



Figure 2 Capacities of corroded reinforcing bars (Feng et al., 2016b)

The broken line  $P_{yld \cdot x\%}/P_{yld \cdot 0}$  in Figure 2 shows the reduction in the yield capacity due to corrosion which depends only on the reduced cross-sectional area due to corrosion. The unbroken lines  $P_{lc}$ .  $_{x\%}/P_{yld \cdot 0}$  show the change in the IC debonding resistances for various bar diameters *d* that range from 10 mm to 40 mm. It can be seen that  $P_{lc}$  initially increases with corrosion as small amounts of corrosion improve the bond (Al-Sulaimani et al., 1990; Almusallam et al., 1996a; Berto et al., 2008) after which there is a rapid reduction in  $P_{lc}$  with corrosion which is followed by a gradual reduction. Where  $P_{lc \cdot x\%}/P_{yld \cdot 0}$  is greater than  $P_{yld \cdot x\%}/P_{yld \cdot 0}$ , yield will occur before debonding and vice versa. It can be seen that these transition points, shown as dot points in Figure 2, range from 4.1% corrosion for 40 mm diameter bars to 6.6% for 10 mm diameter bars where the scatter of this range is given elsewhere (Feng et al., 2016b). Hence small diameter bars can sustain a higher amounts of corrosion than large diameter bars before debonding. Furthermore after debonding, the smaller diameter bars can resist a higher proportion of their yield capacity than larger diameter bars as shown by the variation after the transition point.

It may be worth noting in Figure 2 that for corrosion levels less than the transition point, the steel bar is acting as bonded reinforcement. In contrast, with corrosion levels greater than the transition point the steel bars are now debonded and subsequently act as tendons. Examples are given for 10 mm bar diameters at the top of Figure 2 where it can be seen that for corrosion levels up to 6.6% the bars remains bonded and act as reinforcement and for higher corrosion levels they acts as tendons. The ranges for 40 mm bars are also shown where the transition occurs at a lower percentage of 4.1%.

In this paper, a new analysis procedure based on the fibre reinforced polymer (FRP) plate debonding work of (Oehlers et al., 2015, 2016) is developed to predict both the strength and ductility of beams with: either bonded bars in which the bars acts as reinforcement that is the longitudinal stress in the bar varies along its bonded length; or with regions of unbonded bars in which the unbonded bars act as tendons with uniform stress along the debonded length. There is already much experimental work on RC beams with bonded bars (Almusallam et al., 1996b; Jin and Zhao 2001; Val et al., 1998) and on RC beams with regions of unbonded bars (Cabrera 1996; Coronelli and Gambarova 2004; Mangat, Pritpal S and Elgarf, Mahmoud S 1999). The aim of this paper is to provide the fundamental mechanics that govern and quantify both behaviours and their interaction. Hence the emphasis of this paper is on simulating the mechanisms that has already been recognised in practice.

In the following, the mechanics of reinforcement debonding is first explained along with a generic procedure for predicting the capacity of beams with unbonded reinforcement. A generic segmental approach, previously developed by the authors (Oehlers et al., 2014a, 2014b), is then summarised as it provides a technique for obtaining through the mechanics of partial interaction: the necessary sectional behaviours of a member with either bonded or unbonded reinforcement; and can directly incorporate the reduction in tension stiffening and increase in crack widths due to deterioration of bond. Examples of the application of the segmental and member approaches are then provided to illustrate the transition from bonded to unbonded behaviour that occurs through corrosion.

#### **Debonding of reinforcement**

Consider the half span of a beam in Figure 3(b) to which a distribution of moment M in Figure 3(a) is applied. The behaviour of the reinforcing bars in the beam in Figure 3(b) are analogous to the pull test in Figure 3(c) in which the reinforcing bars are encased in a prism of width b and depth h as shown on the right hand side of Figure 3(b); full descriptions of this analogy are given elsewhere (Oehlers et al., 2015, 2016). Figures 3(c-e) describe the stages of debonding.



Figure 3 Member debonding mechanism

Consider at first the moment distribution OA in Figure 3(a) where the maximum moment  $M_A$ , that is at the mid-span at A, is less than the IC moment  $M_{IC}$  which is the moment when the force in the bar first reaches  $P_{IC}$ . In this case, the force in the reinforcing bar P in Figure 3(b) is less than  $P_{IC}$  for that reinforcing bar of diameter d and corrosion level x%. The force P in Figure 3(b) induces an interface

slip  $\delta$  which at the crack face will be referred to as  $\Delta$  as shown and which is also half the crack width  $w_{cr}$  at the level of the reinforcing bar. The analogous pull test (Oehlers et al., 2015, 2016) is shown in Figure 3(c) where the slip of the bar from the crack face is  $\Delta$  for the force *P*. The relationship between *P*,  $\Delta$  and the distribution of  $\tau$  over the length  $L_{Pl}$ , in which there is partial interaction that is slip, can be derived from PI tension stiffening numerical analyses (Oehlers et al., 2014a) using the appropriate bond-slip characteristics in Figure 1. As *P* in Figure 3(c) is less than  $P_{lC}$ , the bond stresses  $\tau$  are not fully developed, that is the integral of these shear stresses over the bonded area along  $L_{Pl}$  has not reached its maximum value, because the slip  $\Delta$  is less than  $\delta_{max}$ .

Now consider the moment distribution OB in Figure 3(a) where the maximum moment is  $M_{IC}$  such that the bar force P in Figure 3(b) is now  $P_{IC}$  and the half crack width at the level of the reinforcement  $\delta$  is now  $\delta_{max}$  as shown in Figure 3(d). In this case, the shear stresses  $\tau$  in Figure 3(d) are fully developed over a length of  $L_{crt}$ . The strain in the bar at the crack face due to  $P_{IC}$  is  $\varepsilon_{IC}$  that is  $P_{IC}/(EA)_r$  where  $(EA)_r$  is the axial rigidity of the reinforcing bar. Any further increase in  $\Delta$  beyond  $\delta_{max}$  in Figure 3(d) as in Figure 3(e) results in no change in the bond stress distribution, that is the force in the bar remains at  $P_{IC}$ . However, the further extension of the bar  $\delta_{ext}$  in Figure 3(e) can only be accommodated through debonding over length  $L_{db}$  in Figure 3(e), such that extension of the bar  $\delta_{ext}$  is equal to  $\varepsilon_{IC}L_{db}$  so that the total slip of the bar relative to the crack face  $\Delta$  is given by

$$\delta_{rb} = \delta_{max} + \varepsilon_{IC} L_{db} \tag{1}$$

The slip  $\delta_{rb}$  in Figure 3(e) is the half crack width at the level of the bar. Within the length  $L_{db}$ , the bar is debonded because the slip is greater than  $\delta_{max}$ . Within  $L_{crt}$ , the bar is bonded but because the slip is finite there is partial interaction and beyond  $L_{crt}$  where the slip  $\delta$  is zero, in the region labelled  $L_{Fl}$ , there is full interaction.

Following debonding in the beam in Figure 3(b), the flexural cracks close within the debonded region  $L_{db}$  (Liu et al., 2007; Oehlers et al., 2015, 2016) as in Figure 3(f). The force within the reinforcement is constant at  $P_{IC}$  over the debonded region  $L_{db}$ . Consequently, the beam within the debonded region  $L_{db}$  acts as a passively prestressed member with a passive prestress  $P_{IC}$  (Oehlers et al., 2015, 2016), that is the bars within  $L_{db}$  now act as tendons with a constant axial load  $P_{IC}$ . In the passively prestressed region as per the analogy with the pull test in Figure 3(e), the total extension of the bar over the unbonded region  $L_{db}$  is given by Eq. 1. In order to satisfy the requirements of compatibility,

the total deformation of the RC beam at the level of reinforcement  $\delta_{RC}$  over the length  $L_{db}$  must be equal to the total deformation of the tendon  $\delta_{rb}$ , that is

$$\delta_{RC} = \int_0^{L_{db}} \varepsilon_{RC} = \delta_{rb} \tag{2}$$

where  $\varepsilon_{RC}$  is the effective strain in the RC beam at the level of the tendon.

To determine the capacity of the beam with unbonded reinforcement in Figure 3(f), it is a question of varying the moment distribution in Figure 3(a) until either total debonding of the reinforcement occurs or the moment capacity is satisfied through concrete softening. It is important to note that in order for the force  $P_{IC}$  to be developed in the reinforcement, a portion of the bar of length  $L_{crt}$  in Figure 3(f) must be bonded. Closed form solutions (Haskett et al., 2008) for  $L_{crt}$  and  $P_{IC}$  are given in Appendix 2, although, in this paper they have been determined through numerical analyses (Oehlers et al., 2014a).

It is necessary to develop an analysis procedure which can simulate the sectional behaviour of a member with corroded reinforcement in both the bonded and unbonded state. Here a segmental analysis procedure previously developed and validated widely for conventional and prestressed members by the authors (Knight et al., 2013b) is summarised as a potential solution technique in the following. However any analysis procedure capable of simulating the mechanics of the segmental analysis can be applied.

