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Spray and Combustion Investigation of Post Injections under Low Temperature Combustion Conditions with Biodiesel

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Abstract

Post injection is a multiple injection strategy that is commonly used as a particulate matter control measure to reduce soot emissions, yet the mechanisms and the interactions between the main and post injections are only vaguely understood. For

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3 this work, experiments were performed to assess the effects of varying dwell time be-
4 tween the main and post injections in a compression-ignition (CI) engine environment
5 simulated using a constant-volume combustion chamber (CVCC). The ambient den-
6 sity, bulk temperature and oxygen concentration used for this work were controlled at
7 19.4 kg/m³, 900 K and 15 vol.% O₂, respectively. A canola oil based biodiesel was
8 tested and injected at a fixed injection pressure of 100 MPa into the simulated CI en-
9 gine environment. A mass ratio of 80% to 20% was maintained between the main and
10 post injections, with the dwell time between the injections varied from 1.5 to 2.5 ms.
11 Comparative measurements were performed using the same fuel and injection sched-
12 ules, but at a higher ambient gas temperature condition of 1100 K. Optical diagnostics
13 methods, including diffused-back illumination and high-speed flame luminosity imag-
14 ing, were used to assess the spray and combustion processes of the post injection test
15 case. Under the conditions of this work, it was found that the ignition delays, igni-
16 tion locations and the flame lift-off lengths of the post injection flames are consistently
17 shorter than those of the main injections, with the variations influenced by the extent
18 of the interaction of the post injection with the combustion products from the main
19 injection. Two-color pyrometry technique was also used to measure the soot tempera-
20 ture and soot concentration factor information of the main-post injections cases. The
21 data revealed a greater interaction between the main and post injections resulted in a
22 more rapid development of the soot zone of the post injection with higher temperature,
23 after ignition. The distribution of the most probable soot concentration factors of the
24 post injection was also found to be narrower, with lower soot content values.
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47 **1 Introduction**

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50 The continuous need to maximize fuel economy and engine power whilst minimizing emis-
51 sions intensifies the call for innovative combustion and after-treatment technologies. The
52 development and implementation of injection systems that are capable of advanced injec-
53 tion strategies, such as multiple injection, which began in the early 1990s,¹ paved the way
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3 for considerable research²⁻⁴ and interest into the application of such strategies. Since then,
4 multiple injection strategies are commonly employed in modern engines to achieve a range
5 of improvements, such as refined engine control, reduced combustion noise, lower soot pro-
6 duction and/or enhanced soot oxidation.⁵⁻⁸
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11 Post injection is a multiple injection strategy that involves the introduction of a small
12 quantity of fuel after the end of main injection event. The post injection strategy is gener-
13 ally used as a measure to reduce soot emissions, or to enable exhaust gas after-treatment
14 technologies.^{9,10} Questions, however, remain about the mechanisms through which reduced
15 pollutant emissions is achieved, and whether interactions between the combustion of main
16 and post injections contribute to the observed outcomes.^{9,11} For example, previous stud-
17 ies^{11,12} have reported that the enhanced mixing induced by the post injection can bring
18 fresh oxygen to the soot from the main injection to increase soot oxidation. Other works^{11,13}
19 have noted that the additional heat release, induced by post injection, can elevate in-cylinder
20 temperature conditions to promote soot oxidation. Several studies,^{14,15} on the other hand,
21 have attributed the reduced exhaust soot emission to the suppression of soot formation that
22 arose from the discontinuous introduction of the fuel through a series of smaller injection
23 processes. The different findings presented in the literature imply that the mechanisms and
24 the interactions between the injections can vary, depending on the injection schedule, the
25 fuel type and the ambient conditions under which the post injection occurred. A better
26 understanding of the mechanisms associated with various operating conditions is therefore
27 critical to enable consistent, effective implementation of the post injection strategy.⁵
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45 In addition to multiple injection strategies, the use of alternative fuels, such as biodiesels,
46 is also a promising viable approach to reduce particulate matter, CO and unburned hydro-
47 carbon emissions, when compared with conventional diesel fuel. Whilst the use of biodiesels
48 has been reported to cause an increase in NO_x emission, this issue can be alleviated by
49 using biodiesels in low-temperature combustion (LTC) mode.¹⁶ Several studies have looked
50 into combining LTC modes, multiple injection strategies and alternative fuels to achieve
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3 further engine performance improvement and emissions reduction.^{16,17} However, depending
4 on their feed stocks,¹⁸ biodiesels can have different properties that would impact on the fuel
5 atomization, evaporation, combustion and pollutant formation processes.^{17,19} As such, whilst
6 significant benefits can be achieved, they can only be realized through improved understand-
7 ing of the mechanisms involved with different combinations of multiple injection strategies,
8 combustion conditions, and fuels.
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11 This work aims to improve the understanding associated with the implementation of post
12 injection strategy, when used in conjunction with biodiesel under LTC condition, with a focus
13 on the interaction between the main and post injections for selected main-post injection
14 schedules. Canola oil based biodiesel fuel with well-known composition was injected into
15 a simulated compression-ignition (CI) engine condition with 19.4 kg/m³ ambient density,
16 5.1 MPa ambient pressure, 900 K bulk temperature and 15 vol.% O₂ concentration, inside an
17 optically-accessible constant volume combustion chamber (CVCC). It is noted that in engine
18 experiments, changes that are made to the operating parameters, such as intake temperature,
19 intake pressure, engine speed and engine load, would often result in simultaneous changing
20 in several basic parameters of the engine, such as ambient temperature, density, pressure
21 and injection timing.²⁰ This has resulted in some challenges in isolating the effect of basic
22 parameters on the spray or combustion events of interest for detailed understanding, when
23 interpreting engine data. For this work, the experiments are therefore performed in a CVCC,
24 which is capable of providing more accurate and direct control of the basic parameters.²¹
25 It is also noted that the experimental conditions were selected for this work so that free
26 jets can be generated. This is to avoid the complexities that can arise from flame-wall
27 interaction – a phenomenon that remains only vaguely known, due to the multitude and
28 complexity of the associated processes.²² The advanced understanding that is derived from
29 the free jet experiments, nevertheless, is still useful to help the research community to better
30 understand the basic processes affecting main-post injections, which in turn, can be extended
31 to results in more complex and realistic engine scenarios. The canola oil based biodiesel is
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of interest to this work as it has been previously investigated by the authors under open flame burner, performance engine and CVCC settings.^{23,24} The biodiesel, which has been shown to be sooting even under moderate exhaust gas recirculation (EGR) conditions, is selected for post injection as a soot reduction approach.²⁴ The mass ratio of the main to post injection was maintained at 80% and 20% throughout the experiment. For this work, the dwell time, and hence the coupling between the main and post injections, was varied to examine its effects on the spray and combustion properties. A high-speed digital camera was used to record the flame luminosity and two-color images from the combustion events. A detailed analysis was performed on the flame images recorded to characterize the main-post combustion properties, including ignition delay, ignition location, and flame lift-off lengths, in addition to soot temperature and soot concentration factor (KL) distributions measured using two-color pyrometry. The liquid spray and length information of the main and post injections were also characterized in non-reacting environment simulated using the CVCC. In addition, to examine the sensitivity of the results to the variation in ambient temperature, comparative measurements were repeated at a higher ambient gas temperature condition of 1100 K that is known to increase soot formation,²⁵ but with the same fuel and injection schedules.

2 Experimental Details

2.1 Constant-volume Combustion Chamber

The experiments were conducted in an optically-accessible CVCC at UNSW Sydney, under simulated CI engine condition. A schematic diagram of the chamber, along with the high-speed flame luminosity imaging setup, is provided in Fig. 1. The vessel has a cubical combustion chamber, 114 mm on each side, with optical access provided by side-port windows (102 mm diameter). A single-hole solenoid fuel injector was mounted at the center of a metal side-port of the CVCC. An agitator was mounted at the top of the CVCC and was used

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3 to maintain a spatially uniform temperature environment in the chamber. The CI engine
4 condition within the chamber was simulated by metering acetylene, hydrogen, oxygen and
5 nitrogen gases into the CVCC. The combustible gas mixture was subsequently spark-ignited
6 to create a high temperature and pressure environment. Following the premixed combustion,
7 the combustion products inside the chamber were allowed to cool down through heat trans-
8 fer to the cooler chamber wall, during which the pressure inside the chamber was monitored
9 with a pressure sensor (Kistler 6052C). For this work, an ambient condition with gas density,
10 pressure and temperature of 19.4 kg/m^3 , 5.1 MPa and 900 K, respectively, was targeted. The
11 fuel injector was triggered once the targeted condition was reached. The metering of the
12 reactant gas was also controlled so that an environment with 0 or 15 vol.% oxygen concentra-
13 tion can be generated after the premixed combustion process. The 0 vol.% ambient oxygen
14 concentration (non-reacting) condition was used to provide insights into the liquid length
15 penetration characteristics of the sprays with varied injection schedules, without the complex
16 effects of heat release from the combustion processes. The 15 vol.% (reacting) ambient oxy-
17 gen environment was selected to mimic operating condition for modern compression-ignition
18 engines that use moderate EGR and have minimal NO_x emissions.²⁵ For comparison pur-
19 pose, measurements were also repeated under the same ambient condition, but at a higher
20 ambient temperature of 1100 K. A summary of the ambient experimental condition for this
21 work is listed in Table 1.