#### Segmental analysis

The segmental analysis procedure has been previously developed by the authors to simulate the full range of behaviours of RC (Oehlers et al., 2014b) and prestressed concrete (Knight et al., 2013b) members. The benefit of the approach is that it directly simulates the localised behaviours that control the global behaviour of reinforced concrete through the application of established partial interaction theory (Oehlers et al., 2014a); inputs of which are the local bond stress slip  $\tau / \delta$  relationship and concrete softening. This approach directly simulates crack formation, widening and tension stiffening and can through mechanics directly simulate the time effects of creep and shrinkage (Knight et al., 2013a; Visintin et al., 2013) although these time effects will not be considered in this paper. Moreover, either through the direct application of shear friction theory

(Visintin et al., 2012), or through the use of a size dependent stress strain relationships (Chen et al., 2013), the approach simulates the formation and failure of concrete softening hinges. As the approach is now well established and validated, only a brief presentation is given here and readers are referred to (Oehlers et al., 2014a, 2014b) for a more detailed explanation and discussion. However as already stated above, any convenient approach could be used to derive the sectional properties required for the debonding analysis, that is the debonding analysis does not depend specifically on the results from a segmental analysis.

#### Segmental analysis prior to reinforcement debonding

A segment of length  $L_{def}$  in Figure 4(b) has been extracted from an RC beam such as in Figure 3(b) (Oehlers et al., 2014b; Visintin et al., 2012); the segment length  $L_{def}$  in Figure 4(b) needs to encompass the length of the concrete softening wedge  $L_{wdg}$  which equals  $d_{NA}/\tan \alpha$  (Oehlers et al., 2014b) where  $\alpha$  is the angle of the sliding wedge as shown and can be taken as 26°. Imposing the Euler Bernoulli deformation in Figure 4(c) on the right hand side of the segment in Figure 4(b) causes a total rotation of the segment end of  $\theta_T$  in Figure 4(c) which is equal to the sum of rotations at each crack face; in the case shown  $\theta_T$  is equal to  $3\theta$  where  $\theta$  is the rotation of an individual crack face. For analysis, it is now a matter of determining the corresponding moment M to achieve  $\theta_T$ .

In the uncracked regions of the beam in Figure 4(b) that is within the depth  $d_{NA}$ , the longitudinal deformation in Figure 4(c) divided by  $L_{def}$  gives the strain profile in Figure 4(d). Based on this distribution of strain, the distribution of stress in Figure 4(e) in the uncracked region can be determined from: the compression reinforcement secant moduli that is the stress strain relationship whether linear or non-linear; the concrete secant moduli prior to compression softening as in Distribution A in Figure 4(g) (Hognestad et al., 1955); and the size dependent effective concrete moduli (Chen et al., 2013) after softening as in Distribution B which allows for the formation of wedges. From the stress distributions in Figure 4(e) can be determined the resultant compressive force in the concrete that is  $P_{cc}$  in Figure 4(f) and that in the reinforcement  $P_{rc}$ . The analysis could include the tensile force in the uncracked concrete just below  $d_{NA}$  but it is common practice to ignore this at the ultimate limit state.

For reinforcement crossing a crack in Figure 4(b), the strain in the reinforcement is not equal to the strain in the concrete at the same level, that is full interaction cannot be assumed. For example in the top layer of the tension reinforcement, the tensile reinforcement force  $P_{rtt}$  shown in Figure 4(f) is a function of the slip of the reinforcement from an individual crack face  $\Delta_t$  in Figure 4(b). The

relationship between  $P_{rtt}$  and  $\Delta_t$  is the crack opening stiffness  $K_t$  and can be determined from established partial interaction theory applied either numerically (Knight et al., 2013a; Visintin et al., 2013) or from mechanics (Muhamad et al., 2012) or from semi mechanical expressions (Zhang et al., 2016) and which depend on the bond-slip properties ( $\tau/\delta$ ). Similarly for the bottom layer of tension reinforcement,  $P_{rtb}$  in Figure 4(f) depends on  $\Delta_b$  in Figure 4(b) that is the slip at an individual crack face and not the total slip  $3\Delta_b$  in Figure 4(c).



Figure 4 Segmental analysis prior to debonding



Figure 5 Results of segmental analyses – M/ $\theta$  and M/ $\chi$ 

Having determined the longitudinal forces in the reinforcement and concrete in Figure 4(f), the Euler Bernoulli deformation in Figure 4(c) can be moved up or down until equilibrium of longitudinal forces is obtained. After which, the moment corresponding to the rotation of the segment end  $\theta_{T}$  in Figure 4(c) can be determined by taking moments of the forces in Figure 4(f) at any level. The above analysis can be repeated for a range of rotations to produce the full moment rotation  $M/\theta$  relationship such as the unbroken line in Figure 5 labelled 'bonded'; dividing the rotation  $\theta$  by the half segment length  $L_{def}$  in Figure 4(b) gives the moment effective curvature relationship  $M/\chi$  in Figure 5. Importantly this moment effective curvature relationship is different from that obtained from a classical full-interaction moment curvature relationship as it directly allows for bond slip and hence tension stiffening of the reinforcement through the application of partial interaction theory as well as the effects of concrete softening. This bonded analysis can also be used to determine the moment at which debonding of the reinforcement to  $P_{IC}$ .

#### Segmental analysis for unbonded reinforcement

When tension bars debonds that is where the slip exceeds the slip capacity  $\delta_{max}$ , then the bars now act as tendons with a prestress of  $P_{IC}$ . Hence if the bottom layer of tension reinforcement in Figure 4(b) debonds then it is no longer acting as reinforcement but as a prestressing tendon with a force  $P_{IC}$ . There are numerous approaches to performing the analysis of a prestressed member (Oehlers et al., 2016). One way is to: simply replace  $P_{rtb}$  in Figure 4(f) with  $P_{IC}$ ; repeat the analysis described above for the unbonded case that is to move the neutral axis  $d_{NA}$  in Figure 4(b) until equilibrium is achieved i.e. the sum of forces is zero; after which moments must be taken at the level of the tendon, that is at  $d_{NA}$  plus  $d_{tend}$  from the compression face, to obtain the applied moment for the imposed rotation  $\theta_T$ . Should both layers of tension reinforcement debond, then the force in the second layer  $P_{rtt}$  in Figure 4(f) is also replaced by  $P_{IC}$  for that layer. Equilibrium is obtained and the moment taken about the position of the resultant of both prestressing forces.

The above analysis can then be repeated for increasing rotations to produce the moment rotation relationship  $M/\theta$  shown as the broken line in Figure 5 labelled 'unbonded'. From which, dividing  $\theta$  by  $L_{def}$  gives the moment curvature relationship  $M/\chi$  for the unbonded case. Furthermore, multiplying the curvature  $\chi$  by  $d_{tend}$  in Figure 4(b) gives the strain in the RC member at the level of the tendon  $\varepsilon_{RC}$  that is required for the ensuing member debonding analysis.

#### Member analysis

A member debonding analysis is illustrated in Figure 6 for a half span of a symmetrically load simply supported beam. The distribution of moment is shown in Figure 6(a) where distances are measured from mid-span. The maximum applied moment in Figure 6(a) at mid-span is  $M_{max}$  which is greater than  $M_{lc}$  to ensure debonding. Consequently the force in the debonded reinforcement, that is the tendon, is  $P_{lc}$ . The following procedure first assumes that all of the tension reinforcement is debonded, that is it is acting as a tendon with a force  $P_{lc}$ , and then the length of the debonded region  $L_{db}$  is determined through mechanics.



Figure 6 Member debonding analysis through deformations

The variation in the longitudinal strain in the RC beam at the level of the tendon  $\varepsilon_{RC}$  along the length of the beam is shown in Figure 6(b); this can be derived from the distribution of  $\varepsilon_{RC}$  with moment in Figure 5. From Eq. 2, integrating the strains in Figure 6(b) gives the RC beam deformation  $\delta_{RC}$  in Figure 6(c) with respect to mid-span. This is the deformation of the RC beam within a debonded region which in this case is assumed to be the whole half span. From Eq. 1, the deformation of the reinforcement  $\delta_{rb}$  in Figure 6(c) is the accumulation of slip within  $L_{crt}$  in Figure 3(e) which is  $\delta_{max}$  plus the extension of the unbonded plate  $\varepsilon_{IC}L_{db}$ . Hence the slope of  $\delta_{rb}$  is  $\varepsilon_{IC}$  as shown in Figure 6(c) where  $\varepsilon_{IC}$  is  $P_{IC}/(EA)_r$ . The intercept of  $\delta_{rb}$  and  $\delta_{RC}$  in Figure 6(c) is the length of the debonded region from mid-span  $L_{db}$  required for compatibility.

It may be worth noting that  $\delta_{max}$  in Figure 6(c) is the slip accumulated within the bonded region  $L_{crt}$  in Figure 3(e) for which closed form solutions are given in Appendix 2, although, in this paper they have been determined numerically (Knight et al., 2013a). Hence there must be a bonded region of at least  $L_{crt}$  beyond  $L_{db}$  in Figure 6(c) as shown, otherwise, the bar force of  $P_{IC}$  could not be obtained purely through the bond stresses. If the remaining length was less than  $L_{crt}$  then mechanical anchors could

be used (Oehlers et al., 2016) in which case  $\delta_{max}$  would be the slip of the mechanical anchor  $\delta_{anch}$ . However this scenario will not be considered further in this paper.

The analysis in Figure 6(c) is shown in Figure 7 for a range of distributed moments in Figure 6(a) in which the maximum moment  $M_{max-x}$  ranges from  $M_{max-1}$  to  $M_{max-6}$ . Each concrete deformation graph  $\delta_{RC}$  in Figure 7 has been labelled with the maximum moment  $M_{max-x}$ . As the reinforcing bar deformation  $\delta_{rb}$  is independent of the applied moment as can be seen in Eq. 1, there is only one variation A-B-C-D to consider as shown for a specific  $\delta_{max-1}$ .