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41 A Bosch common-rail (CP4) system with a single-hole solenoid injector (105 μm) was
42 used as the fuel injection system. A common-rail PCV driver (Zenobalti, ZB-1200) was
43 used to regulate and maintain the injection pressure at 100 MPa. In addition, an injection
44 driver (Zenobalti, ZB-5100) was used in conjunction with a digital delay generator (Stanford
45 Research Systems DG 535) to control the triggering of the fuel injection system. The single-
46 hole injector was used to avoid the complexity that can arise from jet-jet interaction. In
47 this work, the multiple injection case was tailored to represent a ‘main plus post’ injection
48 schedule, with a total injected fuel mass of 10 mg. A single injection case, with its injection
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3 duration adjusted so that it has a total injected fuel mass as the main-post injection case, was
4 also measured for reference purpose. The rate of injection (ROI) profiles of the main-post
5 and single injection cases were measured using a Bosch tube type injection rate meter. The
6 fuel mass ratio of the main to post injections was fixed as 80% to 20%. Dwell time (DT),
7 which is defined here as the time between the end of electronic command of the main and the
8 actual start of injection for the post, was set as 1.5, 2.0 and 2.5 ms for the main-post cases.
9 It is noted that the shortest DT used (1.5 ms) is near the limit of the injector capability,
10 for which the solenoid valve and needle lift can be actuated reliably. A summary of the fuel
11 injection conditions is provided in Table 1.
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21 It is noted that this work is part of a larger project that is aimed at improving the
22 understanding of the combustion and pollutant emission characteristics of biodiesels. In
23 the authors' previous work,^{23,26,27} four surrogate biodiesel fuels, which were abbreviated as
24 C810, C1214, C1618 and C1875 in previous publications, comprised of fatty acid methyl
25 esters (FAMES) that are derived from palmera-based and coconut-based oils (C810, C1214),
26 pale-based oil (C1618), and canola-based oil (C1875), respectively, were examined as they
27 have physico-chemical properties that are adequate to represent biodiesels from a broad
28 range of feed stocks. Biodiesels C810 and C1214 are representatives of saturated FAMES
29 with short and medium carbon chain lengths. Specifically, biodiesels C1618 and C1875, on
30 the other hand, have long and similar chain lengths but with different saturation degree;
31 with C1618 being partially saturated and C1875 being almost fully unsaturated. These dif-
32 ferences in the molecular structures have been previously shown to affect the physical and
33 chemical mechanisms that occur during combustion, and are correlated with the ensuing
34 engine performance and pollutant emission trends. The C1875 fuel, which has highest soot
35 propensity amongst the four surrogate fuels because of its long carbon chain and low degree
36 of saturation, has been shown to be reasonably sooty even at moderate EGR condition, and
37 is therefore selected for this post injection for soot reduction study under exhaust gas recir-
38 culation condition. A detailed description of the fuel can be found in Ref.²³ and therefore,
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3 only a short summary the main compositions and properties of the biodiesel is provided in
4 Table 1. In brief, the biodiesel fuel used has an oxygen content, iodine, saponification and
5 cetane numbers of 10.83 wt%, 105, 185 and 59, respectively. The iodine and saponification
6 numbers of the fuel indicate that it is almost unsaturated and has a long carbon chain length.
7 The high cetane number, on the other hand, implies that the fuel has a short ignition delay.
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15 2.2 Optical Diagnostics

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17 Two optical techniques were used for this work, namely diffused-back illumination (DBI) and
18 high-speed natural flame luminosity imaging. For both of these optical diagnostic methods,
19 which were not performed simultaneously, a high-speed camera (Photron SA-5) that was
20 equipped with a 85 mm f#1.8 Nikkor lens, was used to record the events. The f-stop of
21 the camera lens and the exposure time of the camera were adjusted between the DBI and
22 high-speed flame luminosity imaging setups to ensure a good balance between optimum
23 light level and camera exposure. For the DBI imaging, the collimated light output from a
24 continuous, high-powered LED that was emitting at a central wavelength of 455 nm, was
25 used for illumination. An engineered diffuser was also placed between the light source and
26 the spray to ensure homogenized illumination. The camera, which was positioned directly
27 opposite to the LED light source, was operated at a frame rate of 15,000 frames per second
28 (fps), with 1 μ s exposure and a pixel resolution of \sim 0.14 mm per pixel. For the high-speed
29 flame luminosity imaging, the time-resolved flame images of the combustion of multiple and
30 single injection cases were captured using the high-speed camera, which was also operated
31 at the same frame speed and exposure time. The pixel resolution of the image was \sim 0.2 mm
32 per pixel. Typical time sequenced flame luminosity images recorded for a main-post injection
33 case, with a dwell time of 1.5 ms, are presented in Fig. 2. It is noted that for both DBI and
34 high-speed flame luminosity imaging, the camera was synchronized to the start of injection
35 of the injector. At least five runs were performed for each test condition to ensure good
36 repeatability, and at least 150 images were recorded for each run, to ensure that entire
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3 combustion event was captured.
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7 **3 Image post-processing**

8 **3.1 Diffused back illumination imaging post-processing**

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11 To determine the spatial extent of the liquid phase in the DBI images, the light intensity,
12 I , at a pixel location from an image with spray, was compared against the background
13 intensity, I_o , at the same pixel location from an image with no spray. To determine the
14 cut-off I/I_o value suitable for use to derive liquid length information from the DBI images,
15 both DBI and Mie-scattering images were recorded for a series of evaporating sprays under
16 test conditions that are similar to this work. The Mie-scattering images obtained was first
17 processed to derive liquid boundary information. It is noted that an image intensity value
18 that corresponds to 3% of the maximum intensity, which was widely used as the threshold
19 setting for the processing of Mie-scattering images in the literature,^{28,29} is also applied here
20 for consistency reason. A systematic variation of the I/I_o cut-off value used to process the
21 DBI images of the same sprays was then performed. A threshold value of 0.3 was found to
22 give the most consistent agreement between both techniques, and is therefore used for this
23 work. It is noted that the Mie-scattering imaging was performed using high-speed camera
24 imaging with side illumination, and was only used for the calibration of the DBI results. A
25 schematic diagram of the DBI and Mie-scattering imaging setups, and their orientations in
26 relation to the chamber, is shown in Fig. 3.
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47 **3.2 Flame luminosity imaging post-processing**

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50 A novel color band approach, which was first introduced by Larsson³⁰ and further expanded
51 upon by Svensson *et al.*³¹ was implemented to provide soot temperature and soot KL (a factor
52 that is proportional to the soot volume fraction and gas layer thickness^{31,32}) information.
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54 The color band approach, which only requires the use of a single digital color camera for soot
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3 two-color measurements, has the advantage of avoiding introducing errors due to potential
4 misalignment of frames taken by two cameras and eliminates the need for complex optics
5 that are typically required for the more classical implementation of two-color pyrometry
6 technique. The general two-color thermometry theory has been detailed in the literature^{31–33}
7 and is therefore not described in detail here. In essence, for each pixel, a modified Planck's
8 blackbody function, which incorporates wavelength-dependent soot emissivity model and
9 responsivity of the detection system used (optics train, filter and high-speed camera), was
10 applied to the red and green color bands to yield two equations with two unknowns (*e.g.*, the
11 soot temperature and soot KL factor). The optical response of the high-speed camera used,
12 for each of its color channel, is shown in Fig. 4. The technique was subsequently calibrated
13 against a tungsten lamp with known spectral properties.
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25 Following the approach of Zha *et al.*,³² to reduce the computational time during image
26 processing, two universal surfaces (Fig. 5) that map the domains of the red and green pixel
27 intensities to soot temperature and KL surfaces, were generated. By matching the pixel
28 intensities recorded for the red and green channels to the parameter spaces of the universal
29 surfaces, the solutions to the two equations can be sought in a time-efficient manner. It
30 should be noted that the two-color pyrometry technique is a line-of-sight method and there-
31 fore, the optical signals detected are inherently integrated along the optical path.^{31,34} In
32 previous studies,^{31,34} the accuracy of the two-color technique has been observed to be highly
33 susceptible towards the spatial gradients in soot properties, especially temperature, in the
34 optical path. Additionally, the deduced two-color temperature and soot concentration values
35 have been shown to be biased towards soot within the hot flame surface that is closest to
36 the camera.³¹ For example, Musculus *et al.*³⁴ have reported that the two-color technique can
37 overestimate the actual soot temperature by 200 K, whilst underestimating the true soot
38 concentration by 50%. In a separate previous study by Svensson *et al.*,³¹ it was shown that
39 the two-color technique can have a temperature uncertainty in the range of ~ 150 K, and
40 is only reliable for qualitative soot concentration measurement. It is therefore necessary to
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3 consider all these limitations, when interpreting the two-color data obtained.
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7 **4 Results and discussion**

8 **4.1 Liquid penetration lengths**

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11 The quasi-steady liquid length measurements of the main-post injections with single injec-
12 tion case are presented and compared in Fig. 6, to give insights into the potential effects
13 of DTs on the characteristics of the liquid phase. It should be noted that both the liquid
14 penetration measurements were performed under high-temperature, high-pressure but inert
15 (0% ambient oxygen) conditions, as this would help to eliminate the uncertainty associated
16 with heat-release effects on liquid penetration, and permit comparison with previous liquid
17 length studies.³⁵ The average liquid lengths of the sprays are observed to be relatively sta-
18 ble across the stabilized periods of their injections, albeit with slight fluctuations (22%).
19 The liquid lengths of the main injections of the multiple injection cases are also found to
20 similar to that measured for the single injection case. Together, these findings imply that
21 sufficient quantities of fuel were injected during the main injection periods of the multiple
22 injection cases to reach quasi-steady liquid lengths. From the figure, it can also be seen
23 that the maximum liquid penetrations of the post injections are comparable to that of the
24 corresponding main injections and are not found to be sensitive towards the variation in
25 DT, especially considering the experimental uncertainty. The liquid penetration profiles of
26 the post injections, however, are observed to vary with changing DT. Specifically, from the
27 liquid penetration profiles of the post injections, it can be seen that the time that is required
28 for the post injection to reach the maximum liquid penetration distance is found to increase
29 with increasing DT. It is noted that similar observations were also reported in a previous
30 study.³⁵ In that study, it was shown that the penetration rate of the second injection can
31 be greater than the first injection, because the second enters into cool, fuel-laden mixture
32 region left by the first.³⁵ It should be noted it is unclear if these spray characteristics would
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3 be observable in reactive ambient conditions.
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7 **4.2 Flame luminosity plots**

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10 To visualize the effects of the DT on the combustion characteristics, radial integration of the
11 flame luminosity at each axial location of each frame was performed for the high-speed images
12 that were recorded for the main-post and single injection cases. The ensuing contour plots,
13 which are also known as Intensity-aXial-Time (IXT) plots in the literature,⁵ are presented in
14 Fig. 7 and are used to derive key combustion characteristics of the injection cases, including
15 ignition location, ignition delay, flame lift-off length, flame penetration distance and internal
16 flame structure information. It is noted that ignition location is defined here as the distance
17 from the nozzle where the flame luminosity is first detected. The ignition delay time, on
18 the other hand, is defined as the elapsed time after the start of injection (aSOI), until the
19 first detection of flame luminosity. The flame lift-off length and flame penetration distance
20 refer to the average quasi-steady distances of the flame base and flame tip from the injector
21 nozzle, respectively.
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34 In Fig. 7, for the main-post injection cases, the two ‘islands’ on the plots represent the
35 main (larger) and post (smaller) injection events. From the figure, it can be seen that whilst
36 the overall shape of the islands on the contour plots are similar, some differences in the flame
37 penetration, start of ignition, ignition location and intensity distribution characteristics can
38 be observed for the post injections. In Fig. 7, the maximum flame penetration distances
39 of the post injections are found to be lower than their corresponding main injections, and the
40 single injection reference case. This may be partly due to interactions between the fresh
41 fuel from post injection with the combustion products from the main pulse. In addition,
42 recent work^{36,37} have also demonstrated that the strong enhancement in entrainment that
43 occurs after the end of injection can interact with the fuel jet, causing the fuel vapor velocity
44 and hence, penetration to fall below its steady-state value. Together, these can prevent the
45 post injection flames from reaching their maximum quasi-steady state development. From
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3 Fig. 7, it can also be observed that both the ignition locations and the flame lift-off lengths
4 of the post injections are lower than their main injections and the single injection reference
5 case. The ignition and lift-off distances of the injections, nevertheless, are still found to be
6 greater than the maximum liquid penetration lengths observed in Fig. 6. These findings
7 therefore indicate that there is no interaction between the spray and combustion processes
8 under the test conditions of this work. When comparing the intensity distributions within
9 the contour plots in Fig. 7, the peak luminosity values for both the main and post injection
10 combustion events are found to be similar for all DTs. The post injections, however, are
11 found to have marginally smaller areas with higher intensity, with the smallest area observed
12 for the shortest DT (*i.e.*, 1.5 ms).
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23 To further understand the changes in the ignition and combustion characteristics of the
24 post injection events, the ignition delays, ignition locations and the flame lift-off lengths
25 of the post injections, which are derived from the corresponding IXT plots in Fig. 7, are
26 also plotted against the average values of their main injections in Fig. 8. Dashed lines
27 through the data are used to help the visualization of the trends. Error bars (1 standard
28 deviation) are also included to show the uncertainty associated with each data point. It is
29 evident that the ignition delay, ignition location and flame lift-off length values of the post
30 injections are shorter than that of the main injections. In addition, there is also a clear trend
31 of shortening ignition delays and ignition locations with decreasing DT, whilst the flame
32 lift-off lengths appear to reach an asymptote with longer DT. Previous studies^{38,39} have
33 reported that changes in ignition delay can impact on the time available for fuel-air mixing.
34 This will directly affect the heat release profiles of the premixed and the mixing-controlled
35 combustion processes, which in turn, will change the soot and temperature distribution of
36 the flame.⁵ Given that natural luminosity of a sooty flame is mainly comprised of hot soot
37 incandescence,⁴⁰ which is a function of the local soot concentration and temperature,⁴¹ the
38 observed changes in the intensity distributions in the IXT plots (Fig. 7) with varied DTs can
39 therefore be expected. In a previous study by Cung *et al.*,⁵ it was noted that when sufficiently
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3 short DT is used, the combined momentum of the closely-coupled injections can push the
4 ignition location and flame lift-off length of the later injection downstream from the nozzle.
5 A near linear correlation between the changes in the ignition delays and ignition locations, in
6 addition to a relatively invariant lift-off lengths of the flames across the varied DTs, however,
7 is observed here. These trends imply that for the test conditions of this work, the DTs used
8 were sufficiently long such that the momentum from the main injections have adequately
9 decayed. From the time-sequenced flame luminosity images for the main-post injection with
10 DT=1.5 ms (Fig. 2), it can be seen that whilst the combustion of the post injection was
11 progressing towards the tail of the main injection, the combustion events were sufficiently
12 separated. This observation is also reflected in the IXT plots presented in Fig. 8. From
13 the figure, in the case of DT=1.5 ms, it can be seen that whilst the combustion of the post
14 injection initiated when the main injection was still active, the contours associated with the
15 two injection events are distinguishable. When the DT is longer, as in the cases of DT=2.0
16 and 2.5 ms, it can be also inferred from the IXT plots in Fig. 7 that the post combustion
17 events only started after the main injections have extinguished. The consistently shorter
18 flame lift-off lengths of the post injection flames, when compared with those of the main
19 injection flames, also indicates that the injection duration specified for the post injection
20 was not sufficiently long for the flames to revert back to their natural lift-off distances. It
21 should also be noted that from Fig. 7, there is no indication of combustion ignition occurring
22 upstream of the lift-off location (*i.e.*, combustion recession⁴²) after the end of injection of
23 the main, for all main-post injection cases.
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45 To further understand the changes in the ignition and combustion characteristics of the
46 post injection events, the IXT plots for the main-post injection cases, when subjected to a
47 increased temperature ambient (1100 K) that is known to increase soot formation,²⁵ are also
48 generated and plotted in Fig. 9. From the figure, it can be seen that the general features of
49 the IXT plots are similar to that derived for the main-post injection cases in Fig. 7. It is
50 noted, however, in contrast with the IXT plots in Fig. 7, the intensity distributions of the
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3 contour plots for the post injection events are found to be similar for all DTs. In addition,
4 the flame luminosity signals for both the main and post injections are also found to recess
5 back towards the injector, after their end of injections for all DTs – a phenomenon that
6 was not observed at 900 K. This is consistent with the findings of previous studies,⁴² which
7 observed that lifted flame would have a greater propensity to propagate backwards towards
8 the injector after its end of injection under high-temperature CI operating conditions. From
9 the IXT plots, it can also be seen that the contours associated with the two injection events
10 are distinguishable for all DTs, which indicate that the main and post injection combustion
11 events were sufficiently separated at a higher ambient gas condition of 1100 K.
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21 To provide a more quantitative assessment, the ignition delays, ignition locations and the
22 flame lift-off lengths of the post injections, as derived from their corresponding IXT plots,
23 are also plotted against the average values of their main injections, as shown in Fig. 10.
24 When comparing the plots in Figs. 8 and 10, it can be seen at 1100 K, the ignition delay
25 and location values of the post injections are also shorter than that measured for the main
26 injections. The variations in the ignition delays and ignition locations of the post injections
27 across the varied DT range, however, are within measurement uncertainties. The flame
28 lift-off lengths of the post injection flames also appear unchanged and are of comparable
29 values to their main injections, across the DT range. As is noted in previous studies,²⁰
30 an increase in ambient gas temperature would result in reduced lift-off length. The soot
31 processes of the flame would therefore initiate at a distance that is closer to its nozzle, where
32 the momentum effects of the main injections, if present, are expected to be more significant.
33 The relatively trends in ignition parameters of the post injection flames therefore support
34 the previous assertion that the DTs used were sufficiently long so that the momentum from
35 the main injections have decayed. The similarity in the flame lift-off length values between
36 the main and post injection combustion events, on the other hand, implies that the earlier
37 ignition that occurred because of the higher ambient gas temperature, may have provided
38 the post injection flames with sufficient time to stabilize at their natural lift-off distances
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3 before their end of injections. Together, one can therefore anticipate the ensuing the soot
4 and temperature distribution, and hence, the natural luminosity of the post injection flames,
5 to be similar across the DT range, as is observed in their IXT plots (Fig. 9).
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10 **4.3 Soot temperature and KL images**

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12 As is noted in the previous section and other studies,^{40,41} the natural luminosity of a flame
13 is a function of the local soot concentration and temperature. To gain further understanding
14 of the interaction between the main and post injections, the soot temperature and KL
15 distributions of the main and post injections at two ends of the investigated DT range (*i.e.*,
16 DTs=1.5 and 2.5 ms) are generated, as presented in Figs. 12 and 13.
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24 In the case of DT=1.5 ms, the soot temperature and KL distributions of the main and
25 post injections are compared at three selected timing pairs of $t_1=0.4$ ms vs $t_2=4.7$ ms,
26 $t_1=0.6$ ms vs $t_2=4.9$ ms and $t_1=0.8$ ms vs $t_2=5.1$ ms, as are shown in Fig. 12. The t_1 and t_2
27 correspond to the time after start of injection, for the main and post injections, respectively.
28 The temporal positioning of these image pairs in the context of their injection rate profiles
29 are shown in Fig. 11. It can be seen that the timing pairs are selected from the quasi-steady
30 injection period to minimize the effects of the transient behaviors of the injection at the start
31 and end of injections on the current findings. A shift of 4.3 ms between the two injections
32 is selected, to ensure that the same amount of fuel has been injected for the main and post
33 injections, at the three selected timing pairs.
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44 Figure 12 presents the soot temperature and KL distributions for the main-post injection
45 case, at three selected timing pairs. To facilitate direct, qualitative comparison, the soot
46 temperature and KL images are divided into two, with the main and post injections presented
47 at the left and right halves, respectively. The same scaling is also adopted for all time instants
48 to facilitate qualitative comparison. For the soot temperature and KL images that are
49 generated for the first timing pairs, it can be seen for the post injection event at $t_2=4.7$ ms,
50 soot region is detectable at an axial distance of ~ 20 mm and is found to extend to an axial
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3 distance of ~ 28 mm from the injector nozzle. No two-color data, however, is observed at
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5 $t_1=0.4$ ms. However, for the images that are produced for the second timing pairs, it can be
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7 seen that the soot region becomes detectable for both the main and post injections, at an
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9 axial distance of ~ 24 mm from nozzle. The soot region of the post injection at $t_2=4.9$ ms
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11 is observed to extend to an axial location of ~ 41 mm, which is more downstream than
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13 that measured for main injection at $t_1=0.6$ ms (~ 31 mm). For the third timing pairs, the
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15 same trends are observed to persist. The soot regions of both main and post injections at
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17 $t_1=0.8$ ms and $t_2=5.1$ ms are observable at similar axial distances from nozzle (~ 25 mm).
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19 The span of the soot region of the post injection at $t_2=5.1$ ms (~ 48 mm) is also found to
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21 be longer than that of the main injection at $t_1=0.8$ ms (~ 38 mm). It should be noted that
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23 the soot region that is observable in the downstream region of the post injection at all three
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25 timings are from the main injection event, which was still active, during the initiation of the
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27 combustion of the post injection.
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30 In the case of $DT=2.5$ ms, the soot temperature and KL distributions of the main and
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32 post injections are compared at three timing pairs of $t_1=0.4$ ms vs $t_2=5.7$ ms, $t_1=0.6$ ms
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34 vs $t_2=5.9$ ms and $t_1=0.8$ ms vs $t_2=6.1$ ms, and are presented in Fig. 13. The temporal
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36 positioning of these image pairs in the context of their injection rate profiles are also shown
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38 in Fig. 11. In this case, a shift of 5.3 ms between the two injections is selected to ensure the
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40 same amount of injected fuel at the three selected timing pairs. For the first timing pairs
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42 ($t_1=0.4$ ms and $t_2=5.7$ ms), it can be seen that soot region of the post injection is detectable
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44 at a distance of ~ 20 mm from the nozzle. The image that is produced at $t_1=0.4$ ms, on
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46 the other hand, is found to only contain a few data points above detection limit. For the
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48 images that are generated for the second and third timing pairs ($t_1=0.6$ ms vs $t_2=5.9$ ms
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50 and $t_1=0.8$ ms vs $t_2=6.1$ ms), the soot regions of both the main and post injection events
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52 are detectable at ~ 20 mm from the nozzle. The soot regions of the post injections are also
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54 found to have longer radial and axial spans, when compared with that observed for the main
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56 injections at corresponding time aSOI.
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3 From the soot temperature images that are produced for the post injection events in
4 Figs. 12 and 13 at $DT=1.5$ and 2.5 ms, it can be seen that the flame temperature of higher
5 values are, to some extent, more evenly distributed within the frontal regions than that
6 observed for the main injection flames at the same timings. As has been noted previously,
7 no direct flame interaction between the main and post injection flames is observed, and that
8 the coupling between the injections are mainly attributed to the interactions between the post
9 injections and the combustion products from the main injections. Therefore, the relatively
10 uniform temperature distributions that are observed in the soot temperature images of the
11 post injections, may have been caused by the remaining combustion products heating the
12 frontal regions of the incoming post injections.⁵