Figure 7 Interpreting the results of member debonding analyses

From a segmental analysis, the moment at which the force in the bottom layer of the tension reinforcing bars in Figure 4(b) reaches  $P_{IC}$  can be determined as  $M_{IC}$ . Let  $M_{max-1}$  in Figure 7 be  $M_{IC}$ , that is the reinforced concrete deformation  $\delta_{RC}$  in Figure 7 is given by O-E. As the RC deformation O-E lies below the reinforcing bar deformation A-B-C-D, member debonding does not occur as the deformation capacity of the reinforcing bar can easily accommodate that of the RC beam. Increasing the maximum moment to  $M_{max-2}$  causes an intercept at Point B. Hence when the applied moment distribution reaches  $M_{max-2}$  there is rapid unstable debonding from mid-span over the length  $L_{db-B}$  and which then stabilises at the intercept  $L_{db-B}$ . It can now be seen that there are two mechanisms that control member debonding; the onset of  $P_{IC}$ ; and compatibility at the intercept of  $\delta_{rb}$  and  $\delta_{RC}$ . Both are required for member debonding.

Increasing the maximum moment to  $M_{max-3}$  in Figure 7 causes stable debonding from Points B to C, that is the debonded region gradually increases with increasing applied moment from  $L_{db-B}$  to  $L_{db-C}$ . A further increase in the applied moment to  $M_{max-4}$  causes debonding to the beam end. This is theoretically impossible as, as explained previously, a bonded length of  $L_{crt}$  is required to achieve  $P_{lc}$ . However if the reinforcing bar is mechanically anchored at its ends, as might occur with a bend in the bar, such that this mechanical anchor can resist  $P_{lC}$  with a slip  $\delta_{anch} = \delta_{max}$  then the analysis is valid. However if this is not the case, then the mechanics of anchored members can be applied as explained elsewhere (Oehlers et al., 2016).

Now apply a maximum moment that is equal to the RC beam moment capacity  $M_{asc}$ , that is when the ascending branch of the concrete compressive stress/strain is fully developed as in Distribution A in Figure 4(g) (Visintin et al., 2012). This is shown as  $M_{max-5} = M_{asc}$  that is O-K-H in Figure 7. As O-K-H always lies above A-B-C-D, that is there is no intercept, compatibility cannot be achieved, hence  $M_{asc}$ cannot be achieved as the reinforcing bar cannot accommodate the required RC beam deformation. Applying a further rotation to the beam segment will eventually cause the concrete softening stresses in Distribution B in Figure 4(g) to be fully developed. The moment at which this occurs  $M_{des}$ (Oehlers et al., 2014b; Visintin et al., 2012) is usually slightly less than  $M_{asc}$  but it is the moment capacity at maximum ductility. To achieve this moment requires an increase in the RC beam elongation from O-K-H to O-L-I in Figure 7 and once again there is no intercept with the reinforcement elongation emanating from  $\delta_{max-1}$  and, therefore, cannot be achieved.

It may be worth noting that a reduced corrosion increases  $\delta_{max}$  in Figure 1. Hence a reduced corrosion may increase  $\delta_{max-1}$  in Figure 7 to say  $\delta_{max-2}$ . Furthermore a reduced corrosion increases  $P_{IC}$  in Figure 2 consequently increasing  $\varepsilon_{IC}$  from say  $\varepsilon_{IC-1}$  to  $\varepsilon_{IC-2}$  as shown in Figure 7 which raises the reinforcement deformation to J-K-L-M. This allows the intercepts K and L such that in the debonded region of the beam a hinge can start and complete to allow additional ductility. From this analysis it can be seen that corrosion reduces both the strength and ductility and can be designed for. Finally when the reinforcement deformation such as N-P always lies above the reinforced concrete deformation then member debonding does not occur such that the properties of the beam can be derived from a segmental bonded analysis.

As explained previously, rapid and unstable debonding occurs from mid-span to  $L_{db-B}$  in Figure 7 when the maximum applied moment is  $M_{max-2}$ . After which, stable debonding occurs with increased moment. Hence a large amount of corrosion could occur within  $L_{db-B}$  without affecting the moment capacity except in reducing the cross-sectional area which is easily accounted for. Hence the critical

region in a beam is not adjacent to the position of maximum moment as might be expected but is in the region that lies outside  $L_{db-B}$ .

#### Application of member debonding analyses

The above segmental and member debonding analyses have been applied to RC beams with the cross-section in Fig. 8(a). The beam is simply supported with a span of 8m, the steel reinforcement is allowed to strain harden after yielding, and the beam is subjected to a uniformly distributed load. Full details of the analyses are given by Feng et al. (2016b) and examples of the properties used are summarised in Appendix 3.



Figure 8 RC beam sections used in member analyses

For the 28 mm tension reinforcing bars in Figure 8(a):  $P_{yld}$  for different corrosion levels are listed in Column (3) in Table 1; and  $P_{lc}$  from numerical simulations (closed form solutions in Appendix 2 could have been used but would give slightly different values) using the bond properties of the corroded reinforcement in Appendix 1 are listed in Column (2) in Table 1. A comparison of  $P_{yld}$  with  $P_{lc}$  shows that the transition point, that is when the yield capacity exceeds the IC debonding resistance with increasing corrosion as illustrated in Figure 2, lies between 4% and 6% in Table 1; the actual value being 5.7%. Hence debonding does not occur with corrosion levels less than 5.7% for these 28 mm reinforcing bars. Consequently a bonded analysis, as illustrated in Figure 4, applies for the corrosion levels of 0%, 1% and 4% in Table 1 and the remaining higher corrosion levels require an unbonded analysis.

The results of an unbonded analysis using the approach illustrated in Figure 7 and for the section in Figure 8(a) with 8% corrosion in the tension reinforcement, is shown in Figure 9. Increasing the corrosion level to 8% that is beyond the transition point of 5.7% means that  $P_{IC}$  occurs before  $P_{yId}$ .

Consequently member debonding may possibly but not necessarily occur, bearing in mind that the following two criteria are required for member debonding: the attainment of  $P_{IC}$ ; and compatibility along the debonded region.



Figure 9 Member debonding analysis of beam with 8% corrosion

As previously explained, the reinforcement deformation  $\delta_{rb}$  in Figure 9 is independent of the applied moment being dependent on:  $\delta_{max-8\%}$  which in this case is 1.49 mm as shown at the intercept of  $\delta_{rb}$  with the ordinate; and  $\varepsilon_{lC-8\%}$ , which is  $P_{lC-8\%}/(EA)_r$  as explained in Figure 6(c) and which in this case is 0.0018 that is the slope as shown. When the maximum moment  $M_{lC} = 257$  kNm that is when  $P_{lC}$  is first achieved, all of  $\delta_{RC}$  labelled O-E in Figure 9 lies below  $\delta_{rb}$  labelled A-B-C-D so that the deformation of the reinforcement can easily accommodate the RC deformation. Hence member debonding will not occur even though  $P_{lC}$  is attained because compatibility is not achieved. Increasing the applied moment with a maximum of 282 kNm that is deformation O-B-F, causes an intercept at *B* which occurs at  $L_{db-B} = 0.75$  m. Hence rapid and unstable debonding will occur along the length  $L_{db-B}$  of 0.75 m when this moment distribution is applied. As there is unstable debonding within  $L_{db-B}$ , pockets of severe corrosion within this region are not important as the reinforcement has debonded. What is important is the corrosion in the remainder of the beam beyond  $L_{db-B}$  as this affects stable debonding. Hence the critical region is not within  $L_{db-B}$  but outside this region.

A further increase in moment to  $M_{asc}$  = 284 kNm to deformation O-C-G in Figure 9 will cause stable debonding from  $L_{db-B}$  = 0.75 m to  $L_{db-C}$  = 1.51 m; this assumes that the bonded region to the left of  $L_{db-C}$ *c* is greater than  $L_{crt}$ . Increasing the applied deformation to the beam to allow a hinge to form such that  $M_{des}$  = 273 kNm will cause stable debonding to  $L_{db-D}$  = 1.95m. Any further increase in applied deformation to the beam will cause a rapid reduction in the moment capacity so that for all intents and purposes the failure capacity  $M_{fail}$  is in this case  $M_{des}$  = 273 kNm.

An analysis with 40% corrosion in the beam in Figure 8(a) is shown in Figure 10. In this case, maximum moment capacity  $M_{asc}$  is achieved with debonding to  $L_{db-B}$  of 3.48 m but the greatest ductility at  $M_{des}$  is not achievable due to debonding to the end of the beam. If the end of the reinforcement is anchored such as at a hook, then the strength and ductility depends on the properties of the anchor which if known can be used to quantify the beam behaviour using an alternative approach (Oehlers et al., 2016) but this will not be covered in this paper.



Figure 10 Member debonding analysis of beam with 40% corrosion

The beam in Figure 8(a) has been analysed with varying corrosion levels and the results summarised in Table 1. The corrosion levels in Column (1) range from 0% to 40%. For each corrosion level, the IC debonding capacity  $P_{IC}$  is tabulated in Column (2) and the yield capacity  $P_{yld}$  in Column (3). A comparison of  $P_{IC}$  and  $P_{yld}$  shows that  $P_{IC} > P_{yld}$  for corrosion levels up to and including 4% so that a segmental bonded analysis applies in contrast to a segmental and member unbonded analysis for corrosion levels of 6% and more. At 0% corrosion, the failure moment  $M_{fail}$  in Column (12) is equal to  $M_{des}$  in Column (10) of 430 kNm and this occurs at a curvature  $\chi_{fail} = 2.86 \times 10^{-5}$  mm<sup>-1</sup>. It may be worth noting that as rotation  $\theta$  is the curvature  $\chi$  times  $L_{def}$  where  $L_{def}$  is in effect the hinge length then the curvature at failure is directly proportional to the rotation capacity and consequently is a measure of the ductility. At 4% corrosion,  $M_{fail}$  reduces slightly to 409 kNm and the curvature rises slightly to 3.08x10<sup>-5</sup> mm<sup>-1</sup> such that there is only a minor reduction in strength with corrosion and no reduction in ductility.