23 For comparison, the soot temperature and KL distributions of the main and post in-
24 jections at two ends of the investigated DT range, but at 1100 K, are also generated and
25 presented in Figs. 14 and 15. Again, the soot temperature and KL distributions of the main
26 and post injections are produced at same three selected timing pairs, and the same scaling
27 is adopted for the images to ease comparison. When comparing the soot temperature and
28 KL distributions of the main and post injections at both ambient temperatures, and across
29 the DT range, it can be seen that similar to the two-color images that were produced at
30 900 K, some discrepancies in the radial and axial spans of the main and post injection flames
31 can be observed at 1100 K. However, in contrast to the two-color images at 900 K, the soot
32 regions are already detectable for both the main and post injections, even at the first timing
33 pairs. There is also little or no soot region that is observable in the downstream region of
34 the post injection at all three timings, which indicate that there is no direct flame interac-
35 tion between the main and post injection events, despite the more advanced ignition delays
36 associated with the post injection flames at 1100 K. This is consistent with the observations
37 made in the IXT plots of the main-post injections in Fig. 10. The relatively uniform tem-
38 perature distributions across the jet that are observed for the soot temperature images of
39 the post injections, however, are less apparent at 1100 K. This may be attributable to the
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3 optical uncertainty or limitation of the two-color method, which is discussed next.
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7 **4.4 Joint soot temperature and KL probability distributions** 8 9

10 The temporal evolution of the spatially-averaged soot temperature and KL factor values of
11 main and post injections at the two ends of the investigated DT range are also plotted in
12 Fig. 16. For these plots, the average soot temperature and KL factor values are presented
13 from the start of the soot emergence until the end of soot detection. From Fig. 16, it can be
14 seen that the measured soot temperature and soot KL factor of the main and post injections
15 increase rapidly to reach local peaks, before stabilizing at lower, quasi-steady values during
16 the stabilized period of their injections. The average soot temperature and soot KL factor
17 values of the main and post injection flames, however, are observed to increase after their end
18 of injections, before the flames extinguished. It is noted that the measured values are sensitive
19 to the experimental conditions and settings used. It is therefore challenging to perform a
20 direct comparison of the current measurements with the results of previous studies. The
21 observed values and the transient characteristics, at the start and end of injections, however,
22 are broadly consistent to those measured for biodiesel flames under similar experimental
23 settings by Zhang *et al.*⁴³ The exact reasons for the higher average soot temperature and soot
24 KL factor, at the start and end of stabilized injection periods are unclear at present. However,
25 it should be noted that the timings of the first local peaks are approximately coincident
26 with the ignition delays of the flames, when the combustion processes can be expected to
27 be transient. The accuracy of the two-color data recorded could therefore be affected by
28 the presence of spatial gradients in soot properties across the flames at these time instants.
29 Previous studies^{36,37} have reported greater entrainment of ambient gases into the jet after the
30 end of injection, which can lead to changes in the soot formation and oxidation processes.
31 The second local peaks, which are observed to occur after their end of injection timings,
32 may therefore be attributable to enhanced soot oxidation in the low soot temperature and
33 KL zones from greater ambient gas entrainment. This can result in the measured average
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3 values to be dominated by soot signals from regions of higher local temperature and soot
4 concentration values. Numerical calculations were also performed for comparison with the
5 measured temperature results. For this work, zero-dimensional calculations were performed
6 for the auto ignition of stagnant adiabatic homogeneous mixtures at initial ambient pressure
7 and temperature values of 5.1 MPa and 900 K, respectively, with 15% oxygen concentration.
8 A skeletal mechanism with 115 species and 460 reactions⁴⁴ was used. It is noted previous
9 studies^{45,46} have reported that methyl decanoate/n-heptane mixtures are good surrogates
10 for canola oil based biofuels, an equimolar blend of methyl decanoate and n-heptane as was
11 therefore used as the biodiesel surrogate mixture for the calculations. The results of the
12 numerical calculations reveal that a maximum temperature of 2200 K can be attained at the
13 simulated ambient condition, which is lower than the maximum average temperature value
14 of 2316 K that was experimentally observed during the quasi-steady period for the canola
15 oil biodiesel. As is noted previously, the two-color results can significantly overestimate
16 the actual flame temperature value and are biased towards the soot in the hottest flame
17 surface that is located closest to the detector. In addition, there is also a difference in the
18 higher heating values of methyl decanoate (*i.e.*, 36.7 MJ/kg) and canola oil biodiesel (*i.e.*,
19 38.1 MJ/kg).²³ All these factors contribute to the difference in measured temperature.
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37 Joint probability density functions (PDFs) have been demonstrated to be useful in re-
38 vealing statistical relationships between the variables of interest^{47,48} and are used to provide
39 a measure of the soot temperature and soot KL values occurring concurrently at the same
40 point in time for the main and post injection events. The joint PDFs between the soot tem-
41 perature and KL factor at the three selected timing pairs for both main-post injection cases
42 are generated and presented in Figs. 17 and 18, with the pseudo color contour representing
43 the probability of the data sets. From the PDFs, it can be seen that the spans and the
44 average measured soot KL values decrease as the average measured soot temperature values
45 increase. It is noted that the overall traits of the PDFs obtained are consistent with those of a
46 soot temperature versus soot KL temperature correlation plot for an n-heptane flame, which
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3 was also measured using two-color pyrometry technique in a previous study.³¹ In previous
4 studies,⁴⁹ optical diagnostics have shown that diesel jet flame comprises of a relative cooler
5 inner jet core that is surrounded by a thin diffusion flame, with soot occurring throughout
6 the jet cross section. The two-color data obtained from a diffusion flame is therefore be more
7 weighted towards the soot present in the hotter diffusion flame reaction zone, than in the
8 flame core. In addition, as the temperature of the flame increases, the weight of the soot
9 signal from the flame front would also increase in relation to the soot signal from the flame
10 core, such that the two-color data would become more representative of the soot properties
11 in the flame edge only. All these can contribute towards the lower measured soot KL and
12 span at higher flame temperatures observed in the PDFs.
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23 In the case of $DT=1.5$ ms, for the PDF pairs that are generated for the first time instants
24 ($t_1=0.4$ ms and $t_2=4.7$ ms), it can be seen that no data point is detected at $t_1=0.4$ ms. This
25 is to be expected, given the measured ignition delay of the flame is ~ 0.6 ms (see Fig. 8) and
26 therefore the combustion process has not commenced at this time instant. The measured
27 soot temperature values at $t_2=4.7$ ms, on the other hand, are found to be distributed between
28 1900 K and 2500 K. From Fig. 8, it can be seen that at $DT=1.5$ ms, the measured ignition
29 delay of the post injection is found to be ~ 0.37 ms aSOI. Therefore, the combustion of
30 the post injection would have initiated prior to the first time instant for which the image
31 pairs is selected for comparison. Nonetheless, the observed trend at $t_2=4.7$ ms is mainly
32 attributed to the burnout of the main injection, which is the dominant combustion event at
33 this time instant. From the PDFs that are produced for the second and third timing pairs,
34 it can be seen that the soot temperatures measured at $t_2=4.9$ ms and 5.1 ms, are distributed
35 between 1900 K and 2700 K. These values are not only higher than the temperature of
36 the main injection combustion events observed at $t_1=0.6$ ms and 0.8 ms (between 1600 K
37 and 2380 K), but also higher than those of the combustion process of the main injection at
38 $t_2=4.7$ ms. From Fig. 12, it can be seen that whilst the combustion of the main injection
39 was still active at $t_2=4.9$ ms and 5.1 ms, the combustion regions that are associated with
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3 the main injection are small, and therefore do not significantly influence the overall shapes
4 and trends of the PDFs at these time instants.
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7 In the case of $DT=2.5$ ms, from the PDFs that are generated for the first timing pairs
8 ($t_1=0.4$ ms and $t_2=5.7$ ms), it can be seen that no data point is again detected at $t_1=0.4$ ms.
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10 The data points for the PDF that is generated for $t_2=5.7$ ms, however, are observed to be
11 relatively scattered. It is noted that at this time instant, which corresponds to 0.4 ms after
12 the start of second injection, is approximately coincident with the measured ignition delay
13 of the second injection. Given that the combustion process was still initiating, the images
14 recorded would therefore only contain a low sample size of soot temperature and KL data.
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16 From the PDFs that are produced for the second and third timing pairs, it can be seen that
17 the temperature values measured at $t_2=5.9$ ms and 6.1 ms, are distributed between 1900 K
18 and 2650 K. The measured temperature values for the post injections are again found to be
19 higher than that observed for the main injection combustion events at $t_1=0.6$ ms and 0.8 ms
20 (between 1600 K and 2400 K). As is noted previously, the two-color pyrometry technique
21 has significant temperature uncertainty and therefore the temperature values derived should
22 only be used for qualitative comparison. Nonetheless, the overall trends of the PDFs are
23 consistent in showing that combustion of the post injection events were occurring at higher
24 temperature values. From the PDFs that are presented in Figs. 17 and 18, it can also be
25 seen that the most probable soot KL factors of the post injection are generally observed to
26 have narrower distributions and lower average values than that of the main.
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43 For comparative measurements, the temporal evolution of the spatially-averaged soot
44 temperature and KL factor values of main and post injections at an ambient temperature
45 condition of 1100 K, are also plotted in Fig. 16. When comparing the plots in Figs. 16
46 and 19, it can be seen that the plots share similar overall characteristics, but the average
47 soot temperature and soot concentration factor profiles of the main-post injection cases at
48 1100 K, are less transient at their start of injections and are observed to attain more stable
49 quasi-steady values. As is discussed previously, the higher ambient temperature results in a
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3 shorter ignition delay, which can contribute towards the flame having more time to attain a
4 quasi-steady state, prior to its end of injection. From Fig. 19, the average soot KL factors of
5 the flames at 1100 K in Fig. 19 are observed to be approximately two times greater than the
6 measured values at 900 K. As is noted in previous studies,²⁰ an increase in the ambient gas
7 temperature can result in a shortening of the lift-off length, and hence, reduced amount of
8 fuel-air premixing occurring upstream. This can cause the soot processes to initiate earlier
9 and hence, the peak soot level of the flame to increase, as is observed in this work.
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17 The joint PDFs for both main-post injection cases at the three selected timings are also
18 presented in Figs. 20 and 21. From the figures, it can be seen that some trends in the joint
19 PDFs are already observable, even for the images that were recorded for the first timing
20 pairs. Given that all of the measured ignition delay of the flames are earlier than ~ 0.27 ms
21 (see Fig. 10), the combustion processes for the flames would have commenced to generate
22 sufficient emission signals that can be used for two-color measurements at the first time
23 instants ($t_1=0.4$ ms and $t_2=4.7$ ms). From the figures, it can be seen when $DT=1.5$ ms,
24 the temperature values of the main injection at $t_1=0.4$ ms are distributed between 2000 and
25 2400 K, whereas the measured values for the post injection to span from 2000 to 2600 K
26 at $t_2=4.7$ ms. The distributions and the average values of the PDFs for the main and
27 post injections, however, are similar for the second and third timing pairs. In the case of
28 $DT=2.5$ ms, the overall distributions and the average values of the PDFs for the main and
29 post injections are alike for all three timing pairs. The general similarity in the distributions
30 and average values observed for the post injections, across the varied DTs, implies that
31 the changes in the soot temperature and concentration distributions of the post injections
32 that arise from their interactions with the combustion products from the main pulse are
33 within measurement uncertainty. This is consistent with the earlier observations of the
34 relative invariant intensity distributions in the IXT plots of the post injection flames in
35 Fig. 10. From the figures, it can be seen the most probable soot KL factors of the PDFs at
36 1100 K are distributed over a wider range of soot concentration values than that observed for
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3 the PDFs at 900 K. As is discussed previously, an increase in ambient gas temperature can
4 enhance the soot formation process, and therefore the soot content of the flame. Nonetheless,
5 previous studies³¹ have also indicated that, as the temperature across the flame volume is
6 increased, the measurement would become more and more influenced by the soot in both
7 the flame region and jet core, therefore producing measurements that are higher, but more
8 representative of the soot properties across the flame volume.
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11 Together, the PDF results and the findings presented in the previous sections demon-
12 strate that the ignition and combustion characteristics of the post injections are affected by
13 their interactions with the combustion products from the main injections, over the tested
14 DT range. The results indicate that the changes in soot temperature and concentration
15 distributions are affected by the extent of the interactions between the injections, such that
16 the post injection event with the shortest DT (*i.e.*, 1.5 ms) is found to ignite earlier with
17 soot zone that developed more rapidly with higher temperature and soot concentration. It
18 is presently unclear, however, if the higher flame temperature would result in more effective
19 soot oxidation, or if the more rapid soot zone development would lead to increased engine-
20 out soot emissions. It should be noted that the two-color data would become more biased
21 towards the soot properties at the flame surface, because of the higher temperature values
22 of the post injection combustion process, and this could also contribute towards the lower
23 soot KL values observed. Further investigation, including using more quantitative soot con-
24 centration and temperature imaging techniques such as laser-induced incandescence (LII)
25 and nonlinear two-line atomic fluorescence (NTLAF) methods,⁵⁰⁻⁵³ is required to confirm
26 the current trends qualitatively and to extend them to actual engine outputs.
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49 5 Conclusion

50 An experiment was performed in an optically-accessible, constant-volume combustion cham-
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3 A compression-ignition (CI) engine environment with an ambient density, bulk temperature
4 and oxygen concentration of 19.4 kg/m^3 , 900 K and 15 vol.% O_2 , respectively, were used.
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6 A mass ratio of the main to post injections of 80% to 20% was maintained for the main-post
7 injections, but the DT between the injections were varied from 1.5 ms to 2.5 ms. A canola
8 oil based biodiesel was used and the injection pressure of the fuel was fixed at 100 MPa.
9
10 Comparative measurements were performed using the same fuel and injection schedules, but
11 subjected to a higher ambient gas temperature condition of 1100 K. For this work, diffused-
12 back illumination and high-speed flame luminosity imaging techniques were used to obtain
13 liquid phase and combustion information of the test cases. The results indicated that under
14 the test conditions of this work, the ignition delays, ignition locations and the flame lift-off
15 lengths of the post injection flames were found to be consistently shorter than that of the
16 main-flames. The differences in ignition delays and locations between the main and post
17 injection flames, however, were found to reduce with increasing DT, which suggest that the
18 observed modifications in the ignition and combustion behaviors of the post injections ap-
19 peared to be driven by the extent of their interactions with the combustion products of the
20 main flames. Two-color pyrometry technique was also used to provide soot temperature and
21 soot KL information for the main-post injection cases. From the two-color data, it can be
22 seen that the interaction between the main and post injections was found to cause the soot
23 zones of the post injections to develop more rapidly, and at higher temperature values, after
24 the ignition. The distribution of the most probable soot KL factors of the post injections
25 were found to be narrower, and have lower soot content values. Further studies, however,
26 are required to validate the observed soot concentration trends.
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Table 1: Summary of test conditions, fuel composition, properties and injection conditions.

Test conditions	
Ambient density (kg/m ³)	19.4
Ambient pressure (MPa)	5.1, 6
Bulk temperature at injection (K)	900, 1100
Oxygen level (vol.%)	0 (non-reacting), 15 (reacting)
Fuel fatty acid profiles (wt%)	
Palmitic, C16:0	4.3
Stearic, C18:0	2.2
Oleic, C18:1	63.5
Linoleic, C18:2	18.9
Linolenic, C18:3	9.2
Eicosanoic, C20:0	0.4
Eicosenoic, C20:1	1.1
Fuel properties	
Fuel abbreviation	C1875
Oxygen content (wt%)	10.83
Iodine number	105
Saponification number	185
Cetane number	59
Fuel injection conditions	
Nozzle diameter (μm)	105
Injection pressure (MPa)	100
Injection quantity (mg)	10 (single) 8:2 (main-post)
Injection duration (ms)	4.87 (single) 3.8:1 (main-post)
Dwell time (ms)	Single, 1.5, 2.0 and 2.5

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4 13 Comparisons of spatial distributions of typical, instantaneous soot temperature and soot KL of the main (left half) and post injections (right half), at
5 three selected timing pairs, for the main-post case with a dwell time (DT) of
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7 temperature: 900 K. 48
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13 temperature: 1100 K. 49
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15 15 Comparisons of spatial distributions of typical, instantaneous soot temperature
16 and soot KL of the main (left half) and post injections (right half), at
17 three selected timing pairs, for the main-post case with a dwell time (DT) of
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21 16 The time-resolved results for spatially-averaged soot two-color temperature
22 (upper) and soot KL factor values (lower) for the main-post injection cases
23 with dwell times (DTs) of 1.5 and 2.5 ms, respectively. The start of injection
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27 17 Comparisons of joint PDFs of soot temperature and soot KL of the main
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48 21 Comparisons of joint PDFs of soot temperature and soot KL of the main
49 (left) and post (right) injections at three selected time steps, for a main-post
50 injection case with a dwell time (DT) of 2.5 ms. All time instants have the
51 same color scale. Ambient temperature: 1100 K. 56
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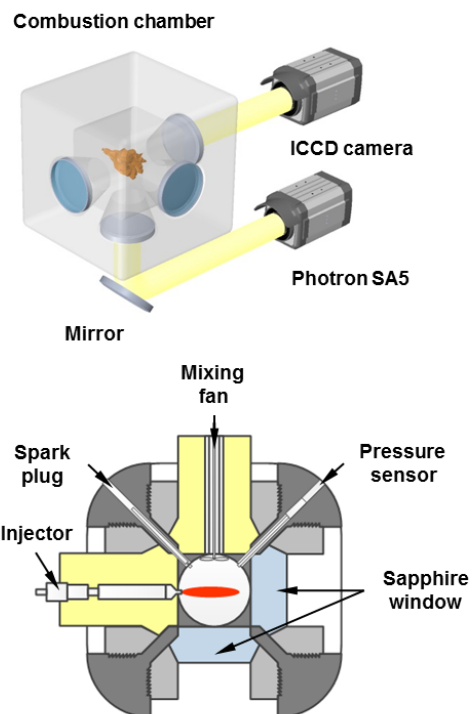


Figure 1: Schematic diagram of the experimental arrangement, including the combustion chamber and high-speed flame luminosity imaging setup.

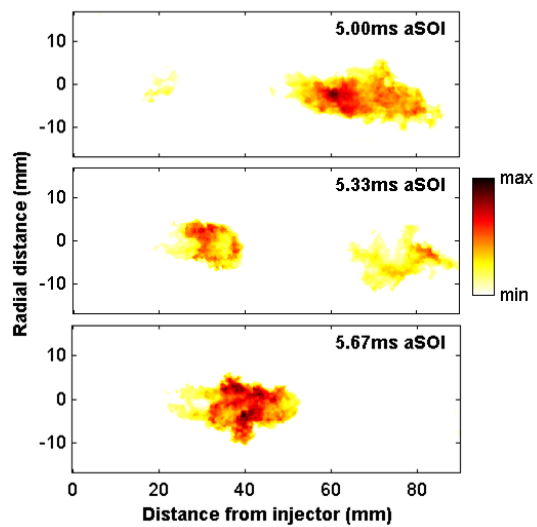


Figure 2: Typical time-sequenced flame luminosity images for a main-post injection case, with a dwell time (DT) of 1.5 ms. The fuel is injected from left to right in these images.

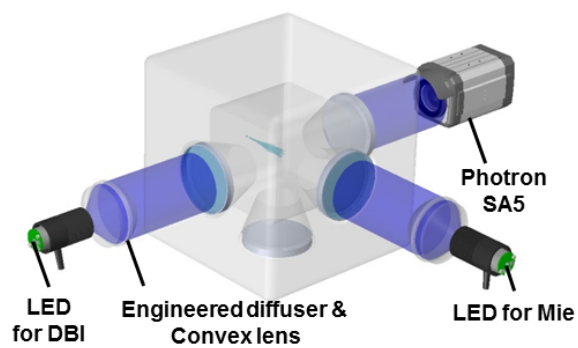


Figure 3: Schematic diagram of the experimental arrangement, including the combustion chamber and diffused back illumination and Mie-scattering imaging setup.