Increasing the rotation to 6% gives the results in Table 1 from an unbonded segmental analysis. The ability to achieve these values from an unbonded segmental analysis depends on member debonding which itself depends on the debonded length. It can be seen that increasing the corrosion to 6% causes  $M_{fail}$  In Column 12 to reduce by 32% to 280 kNm. However the curvature increases by 57% to 4.84x10<sup>-5</sup> mm<sup>-1</sup> that is the major reduction in strength is in part compensated by a very large increase in ductility which is important for the absorption of energy and the redistribution of moment. At 20% corrosion,  $M_{fail}$  has reduced by 46% but the ductility has increased by 104% compared with 0% corrosion. However at 40% corrosion complete debonding of the reinforcement now governs, causing a major reduction in both strength and ductility; that is member debonding once it occurs can severely reduce both flexural capacity and ductility. Also worth noting is that the debonded region increases with corrosion at failure. In this example, the limit to the ductility due to member debonding is reached somewhere between 20% and 40% corrosion.

The analysis of the simply supported slab or shallow beam in Figure 8(b) of 4m span and with 8% corrosion is shown in Figure 11. In this case, member debonding occurs as soon as the maximum of the applied moment reaches  $M_{IC}$ . There is unstable debonding over  $L_{db-B} = 0.58$  m and then stable debonding until  $M_{des}$  is achieved at  $L_{db-D} = 1.59$ m.

The results of the analysis of the slab in Figure 8(b) with varying degrees of corrosion are given in Table 2. By comparing  $P_{IC}$  with  $P_{yld}$  for the 10 mm bar, it can be seen that the transition point occurs between 7% and 8%. At 7% corrosion, the bonded moment capacity  $M_{fail}$  is 47 kNm at a curvature  $\chi_{fail}$  of 18.7x10<sup>-5</sup> mm<sup>-1</sup>. At 8% corrosion the unbonded moment capacity reduces to 36 kNm that is a 23% reduction from that at 7% which is much less than the step change of 32% that occurred in the previous beam analysis. However, the curvature increases to 24.3x10<sup>-5</sup> mm<sup>-1</sup> that is an increase of 30%. The debonded region is 80% of the span and this increases as corrosion increases to 93% when the degree of corrosion is 15%. It can be seen in Table 2 that at 20% corrosion, member debonding prevents the full ductility from being achieved. Hence the limit due to member debonding is achieved somewhere between 15% and 20% corrosion.


Figure 11 Member debonding analysis of slab with 8% corrosion

# Conclusions

It has been shown that the flexural capacity and flexural ductility capacity that is rotation capacity of a beam with corroded steel reinforcing bars is governed by the following complex partial interaction mechanisms:

- The behaviour whilst the corroded bar acts as bonded reinforcement which can be determined from a segmental analysis.
- The transition from bonded behaviour in which the bar is acting as reinforcement to unbonded in which the bar is acting as a tendon. This transition is governed in part by the IC debonding resistance and the yield capacities of the reinforcing bars.
- The behaviour whilst the corroded bar acts as a tendon which can be determined from a segmental unbonded analysis.
- And finally debonding along the member which can limit the capacities from the segmental unbonded analysis.

A numerical analysis for quantifying the flexural capacity and flexural ductility of RC beams with corroded steel reinforcement has been described. The numerical analysis can quantify: whether member debonding can occur; the strength and ductility should member debonding not occur; and the strength and ductility should member debonding occur and the limits on these capacities due to the span of the members.

It has been demonstrated that the transition from the steel bar acting as reinforcement to acting as a tendon can cause a sudden reduction in the moment capacity which is quantifiable. However this is to some degree compensated by a substantial increase in ductility also quantifiable. It is shown through mechanics that the critical region for corrosion may not necessarily be adjacent to the position of maximum moment as may be thought at first instance. Instead it lies outside a mechanically quantifiable distance where unstable crack propagation occurs. The eventual aim of this research is to provide numerical models to help in the assessment of corroded RC beams and in their retrofitting and in developing simple assessment rules for RC beams and slabs with known corrosion levels.

### Appendix 1 Bond-slip properties of corroded steel reinforcement

The research of (Feng et al., 2016b) derives the change in the bond-slip properties of steel reinforcement due to corrosion as illustrated in Figure 1. Its application requires the bond-slip properties prior to corrosion that is  $\tau_{max-0}$  and  $\delta_{max-0}$  in Figure 1 which can be obtained from tests or from Codes (CEB-FIP Model Code 1990: Design Code 1994). The bond-slip model with corrosion effects consists of a non-linear ascending branch and a linear-descending branch.

In the ascending branch in Figure 1, that is where the slip varies from 0 to  $\delta_1$ ,  $\delta_1$  may be considered as a constant valued at 0.175 mm. The bond shear stress at corrosion level C(x%) that is  $\tau_{x\%}$  is given by

$$\tau_{x\%} = \tau_{max-x\%} \left(\frac{\delta}{\delta_1}\right)^{0.4} \text{ when } 0 \le \delta \le \delta_1 \tag{A1-1}$$

in which  $\tau_{max-x\%}$  is the maximum shear stress at  $\delta_1$  for corrosion level of x% and which is given by

$$\tau_{max-x\%} = k_t \tau_{max-0} \tag{A1-2}$$

where  $k_t$  is given by either

$$k_t = \left(-0.032\frac{c}{d} + 0.576\right)x\% + 1, \text{ when } 0 < x\% < 0.3(x\%)_{1-2}$$
(A1-3)

or

$$k_{t} = \left(0.0137 \frac{c}{d} - 0.247\right) x\% + 1.42 + 0.0475 \frac{c}{d} - 3.94 \times 10^{-3} \left(\frac{c}{d}\right)^{2},$$
  
when  $0.3(x\%)_{1-2} < x\% < (x\%)_{2-3}$ 

(A1-4)

or

$$k_t = -0.0016C + 0.224$$
, when  $x\% > (x\%)_{2-3}$  (A1-5)

in which: x% is the level of corrosion in terms of percentage mass loss; c/d is the ratio of cover to the edge of the bar c and the bar diameter d;  $(x\%)_{1-2}$  is the transition point of corrosion level where the peak bond starts to descend with corrosion; and  $(x\%)_{2-3}$  is the transition point where peak bond starts to level off despite increasing of corrosion level. The transition points  $(x\%)_{1-2}$  and  $(x\%)_{2-3}$  are calculated as follows.

$$(x\%)_{1-2} = 0.288\frac{c}{d} + 1.72 \tag{A1-6}$$

$$(x\%)_{2-3} = \frac{-1.20 - 0.0475\frac{c}{d} + 3.94 \times 10^{-3} (\frac{c}{d})^2}{0.0137\frac{c}{d} - 0.245}$$
(A1-7)

The coefficient  $\tau_{max-0}$  in Eq. (A1-2) is the peak bond in bond-slip model when there is no corrosion which is suggested by the CEB model (CEB-FIP Model Code 1990: Design Code 1994) as

$$\tau_{max-0} = 7 \times (\frac{f_c}{25})^{0.25} \tag{A1-8}$$

where  $f_c$  is measured in MPa.

The descending branch of the bond-slip model with corrosion is described in Eq. (A1-9), where  $\delta_1$  is a constant valued at 0.175 mm and  $\delta_{max-x\%}$  is shown in Eq. (A1-10).

$$\tau = -0.161\tau_{max-0}\delta + 0.0282\tau_{max-0} + \tau_{max-C} \quad \delta_1 \le \delta \le \delta_{max-x\%}$$
(A1-9)

$$\delta_{max-x\%} = 0.175 + 6.21k_t \tag{A1-10}$$

# Appendix 2 IC debonding properties

The IC debonding properties in this paper were derived from numerical analyses that can cope with any bond-slip shape. However, it may be worth noting that there are numerous closed form solutions for the IC debonding properties which depend on specific assumed shapes of the bond-slip (Haskett et al., 2008; Muhamad et al., 2011). The simplest solution is to assume that  $\delta_1$  in Figure 1 tends to zero that is we are only dealing with the linear descending branch (Haskett et al., 2008). In this case, the IC debonding resistance is given by

$$P_{IC} = \sqrt{\tau_{max-x\%} \delta_{max-x\%} \sqrt{L_{per} (EA)_r}}$$
(A2-1)

where  $L_{per}$  is the circumference of the reinforcing bar prior to corrosion and  $(EA)_r$  is the axial rigidity of the reinforcing bar in which the cross-sectional area is reduced allowing for corrosion. Furthermore the critical length required to develop  $P_{IC}$  is given by

$$L_{crt} = \frac{\pi}{2\sqrt{\frac{\tau_{max-x\%}L_{per}}{\delta_{max-x\%}(EA)_r}}}$$
(A2-2)

### Appendix 3 Examples of member properties and analyses

Full details of all the assumed properties and calculations are given elsewhere (Feng et al., 2016a). As an example of the material properties, those for the beam in Figure 8(a) with 8% corrosion in the tension reinforcement are given below.