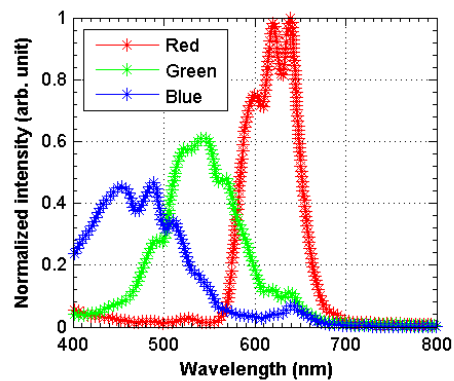


Figure 4: Normalized optical response of the red, green and blue channels of the high-speed camera used.

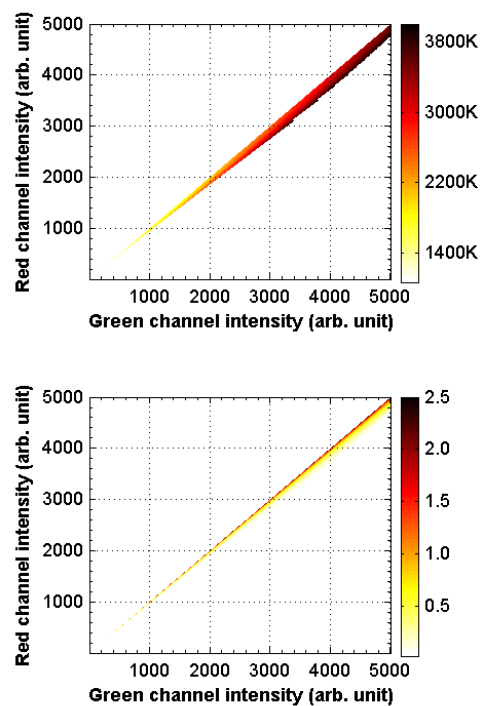


Figure 5: Soot temperature (top) and soot KL (bottom) surfaces in the domain of red and green signal intensity values, expressed in arbitrary units.

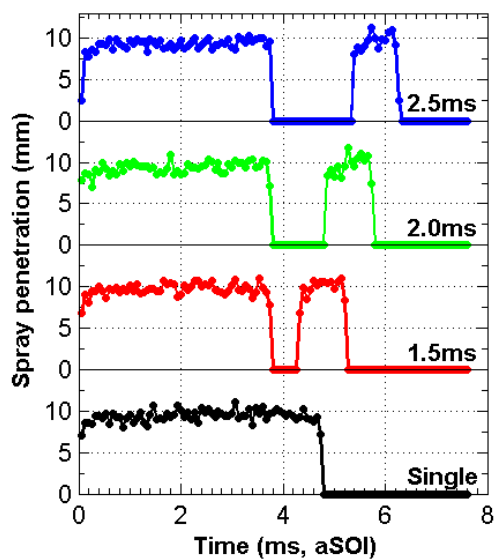


Figure 6: Liquid penetration profiles, as a function of time after start of injection (aSOI), for the main-post and single injection cases. The dwell times of the profiles are also indicated on the plot.

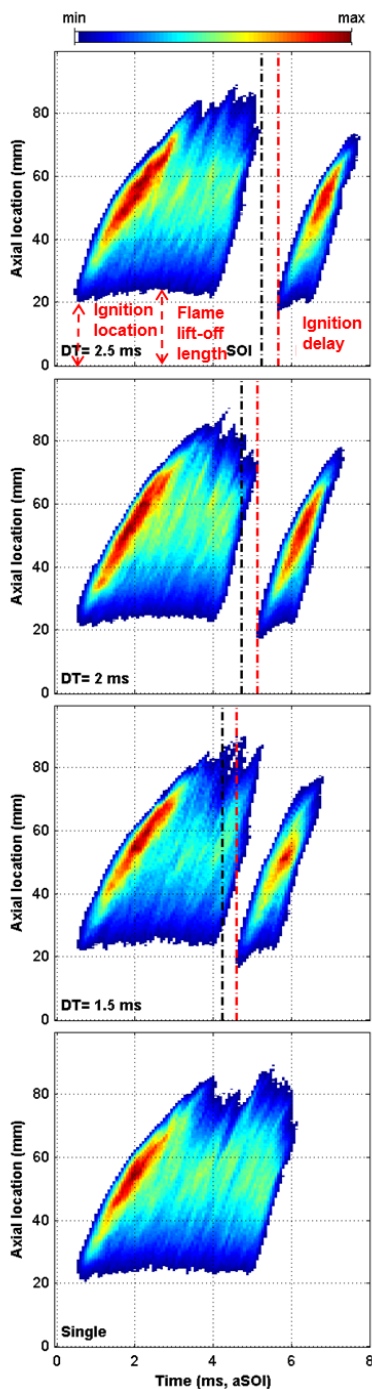


Figure 7: Average Intensity-axial-Time (IXT) plots for the main-post and single injection cases. The start of injection timings and ignition delays of the post injections are indicated with dashed lines. Ambient temperature: 900 K. Fuel: Canola oil biodiesel.

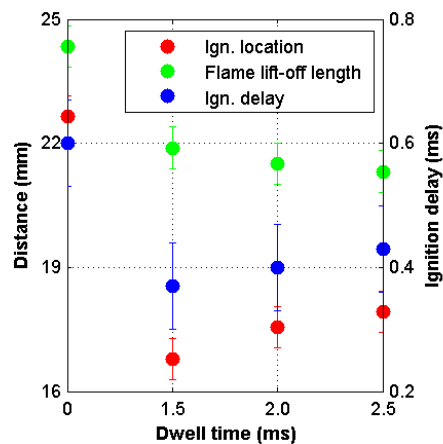


Figure 8: Ignition delay, ignition location and average flame lift-off length values of the main and post injection events for the main-post injection cases with dwell times (DTs) of 1.5, 2.0 and 2.5 ms. Ambient temperature: 900 K.

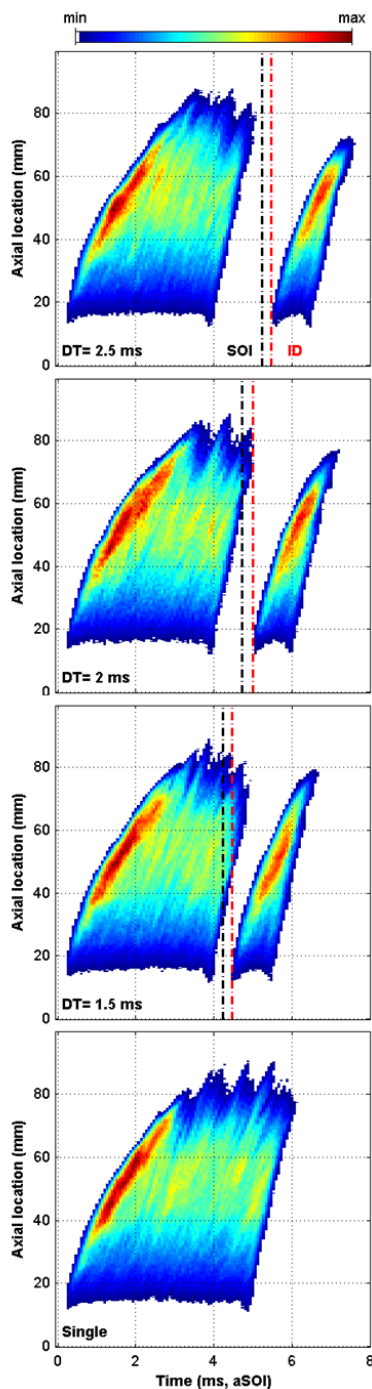


Figure 9: Average Intensity-axial-Time (IXT) plots for the main-post cases. The start of injection timings and ignition delays of the post injections are indicated with dashed lines. Ambient temperature: 1100 K.

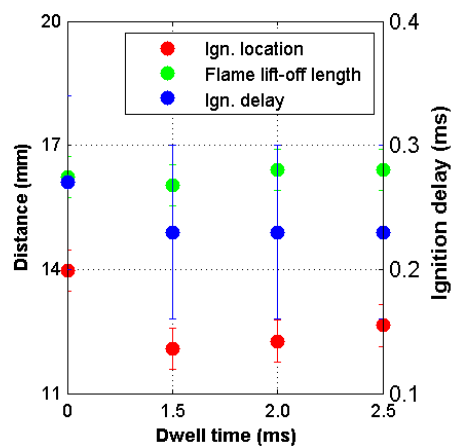


Figure 10: Ignition delay, ignition location and average flame lift-off length values of the main and post injection events for the main-post injection cases with dwell times (DTs) of 1.5, 2.0 and 2.5 ms. Ambient temperature: 1100 K.

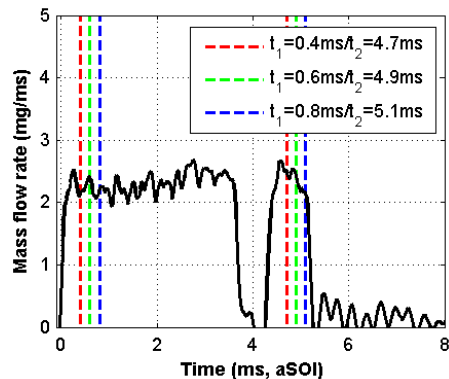


Figure 11: Injection rate profiles for the main-post injection cases, with a fixed fuel mass ratio of main to post injections of 80% to 20%, but with varied dwell times (DTs) of 1.5 ms (top) and 2.5 ms (bottom). t_1 and t_2 represent selected time instants after the start of injection, for the main and post injections, respectively. For DT=1.5 ms (top), the two-color data for the main and post injections are compared at three selected timing pairs of $t_1=0.4$ ms vs $t_2=4.7$ ms, $t_1=0.6$ ms vs $t_2=4.9$ ms and $t_1=0.8$ ms vs $t_2=5.1$ ms, respectively. For DT=2.5 ms (bottom), the two-color data for the main and post injections are compared at three selected timing pairs of $t_1=0.4$ ms vs $t_2=5.7$ ms, $t_1=0.6$ ms vs $t_2=5.9$ ms and $t_1=0.8$ ms vs $t_2=6.1$ ms, respectively.

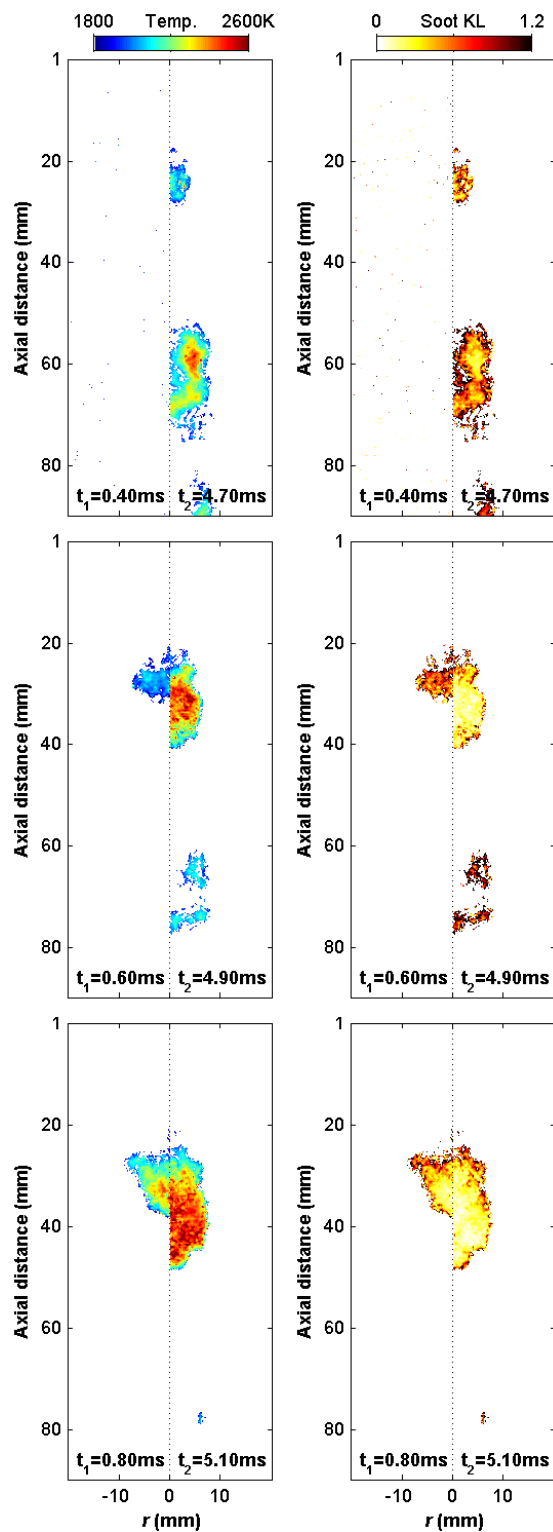


Figure 12: Comparisons of spatial distributions of typical, instantaneous soot temperature and soot KL of the main (left half) and post injections (right half), at three selected timing pairs, for the main-post case with a dwell time (DT) of 1.5 ms. The fuel is injected from the top to bottom, in these images. Ambient temperature: 900 K.

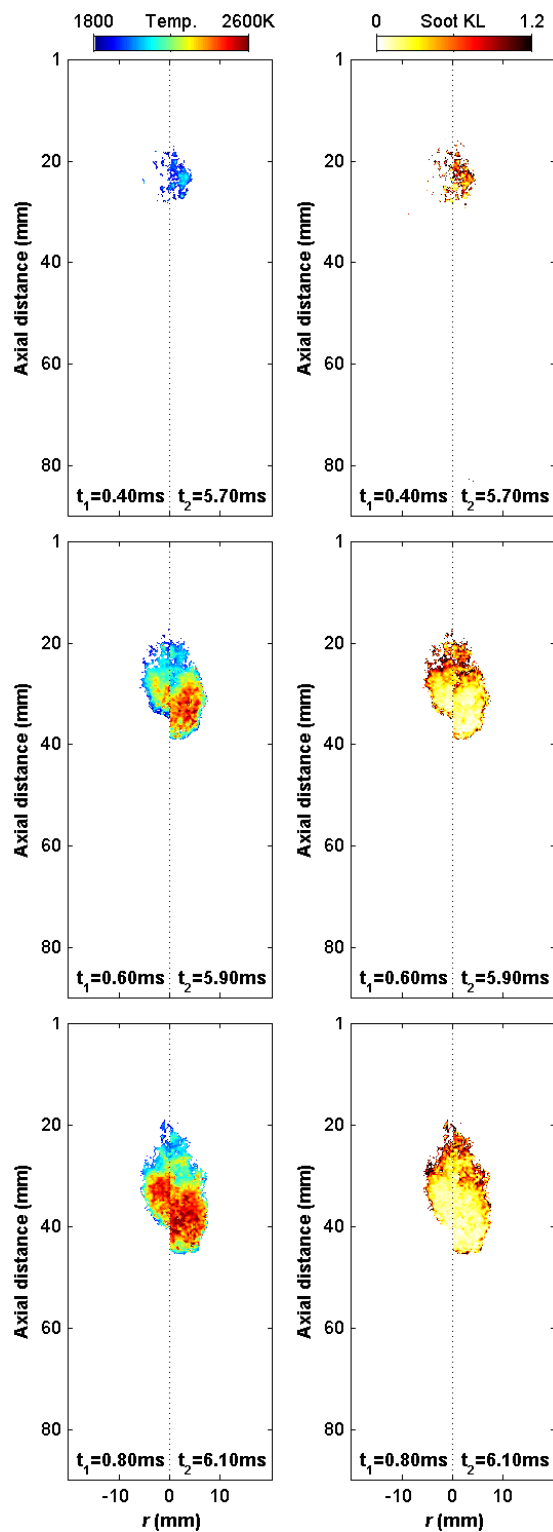


Figure 13: Comparisons of spatial distributions of typical, instantaneous soot temperature and soot KL of the main (left half) and post injections (right half), at three selected timing pairs, for the main-post case with a dwell time (DT) of 2.5 ms. The fuel is injected from the top to bottom, in these images. Ambient temperature: 900 K.

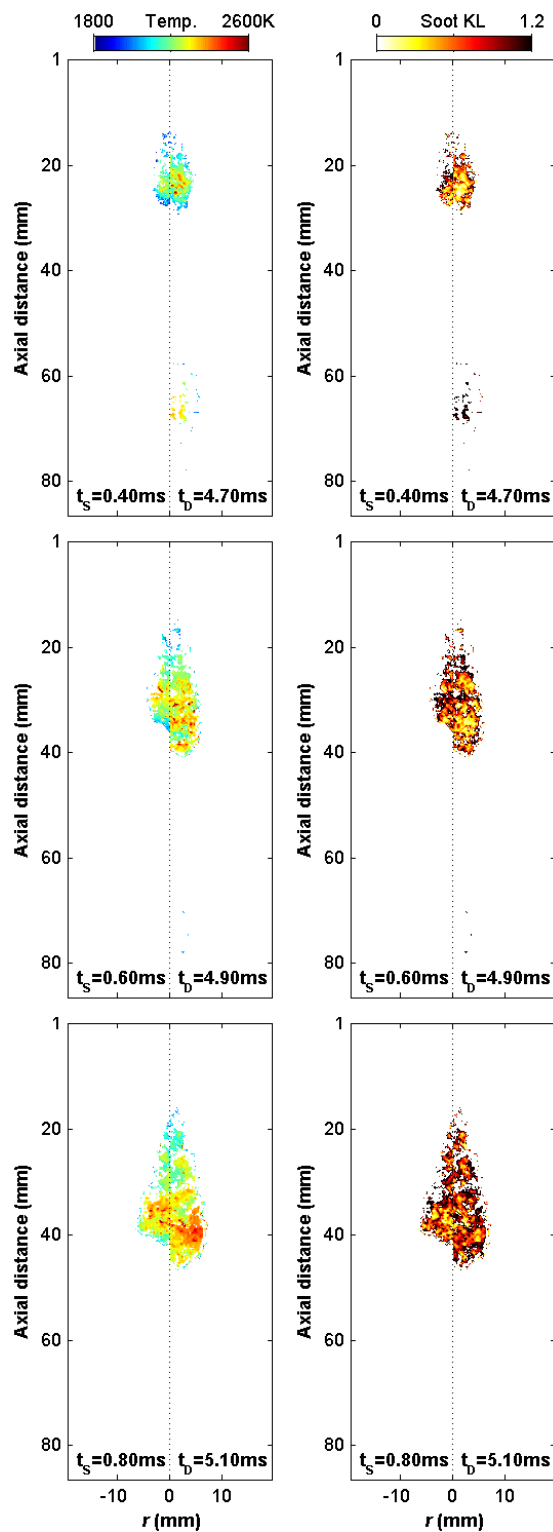


Figure 14: Comparisons of spatial distributions of typical, instantaneous soot temperature and soot KL of the main (left half) and post injections (right half), at three selected timing pairs, for the main-post case with a dwell time (DT) of 1.5 ms. The fuel is injected from the top to bottom, in these images. Ambient temperature: 1100 K.

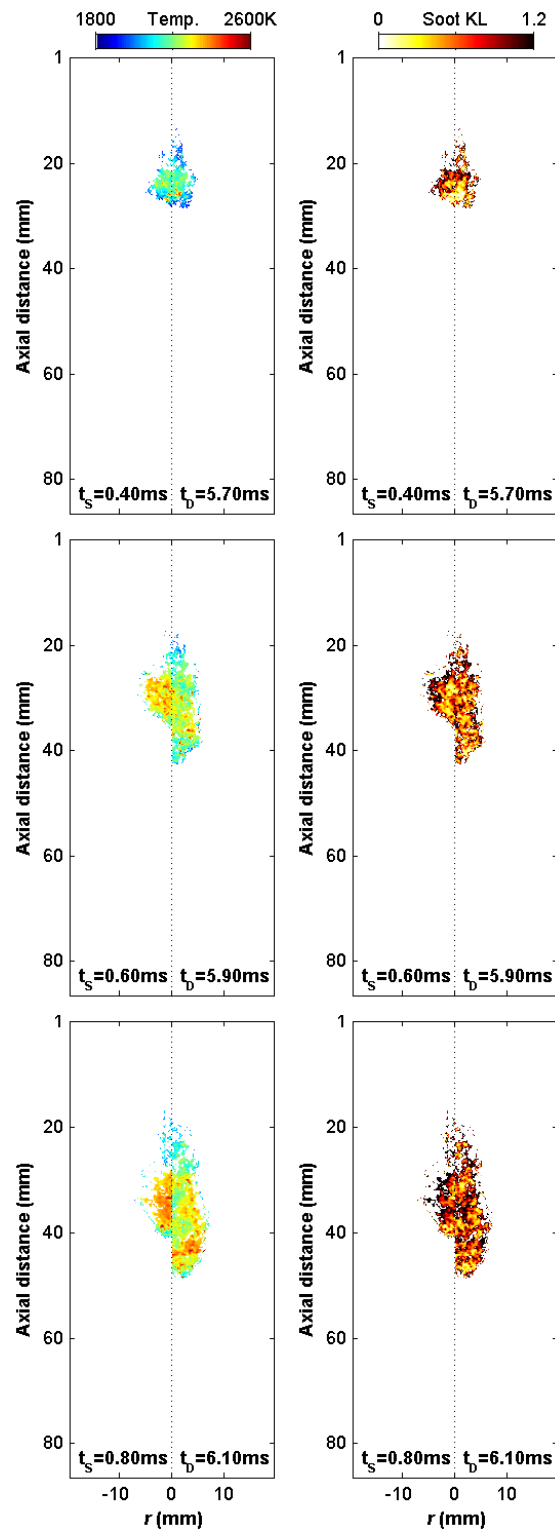


Figure 15: Comparisons of spatial distributions of typical, instantaneous soot temperature and soot KL of the main (left half) and post injections (right half), at three selected timing pairs, for the main-post case with a dwell time (DT) of 2.5 ms. The fuel is injected from the top to bottom, in these images. Ambient temperature: 1100 K.