concrete properties: compressive cylinder strength  $f_c = 40$  MPa; elastic modulus  $E_c = 23.5$  GPa; ascending branch of stress ( $\sigma$ )/strain ( $\varepsilon$ ) provided by Hognestad (1951)  $\sigma$ =[ $2\varepsilon/\varepsilon_{pk}$ -( $\varepsilon/\varepsilon_{pk}$ )<sup>2</sup>] where  $\varepsilon_{pk}$ = (-0.067 $f_c$ +29.9 $f_c$ +1053)10<sup>-6</sup>; linear descending branch (Visintin and Oehlers 2016) starts at  $\varepsilon_{pk} = f_c$  and terminates at  $\varepsilon_u = 0$  where  $\varepsilon_u = \varepsilon_{u-model} \times 100/L_{def}$  where  $L_{def}$  is defined in Figure 4 and  $\varepsilon_{u-model} = \varepsilon_0 + (3+1000\varepsilon_0)/(77f_c$ -500) where  $\varepsilon_0 = 4.76\times 10^{-6}f_c + 2.13\times 10^{-3}$ .

steel properties: tensile yield strength  $f_y$  = 520 MPa; elastic modulus  $E_s$  = 200 GPa,; and the strain hardening modulus  $E_{sh}$  = 2.6 GPa.

bond properties: maximum shear capacity at zero corrosion  $\tau_{max-0} = 7.87$  MPa; maximum slip capacity at zero shear stress  $\delta_{max-0} = 6.34$  mm; slip at  $\tau_{max}$  that is  $\delta_1 = 0.175$  mm; maximum bond shear stress at 8% corrosion  $\tau_{max-8\%} = 1.66$  MPa; slip capacity at 8% corrosion  $\delta_{max-8\%} = 1.49$  mm; transition point in Figure 2 is 5.7%; length of softening wedge  $L_{wdg} = 237$  mm.

Partial interaction pseudo material properties: Primary crack spacing  $S_{cr-pr}$  = 182 mm; IC debonding resistance of 8% corroded bar  $P_{IC-8\%}$  = 804 kN; critical bond length at 8% corrosion  $L_{crt-8\%}$  = 1468 mm; crack opening stiffness at 8% corrosion  $K_{8\%}$  = 400x10<sup>6</sup> N/mm

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Table 1. Beam results with varying corrosion

С	P <sub>IC</sub>	P <sub>yld</sub>	M <sub>IC</sub>	$\chi_{\rm IC} 10^{-5}$	$M_{yld}$	$\chi_{yld} 10^{-5}$	M <sub>asc</sub>	$\chi_{\rm asc} 10^{-5}$	M <sub>des</sub>	$\chi_{des} 10^{-5}$	$M_{\text{fail}}$	$\chi_{fail} 10^{-5}$	$L_{db}/L$
(%)	(kN)	(kN)	(kNm)	$(mm^{-1})$	(kNm)	$(mm^{-1})$	(kNm)	$(mm^{-1})$	(kNm)	$(mm^{-1})$	(kNm)	$(mm^{-1})$	(%)
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)	(13)	(14)
0	1586	1280	-	-	429	1.32	444	1.43	430	2.86	430	2.86	0
1	1663	1267	-	-	428	1.32	435	1.43	431	2.86	431	2.86	0
4	1384	1229	-	-	421	1.32	424	1.43	409	3.08	409	3.08	0
6	828	1203	261	0.68	-	-	292	2.31	280	4.84	280	4.84	46
8	805	1178	257	0.68	-	-	284	2.42	273	4.95	273	4.95	48
10	782	1152	256	0.68	-	-	277	2.42	264	5.16	264	5.16	50
15	726	1088	252	0.70	-	-	258	2.64	247	5.49	247	5.49	58
20	671	1024	238	0.69	-	-	240	2.75	231	5.82	231	5.82	65
40	472	768	174	0.62	-	-	173	3.74	167	7.47	173	3.74	-

# Table 2. Slab results with varying corrosion

C (%)	P <sub>IC</sub> (kN)	P <sub>yld</sub> (kN)	M <sub>IC</sub> (kNm)	$\chi_{IC} 10^{-5}$ (mm <sup>-1</sup> )	M <sub>yld</sub> (kNm)	$\chi_{yld} 10^{-5}$ (mm <sup>-1</sup> )	M <sub>asc</sub> (kNm)	$\chi_{\rm asc} 10^{-5}$ (mm <sup>-1</sup> )	M <sub>des</sub> (kNm)	$\chi_{des} 10^{-5}$ (mm <sup>-1</sup> )	M <sub>fail</sub> (kNm)	$\chi_{fail} 10^{-5}$ (mm <sup>-1</sup> )	L <sub>db</sub> /L (%)
0	518	367	-	-	40.9	2.13	53	12.8	54	16.3	54	16.3	0
1	577	364	-	-	40.2	2.06	55	12.4	55	15.8	55	15.8	0
4	482	353	-	-	39.0	2.21	51	13.3	51	17.1	51	17.1	0
7	383	342	-	-	38.5	2.35	47	14.4	47	18.7	47	18.7	0
8	315	338	36	2.51	-	-	36	18.4	36	24.3	36	24.3	80
10	307	331	35	2.48	-	-	35	19.5	35	25.4	35	25.4	88
15	287	312	33	2.43	-	-	33	20.6	33	27.2	33	27.2	93
20	268	294	31	2.38	-	-	31	21.7	31	29.0	31	21.7	-

# CHAPTER 3

# Manuscript

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Contribution to the Paper	Performed analysis on data processing and programming of numerical models, interpreted data and wrote manuscript.					
Overall percentage (%)	75%					
Certification:	This paper reports on original research I conducted during the period of my Higher Degree by Research candidature and is not subject to any obligations or contractual agreements with a third party that would constrain its inclusion in this thesis. I am the primary author of this paper.					
Signature	Date 19/08/2016					

# **Co-Author Contributions**

By signing the Statement of Authorship, each author certifies that:

- i. the candidate's stated contribution to the publication is accurate (as detailed above);
- ii. permission is granted for the candidate in include the publication in the thesis; and
- iii. the sum of all co-author contributions is equal to 100% less the candidate's stated contribution.

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# A mechanics prediction of reinforcement corrosion in RC beams through the measurement of crack widths

Q. Feng, P. Visintin and D.J. Oehlers

# Abstract

The corrosion of steel reinforcement in reinforced concrete beams is a common occurrence and can be of major concern. The latter stages of corrosion can be detected visually through the occurrence of splitting cracks in line with the reinforcement. This paper shows that a more effective way of monitoring reinforcement corrosion is in measuring the flexural crack widths as this is a direct measure of the deterioration in bond due to corrosion. This paper describes a mechanics based approach for the detection and quantification of steel reinforcing bar corrosion via monitoring of the variation in flexural crack widths under serviceability loading with time. It is shown that continuous measurement of crack widths is a very effective way of monitoring steel corrosion as: it can detect small local areas of corrosion in beam lengths as small as the crack spacings; it is relatively easy to physically measure crack widths; the effects of shrinkage can be easily accounted for; and crack widths are unaffected by concrete creep. In contrast monitoring deflections due to corrosion is difficult as: the results are clouded by concrete creep; it is physically difficult to monitor the whole beam deflection; and beam deflections are insensitive to the effects of localised corrosion and hence the results are only of use should the reinforcement be corroding along the whole span.

*Keywords:* steel reinforcing bars; corrosion; reinforcement corrosion; reinforced concrete beams; monitoring crack widths; crack widths; time effects.

#### Notation

- A<sub>c</sub> = cross-sectional area of concrete prism
- Ar = total cross-sectional area of tension reinforcement
- $B_n$  = bond force in n<sup>th</sup> element of prism
- C = percentage corrosion by weight
- $C_n$  = concrete force in n<sup>th</sup> element of prism
- $C_0 = 0\%$  corrosion
- $C_{1-2} = C$  at transition from Stage 1 to Stage 2; C at start of rapid reduction in bond
- $C_{2-3}$  = C at transition from Stage 2 to Stage 3; C at end of rapid reduction in bond

c = distance from tension reinforcement to tension face; half prism depth

 $D_{co}$  = deflection of beam due to corrosion throughout

 $D_{\text{co-pt}}$  = deflection of beam de to corrosion in part

 $D_{cr}$  = deflection of beam due to creep

D<sub>sh</sub> = deflection of beam due to shrinkage

E<sub>c</sub> = concrete modulus

- E<sub>r</sub> = reinforcement modulus
- k = bond-slip stiffness

 $k(C_0) = k \text{ at } C_0$ 

k(C<sub>2-3</sub>) = k at C<sub>2-3</sub>

L<sub>def</sub> = deformation length in a segmental analysis

L<sub>per</sub> = total circumferential length of tension reinforcement

L<sub>s</sub> = length of prism segment

M = moment

M<sub>s</sub> = serviceability moment

P<sub>cc</sub> = concrete compressive force

P<sub>cr</sub> = force in reinforcing bars at a flexural crack

 $P_n$  = reinforcement force in  $n^{th}$  prism element

 $P_{rc}$  = force in reinforcing bar in compression

S<sub>cr</sub> = flexural crack spacing

T = time

T<sub>0</sub> = time at first monitoring

 $w_{cr}$  = crack width

 $w_{cr0}$  = crack width first measured

 $\Delta_{cr}$  = reinforcement slip at crack face; half crack width  $w_{cr}$ 

 $\Delta_n$  = slip in n<sup>th</sup> prism element

 $\delta \Delta_n$  = increase in slip in  $n^{th}$  element

 $\delta_{\text{1}}$  = bond slip at  $\tau_{\text{max}}$ 

 $\delta_{\text{max}}$  = slip when bond descends at  $\tau\text{=}0$ 

 $\delta_{max}(C) = \delta_{max}$  for 0% corrosion

 $\epsilon_c$  = concrete strain

 $\epsilon_r$  = reinforcement strain

 $\epsilon_{cn}$  = mean concrete strain in n<sup>th</sup> element

 $\epsilon_{rn}$  = mean reinforcement strain in n<sup>th</sup> element

 $\epsilon_{\text{sh}}$  = shrinkage strain

 $\epsilon_{sh0}$  =  $\epsilon_{sh}$  when first measured

 $\varphi_0$  = creep coefficient when first measured

 $\boldsymbol{\theta} = \text{rotation}$ 

 $\tau$  = bond shear stress

 $\tau_{\text{max}}$  = bond shear strength

 $\tau_{max}(C_0) = \tau_{max} \text{ at } C_0$ 

```
\tau_{\text{max}}(\text{C}_{\text{2-3}}) = \tau_{\text{max}} \text{ at } \text{C}_{\text{2-3}}
```

# Figures

- Figure 1: Beam segment components
- Figure 2:  $n^{\text{th}}$  prism element
- Figure 3: Tension stiffening analysis
- Figure 4: Variation of bond strength with corrosion
- Figure 5: Variation in bond-slip with corrosion
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- Figure 7: Monitoring corrosion from crack width
- Figure 8: Monitoring sheet of crack width

Figure 9: Dimensions of the cross-section Figure 10: Variation in crack width with time Figure 11: Monitoring two pairs of cracks Figure 12: Segmental analysis Figure 13: Time dependent beam deflection Figure 14: Change in Deflection with time Figure 15: Varying extent of corrosion

#### Introduction

The corrosion of reinforcement affects virtually all aspects of the behaviour of reinforced concrete. At the serviceability limit state corrosion leads to a degradation of the bond between the reinforcement and the concrete (Almusallam et al., 1996; Cabrera 1996; Feng et al., 2016c; Val et al., 1998), which leads to reduced tension stiffening and increased deflections and crack widths. At the ultimate limit state corrosion leads to a loss of reinforcement area and hence a reduction in strength (Feng et al., 2016a; Jin and Zhao 2001; Mangat and Elgarf 1999). Additionally the degradation of the bond between the reinforcement and concrete may lead to global debonding of reinforcement resulting in a loss of strength and ductility (Eyre and Nokhasteh 1992; Feng et al., 2016b; Val et al., 1998). Given the consequences of corrosion on the performance of reinforced concrete structures, it is vital that engineering practitioners have reliable methods for predicting the level of corrosion of reinforcement.

While several non-destructive electrochemical and transient based techniques are available for predicting reinforcement corrosion (Montemor et al., 2003), these have been reported to be imprecise (Khan et al., 2014). An alternative approach proposed by several researchers (Khan et al., 2014; Rodriguez et al., 1996; Vidal et al., 2004; Zhang et al., 2010) is the prediction of corrosion via correlation of measured longitudinal corrosion crack widths with empirical observations of crack width for known corrosion levels.

In this paper an alternate technique is suggested where it is shown that by monitoring the variation in flexural crack width over time the average level of corrosion between two flexural cracks can be predicted. Importantly this approach, which is based on the mechanics of partial interaction theory, can allow for the combined influence of corrosion and concrete shrinkage and creep (Knight, D et al., 2015; Knight et al., 2013; Visintin et al., 2013a). It also directly makes use of the significant quantity

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of research available which quantifies the variation in the bond between reinforcement and concrete with corrosion, as well as the influence of reinforcing bar diameter, reinforcement cover and concrete strength (Almusallam et al., 1996; Cabrera 1996; Feng et al., 2016c).

The proposed scenario in this paper is that the structural engineer can monitor with time, pairs of adjacent flexural cracks in reinforced concrete (RC) beams or slabs that are in regions of that beam in which there is concern with regard to corrosion. The purpose of this paper is to provide mechanics based approaches for interpreting these monitored results and extracting from them the amount of corrosion. Once the structural engineer has extracted the amount of corrosion, this paper can be used to quantify the effect of the corrosion on serviceability and other published approaches (Eyre and Nokhasteh 1992; Feng et al., 2016b; Yuan and Marosszeky 1991) can be used to determine the effect on the ultimate limit state. It is not the purpose of this paper to try and predict how corrosion will progresses with time. However any predictive model could be used in the analyses procedure described in this paper to predict the effect of further corrosion.

In this paper a partial interaction (PI) numerical segmental analysis of RC beams (Knight et al., 2013; Knight, Daniel et al., 2015; Visintin et al., 2013a) that incorporates the time dependent behaviour of concrete, that is, shrinkage, creep and reinforcement corrosion is first explained. This is followed by a description of the time dependent material properties that can be used in the numerical analyses. These material properties are presented as an example and the readers may substitute any material properties they consider better or more appropriate. The numerical model is then used to illustrate typical variations in crack widths with time which leads to the development of monitoring sheets to help the structural engineer interpret the results of crack width monitoring and, in particular, extract the amount of corrosion between two cracks.

#### PI time dependent mechanics of crack widths

## Tension stiffening mechanics of crack widths

Consider a segment of an RC beam or slab between two flexural cracks of spacing  $S_{cr}$  as shown in Fig. 1(b). Each segment face B-B is subjected to an Euler-Bernoulli displacement A-A as shown that cause rotations  $\theta$ , a constant moment M and a force in the tension reinforcement at the flexural crack of  $P_{cr}$  (Knight, Daniel et al., 2015; Oehlers et al., 2014; Visintin et al., 2013a). Because of the flexural cracks, the tension reinforcement slips relative to the adjacent concrete which is referred to as partial-interaction (PI). It is common practice (Knight et al., 2013; Visintin et al., 2013a) to simulate this PI mechanics using a tension-stiffening prism as in Fig. 1(d) where  $\Delta_{cr}$  is the slip of the

reinforcement relative to the crack face when the force in the reinforcement is  $P_{cr}$  and is equivalent to the half crack width at the level of the tensile reinforcement  $w_{cr}/2$ .

The tension stiffening prism in Fig. 1(c) has a total concrete cross sectional area  $A_c$  and is reinforced with a total area of tensile reinforcement  $A_r$  which has a total bonded perimeter  $L_{per}$ . For analysis the height of the tension stiffening prism is taken such that the reinforcement is located at the centroid c.



Figure 1 Beam segment components

The prism in Fig. 1(d) is divided into x small lengths of  $L_s$  as shown (Knight et al., 2013; Visintin et al., 2013a). The  $n^{th}$  element is shown in Fig. 2. Prior to concrete shrinkage, at a strain  $\varepsilon_{sh}$ , the left hand side (LHS) of the element is located at D-D and the right hand side (RHS) at A-A; the latter will also be used as a base line to measure all deformations. On the application of a concrete shrinkage strain  $\varepsilon_{sh}$ , the concrete face D-D, when unrestrained, will move to the right  $\varepsilon_{sh}L_s$  to B-B shown in Fig. 2(b); this is the unstressed concrete state and any straining from this position  $\varepsilon_{cn}$  will cause a concrete stress. In contrast as the reinforcement does not shrink, any reinforcement straining  $\varepsilon_m$  relative to D-D will cause a stress in the reinforcement.

The force in the reinforcement on the LHS of the  $n^{th}$  element in Fig. 2 is  $P_n$  and the slip is  $\Delta_n$  as shown. The interface bond force  $B_n$  in Fig. 2(b) can be derived from the bond-slip properties for  $\Delta_n$  and the surface over which it acts  $L_{per}L_s$ . Hence the force in the reinforcement reduces to  $P_n$ - $B_n$  on the RHS. The mean of the reinforcement force can be used to derive the mean reinforcement strain  $\varepsilon_{rn}$  which causes an extension  $\varepsilon_{rn}L_s$  as shown. The force on the concrete is  $C_n$  on the LHS and increases by  $B_n$  to that on the RHS as shown, and the mean strain in the concrete is  $\varepsilon_{cn}$  which causes an extension  $\varepsilon_{cn}L_s$  also shown. Hence the change in slip  $\delta\Delta_n$  as shown where the strain component in brackets is referred to as the slip strain  $d\Delta/dx$ .



Figure 2  $n^{\text{th}}$  prism element

The PI analysis depicted in Fig. 2 is applied to the first two elements in Fig. 1(d) in Fig. 3. Consider the first element which is adjacent to the flexural crack in Fig. 3(a). The steps in the numerical analysis are listed (A) to (G) below Element 1:

- (A) At the crack face  $\Delta_1$  is equal to the slip of the reinforcement relative to the crack face  $\Delta_{cr}$ which is equal to half the crack width that is  $w_{cr}/2$ . For analysis, a slip  $\Delta_1$  is imposed such that the problem is to derive the force  $P_1$  to cause the slip  $\Delta_1$ . Hence an initial guess for  $P_1$  is made.
- (B) As the analysis deals with serviceability loads, the bond slip properties can be considered to be linear (Muhamad et al., 2012; Visintin et al., 2013b) that is the relation between bond stress  $\tau$  and bond slip  $\Delta$  is a constant k. Hence for the imposed  $\Delta_1$ , can be derived  $\tau_1$ .

- (C) From the known bond stress  $\tau_1$ , the corresponding bond force  $B_1$  within Element 1 can be derived.
- (D) From equilibrium of forces across the element the change in concrete force and hence mean concrete strain  $\varepsilon_{c1}$  can be determined.
- (E) Similarly, from equilibrium of forces across the element, the change in reinforcement force and hence mean reinforcement strain  $\varepsilon_{r_1}$  can be determined.
- (F) Knowing the concrete shrinkage strain and having determined the average strain in the concrete and the reinforcement, the slip strain  $d\Delta_1/dx$  can be derived.
- (G) Consequently the change in slip within the first element  $\delta \Delta_1$  is known, from which the slip in the subsequent element  $\Delta_2$  can be determined.



## Figure 3 Tension stiffening analysis

The results from the analysis of Element 1 in Fig. 3(a) are now used in the analysis of Element 2 as listed below the element. This procedure is continued until the  $x^{th}$  element in Fig. 1(d) that is adjacent to the mid-length of the prism. By symmetry the slip at mid-length  $\Delta$  is zero. Hence if slip  $\Delta_x$  from the numerical analysis is not zero, then it is a question changing the guessed value of  $P_1$  until it is.

#### Material properties

The mechanics of the tension stiffening analysis described above does not depend directly on the material properties used. For example Code values for the variation of shrinkage and creep with time could be used or any values the reader deems appropriate. A summary of material models can be found in (Gilbert and Ranzi 2011).

Of importance is the variation of the bond stiffness k with corrosion. Research by (Feng et al., 2016c) suggests that the bond strength  $\tau_{max}$  varies with corrosion as shown in the three stages in Fig. 4 where:  $\tau_{max0}$  is the bond strength with zero corrosion; C is the percentage corrosion by weight;  $C_0$  signifies zero corrosion. The transition between the three stages in Fig. 4 can be defined by the points  $C_{1-2}$  which is the percentage corrosion when the bond strength starts reducing rapidly and which is often the onset of the longitudinal splitting cracks; and  $C_{2-3}$  which is the percentage corrosion in bond strength occurs.



Figure 4 Variation of bond strength with corrosion

Again it is worth mentioning that much research has been conducted to quantify the variation in bond properties with corrosion (Albitar et al., 2016; Almusallam et al., 1996; Cabrera 1996; Feng et al., 2016c; Val et al., 1998) and any model deemed appropriate may be used in the analysis. Here the model of (Feng et al., 2016c) is presented as it was derived from the analysis of 377 data points from test results covering a broad range of material properties. The variation in bond-slip with corrosion

(Feng et al., 2016c) is shown in Fig. 5 where:  $\delta_1$  is the slip at  $\tau_{max}$  as shown and can be taken as a constant value of 0.175 mm; and  $\delta_{max}$  is the slip when the bond stress tends to zero.

The ultimate bond strength  $au_{max}$  with corroded reinforcement is defined as

$$\tau_{max-C} = k_t \tau_{max-0} \tag{1}$$

Where the corrosion reduction factor  $k_t$  varies with the level of corrosion C as follows:

$$k_t = \left(-0.032\frac{c}{d} + 0.576\right)C + 1, \text{ when } 0 < C < 0.3C_{1-2}$$
(2)

$$k_t = \left(0.0137\frac{c}{d} - 0.247\right)C + 1.42 + 0.0475\frac{c}{d} - 3.94 \times 10^{-3} \left(\frac{c}{d}\right)^2, \text{ when } 0.3C_{1-2} < C < C_{2-3}$$
(3)

$$k_t = -0.0016C + 0.224$$
, when  $C > C_{2-3}$  (4)

In which: *C* is the level of corrosion in terms of percentage of mass loss; c/d is the ratio of cover to the edge of the bar *c* and the bar diameter *d*;  $C_{1-2}$  is the transition point where splitting cracks form; and  $C_{2-3}$  is the transition point where to the residual bond strength after the formation of splitting cracks. The transition points  $C_{1-2}$  and  $C_{2-3}$  are calculated as follows.

$$C_{1-2} = 0.288 \frac{c}{d} + 1.72 \tag{5}$$

$$C_{2-3} = \frac{\frac{-1.20 - 0.0475\frac{c}{d} + 3.94 \times 10^{-3} (\frac{c}{d})^2}{0.0137\frac{c}{d} - 0.245}} \tag{6}$$

The coefficient  $\tau_{max-0}$  is the bond strength when there is no corrosion and which has been suggested by the CEB Model Code (CEB-FIP Model Code 1990: Design Code 1994) to be

$$\tau_{max-0} = 7 \times (\frac{f_c}{25})^{0.25} \tag{7}$$

It should be noted that Eq. 7 corresponds to the scenario in which where good bond conditions are present. The variation in bond strength with corrosion given Eq. 1-6 is independent of the definition of  $\tau_{max-0}$  and hence Eq. 7 can be substituted for any bond model covering any initial conditions according to the best judgement of the reader.

As this paper is only dealing with serviceability, only the ascending branch in Fig. 5 needs to be considered as in Fig. 6. The serviceability bond stiffness at zero corrosion is shown as  $k(C_0)$ . From the

work of (Feng et al., 2016c) who determined the average slip at peak stress is 0.175 It is suggested that  $k(C_0)$  could be taken as

$$k(C_0) = 40 \times (\frac{f_c}{25})^{0.25} \tag{8}$$

However, any appropriate value could be taken as it will be shown subsequently that the assessment procedure does not depend on an accurate value.



Figure 5 Variation in bond-slip with corrosion



Fig. 6 Serviceability bond stiffness

# Monitoring sheet

Consider a beam that is being monitored from an early stage starting at time  $T_0$  such that corrosion has not yet started; other scenarios will be considered later. The existing RC beam has two visible

adjacent flexural cracks of mean width  $w_{cr0}$  at a spacing  $S_{cr}$  as shown in Fig. 1(b). Let the moment acting on the beam in the vicinity of these flexural cracks be estimated as  $M_s$  and the shrinkage strain  $\varepsilon_{sh0}$  and creep coefficient  $\phi_0$  at  $T_0$  be estimated from code variations (Gilbert and Ranzi 2010). For a given  $M_{sr}$   $\varepsilon_{sh0}$  and  $\phi_0$  the force in the reinforcement can be determined as  $P_{cr}$  from any standard analysis technique such as the moment curvature approach (*Gilbert and Ranzi 2010*) or from any advance analysis technique such as the segmental approach which directly incorporates the influence of bond-slip and concrete time effects (*Knight et al., 2013; Visintin et al., 2013a*) or estimated by approximating the location of the neutral axis depth (Warner et al., 1998). A tension stiffening analysis as depicted in Fig. 3 can then be applied and the bond stiffness  $k(C_0)$  adjusted until the crack width is equal to the measured value  $w_{cr0}$ .



Figure 7 Monitoring corrosion from crack width

Assuming code values for the variation in shrinkage and creep with time, the tension stiffening analysis in Fig. 3 can be used to derive the variation A-B-C in Fig. 7 that is without corrosion. This variation will be assumed to be appropriate in Stage 1 in Fig. 4 that is from  $C_0$  to  $C_{1-2}$  where corrosion does not lead to a reduction in bond strength. Similarly, by simply varying *k* in Fig. 6 according to the level of corrosion the tension stiffening analysis can also be used to determine the variation in crack widths with increasing corrosion.

Plotting the measured flexural crack width time, which is shown by the dashed line in Fig. 7 it is therefore possible to predict the average level of corrosion between the flexural cracks. For example, should the measured crack widths lie along A-D that is not significantly diverged from the predicted A-B, then this would suggest that the measured crack widening can be attributed to shrinkage and creep. Should divergence occur such as along D-E, then this would suggest that Stage 2 in Fig. 4 has started at time  $T_{1-2}$  in Fig. 7. A levelling off such as E-F in parallel with the predicted value would

suggest that there was no further increase in corrosion. Path F-G suggests further corrosion and a shallower path G-H would suggest Stage 3 in Fig. 4 has been reached.

This monitoring procedure does give an indication of whether detrimental corrosion is occurring and also an indication of the percentage of corrosion. It will be shown later that this information can be used to assess the serviceability deflection and it can also be used to predict the ultimate flexural capacity (Feng et al., 2016b).

## Monitoring crack widths

For a given RC beam, the tension stiffening analysis as explained above can be used to predict the variation in crack width with time for a range of bond stiffnesses k as in Fig. 8. The measured crack width  $w_{cr0}$  can then be used to predict the starting position Point A that is  $k(C_0)$  and the application proceeds as explained previously. These tension stiffening analyses also showed that variations in creep does not affect the crack width even though it will be shown later that it has a significant effect on the deflection. Hence in quantifying the variation in crack width with time, only shrinkage and corrosion needs to be considered.



Figure 8 Monitoring sheet of crack width

The variation A-B-C in Fig. 8 is now the true  $k(C_0)$  in Fig. 7. This is the value in Fig. 6 from which changes in bond stiffness due to corrosion are calculated. Hence it is the reduction in k above  $k(C_0)$  in Fig. 8 that is due to corrosion as shown on the RHS of the figure. Consequently the variation in crack width due to corrosion shown as the dashed line relative to A-B-C can be used to predict the amount of corrosion as already explained using Fig. 7.

As an example of application of the proposed technique, consider the beam cross section in Fig. 9. The beam is constructed from concrete with a compressive strength of 25 MPa, a tensile strength at 2.8 MPa and a modulus of elasticity of 25 GPa. The diameter of reinforcement is 16 mm and has a modulus of elasticity of 200 GPa. The variation in the bond between the reinforcement and concrete has been taken as that defined by (Feng et al., 2016c) which is given by Eq. 1-7 and the variation in corrosion over has been taken as that experimentally recoded by (Vidal et al., 2007). Australian Standards (Australia 2009) have been used to define the variation in concrete shrinkage and creep with time.



Figure 9 Dimensions of the cross-section



#### Figure 10 Variation in crack width with time

The monitoring sheet relating to the above mentioned scenario is shown in Fig. 10, where corrosion is varied from 0%-15%. In Fig. 10, Point A represents the application of load at day zero where concrete shrinkage and creep and reinforcement corrosion is zero. The crack width increases with concrete shrinkage up until day 2000 at which point corrosion commences. It can be observed that between day 2000 and day 5000 a gradual increase in crack width above that which is expected to occur due to concrete time effects alone occurs, that is, there is a deviation from the crack width corresponding to no corrosion. A rapid increase in crack width occurs at approximately day 5000. This point corresponds to a corrosion level of approximately 3%, which according to the model of (Feng et al., 2016c) results in the formation of splitting cracks. Finally, the widening of cracks is observed to slow between points E and F in Figure 10 which corresponds to the complete formation of splitting cracks and loss of significant confinement to the bar by the concrete cover beyond point  $C_{2-3}$  in Figure 4.

Up until this point we have considered the scenario where crack monitoring commenced when the corrosion level is in Stage 1 in Fig. 4 that is before  $C_{1-2}$  that is where the crack opening behaviour follows path A-B in Fig. 8 with time. Hence a crack width  $w_2$  in Fig. 8 will give the same  $k(C_0)$ . However there is a difficulty when monitoring starts after Stage 1 in Fig. 4 as illustrated by  $w_3$  or  $w_4$  in Fig. 8. A solution to this problem is to monitor a pair of cracks in a region where corrosion is not expected as in Fig. 11(a) and also to monitor a pair of cracks in a region where corrosion is expected in Fig. 11(b).



Figure 11 Monitoring two pairs of cracks

Each of the regions in Fig. 11 will have their unique crack spacing, crack width and moment as shown in the square brackets. The analysis depicted in Fig. 8 for the uncorroded region is shown in Fig. 11(a) from which can be derived  $k(C_0)$ . The variation for this stiffness are shown in Fig. 11(b) for the corroded region which is now the base line for predicting corrosion levels as described in Fig. 8. Hence in this approach the uncorroded region is used to determine  $k(C_0)$  for the corroded region.

The above approach of monitoring in corroded and uncorroded regions can be taken one step further. Non-dimensionalising the ordinate in Fig. 11(a) by dividing  $w_{cr}$  by  $w_{cr-u}$  and that in Fig. 11(b) by  $w_{cr-th}$  and then comparing the variations at  $k(C_0)$  generally shows little variation. This is because in the tension stiffening analyses all the material properties including the bond-slip are assumed linear. Hence it is only necessary to compare the proportional increase in crack width in the corroded region  $w_{cr}/w_{cr-u}$  with the proportional increase in the uncorroded region  $w_{cr}/w_{cr-th}$ . Any major divergence would signify corrosion after which the analysis in Fig. 11(b) could be performed to determine the amount of corrosion. Hence initially there is no need to plot the figures in Fig. 11 rather it is only necessary to compare the proportional increases in crack width. Once corrosion is detected then the figures will have to be plotted to determine the amount of corrosion.

## **Monitoring deflection**

The segmental deformation in Fig. 1 can also be used to predict the effect of corrosion on the beam deflection. The RHS of the segment in Fig. 1(b) is shown in Fig. 12. The Euler-Bernoulli deformation A-A in Fig. 12(a), can be converted to a strain, stress and force distributions as shown to the right in order to derive the moment-curvature ( $M/\chi$ ) at serviceability; full descriptions of this numerical analysis are published and validated against experimental results elsewhere (Knight et al., 2013; Visintin et al., 2013a) and hence not repeated here. The tension stiffening analysis has shown that creep has virtually no effect on crack width. However creep will reduce the concrete modulus so that the Euler-Bernoulli deformation A-A needs to move to C-C with an increase in rotation due to creep  $\Delta\theta_{cr}$ . It can be seen how creep significantly increases the deflection but does not affect the crack width. Hence monitoring the crack width is more effective than monitoring the deflection.



Figure 12 Segmental analysis

The moment curvature results from the analysis in Fig. 12 can then be used to predict the deflection of a beam with time as in Fig. 13. It can be seen at time  $T_2$  that the deflection has three components: that due to creep  $D_{cr}$ ; that due to shrinkage  $D_{sh}$ ; and that due to corrosion  $D_{co}$ . When only part of the beam corrodes then the increase in deflection  $D_{co-pt}$  is small and can be clouded by  $D_{cr}+D_{sh}$  that is it would be difficult to detect. Additionally, the monitoring of crack widths allows the average corrosion between each pair of adjacent cracks to be easily determined while a monitored deflection alone does not yield a unique level of corrosion.



Figure 13 Time dependent beam deflection

By way of an example of application, again consider the cross section in Fig. 9 which is used to construct a beam with a span of 3500mm and which is loaded in 4 point bending with the loads applied at the third span. For an applied load which yields a stress in the tensile reinforcement of half of the yield strength, the variation of mid-span deflection with time is shown in Fig. 14 for three different corrosion scenarios (i) where uniform corrosion exists along the entire span as in Fig. 15(a);

(ii) where only 20% of the beam is corroded at mid-span as in Fig. 15(b); and (iii) where only the portion of the beam near the supports is corroded as is Fig. 15(c).



Figure 14 Change in Deflection with time

In Fig. 14 it can be seen that although corrosion commences at day 2000, even when the whole beam is considered to be uniformly corroded, no significant increase in deflection due to corrosion can be detected until splitting cracks form at approximately day 5200 where the corrosion level has reached 3%. This is particularly significant as the small variation in deflection due to corrosion could easily be lost in the variation in concrete creep and shrinkage strains which are known to vary by as much as 30% (Australia 2009).



(c) partly corroded at the end

Figure 15 Varying extent of corrosion

The prediction of corrosion via the monitoring of member deflection is made more difficult when only a portion of the beam is corroded. For example consider the scenarios shown in Figures 15(b) and (c)where only the centre or the ends of the beam have corroded reinforcement. In these scenarios increases in deflection due to corrosion lie within the scatter expected from calculation of time effects, particularly when corrosion is concentrated in regions of low moment. As seen in the deflection measurement for end corrosion, it may therefore be difficult to estimate the level of corrosion from a measurement of deflection even after splitting cracks have formed.

# Conclusions

It has been shown that monitoring crack widths is an effective procedure in monitoring steel reinforcement corrosion in RC beams and slabs because monitoring flexural crack widths can detect local areas of corrosion and the results are not clouded by creep. A partial interaction mechanics based approach that allows for changes in bond properties due to corrosion as well as the effects of creep and shrinkage has been described. It is shown how this model can be used to provide charts for the variation in crack width with time to monitor existing flexural cracks in beams or slabs to predict when the effects of corrosion are deleterious and also to give a guidance to the amount of corrosion that exists. The approach does not predict future corrosion but it can be used in conjunction with future corrosion predictions to estimate their effect on the structure.

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## CONCLUSIONS

Corrosion strongly influences the performance of reinforced concrete structures at the serviceability and ultimate limit states due to a reduction in the cross-sectional area of reinforcement, a deterioration of bond between the reinforcement and concrete, the formation of splitting cracks and ultimately debonding of the reinforcement. This thesis has developed a (i) material model to quantify the deterioration of bond between concrete and reinforcement caused by corrosion; (ii) a numerical model to simulate the debonding behaviour of reinforced concrete in ultimate limit states and (iii) a monitoring technique to detect the corrosion condition of reinforcement at serviceability limit.

The mathematical model of bond-slip relationship with corrosion is built based on a database with 377 data points to show how the bond-slip relationship changes after corrosion of bars occurs. The model was applied to analyse the examples with different material properties and different corrosion level which shows that when corrosion level increases, debonding may happen before bar yielding and bars with large diameter is more easily to be influenced by corrosion than bars with small diameter.

The mathematical model of bond-slip with corrosion indicates that debonding occurs when corrosion amount of reinforcement increases. Then numerical models were presented to simulate the beam behaviour in ultimate limit state before and after debonding of reinforcement. The segmental approach was applied to simulate the capacity of reinforced concrete prior to debonding while the numerical model of debonding was presented to show how to compute the capacity of reinforced concrete beam after debonding, in which condition, the reinforcing bars work as prestressed tendon. The procedures indicates that with certain material properties, even when debonding exists between concrete and bars due to the amount of corrosion, there still might be considerable strength and ductility provided by the structures by the compatibility of deformation between reinforcement and the concrete at the level of reinforcement.

Besides, an effective way of monitoring corrosion in serviceability was introduced by measuring the flexural crack width. Although corrosion influences deflection, the problem with measuring deflection is that deflection is normally affected by creep and shrinkage dramatically. The mechanics based approach described in this thesis shows that crack width is obviously affected by corrosion while creep has very less impact on flexural crack width in contrast. The continuous measurement of crack width indicates the increase of corrosion of steel bars in small local area, while the shrinkage effects with time could be very easily computed from references like building codes. Furthermore,

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the measurement of crack width is much easier than measuring deflection. Hence, this analysis provides a more efficient way to monitor the increase of corrosion of reinforcement inside the structures.

In summary, this thesis provides the mathematical model of bond-slip with corrosion effects, which quantified the reinforced concrete structural behaviour not only in ultimate limit states but also in serviceability limit states. Hence, the contribution of this thesis to future research work could includes these aspects: (1) the study of debonding behaviour of reinforced concrete with small local area of corrosion; (2) the study of the ultimate limit state behaviour of reinforced concrete with prestressed tendon based on the numerical models of segmental approach and the debonding model; (3) the experimental work of stirrup effects on bond with corroded reinforcement.