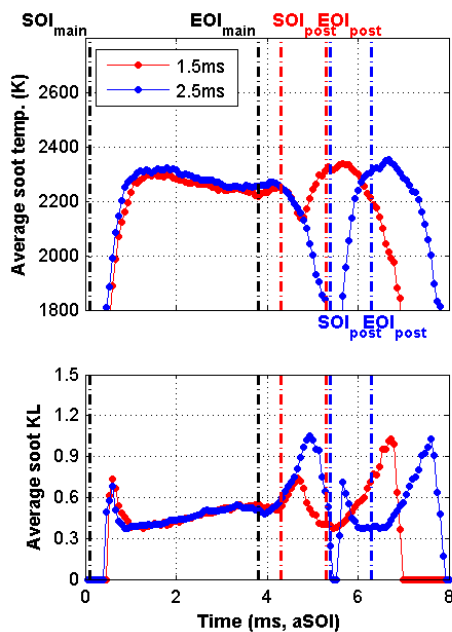


Figure 16: The time-resolved results for spatially-averaged soot two-color temperature (upper) and soot KL factor values (lower) for the main-post injection cases with dwell times (DTs) of 1.5 and 2.5 ms, respectively. The start of injection and end of injection timings for the main-post injection cases are indicated on the plots using dashed lines. Ambient temperature: 900 K.

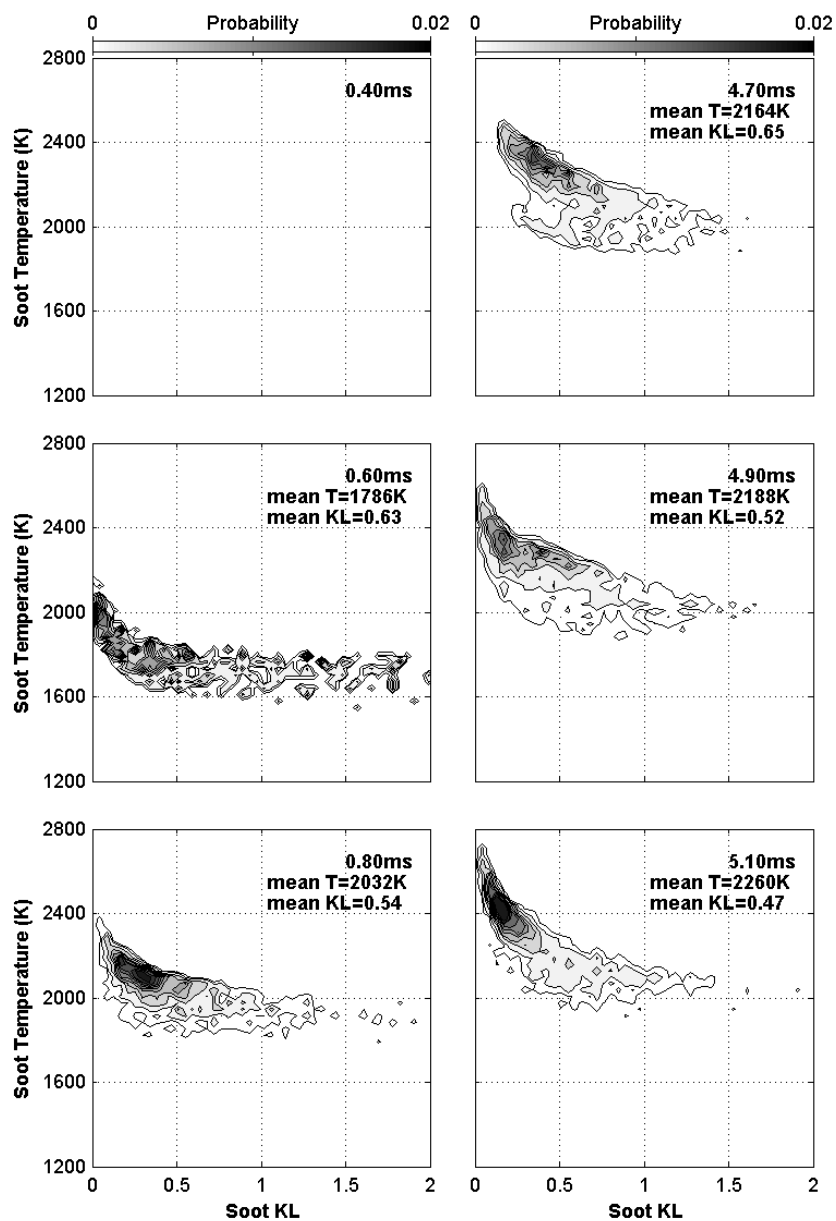


Figure 17: Comparisons of joint PDFs of soot temperature and soot KL of the main (left) and post (right) injections at three selected time steps, for a main-post injection case with a dwell time (DT) of 1.5 ms. All time instants have the same color scale. Ambient temperature: 900 K.

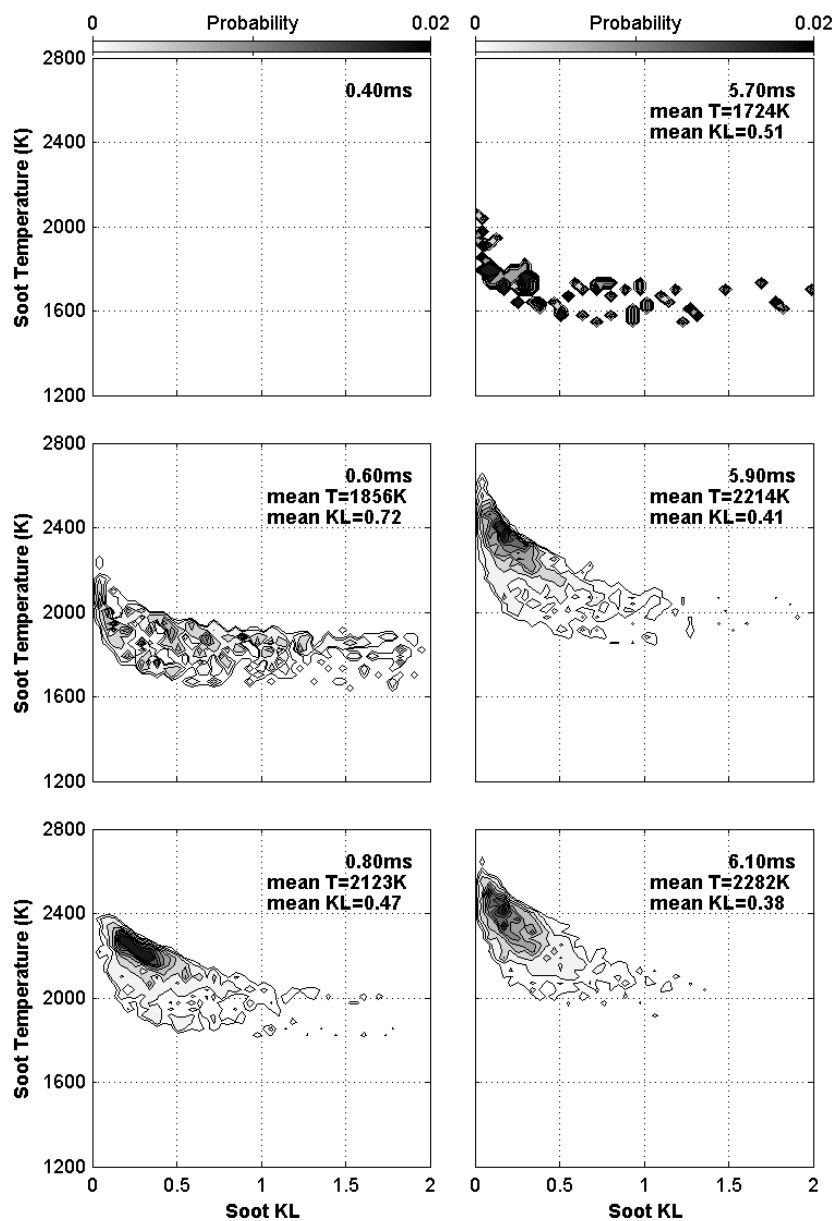


Figure 18: Comparisons of joint PDFs of soot temperature and soot KL of the main (left) and post (right) injections at three selected time steps, for a main-post injection case with a dwell time (DT) of 2.5 ms. All time instants have the same color scale. Ambient temperature: 900 K.

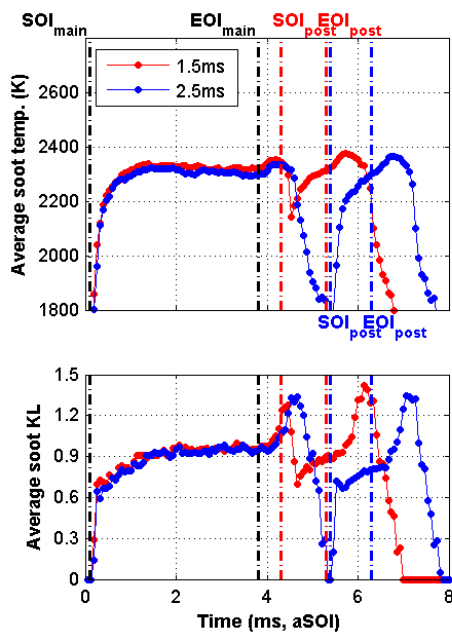


Figure 19: The time-resolved results for spatially-averaged soot two-color temperature (upper) and soot KL factor values (lower) for the main-post injection cases with dwell times (DTs) of 1.5 and 2.5 ms, respectively. The start of injection and end of injection timings for the main-post injection cases are indicated on the plots using dashed lines. Ambient temperature: 1100 K.

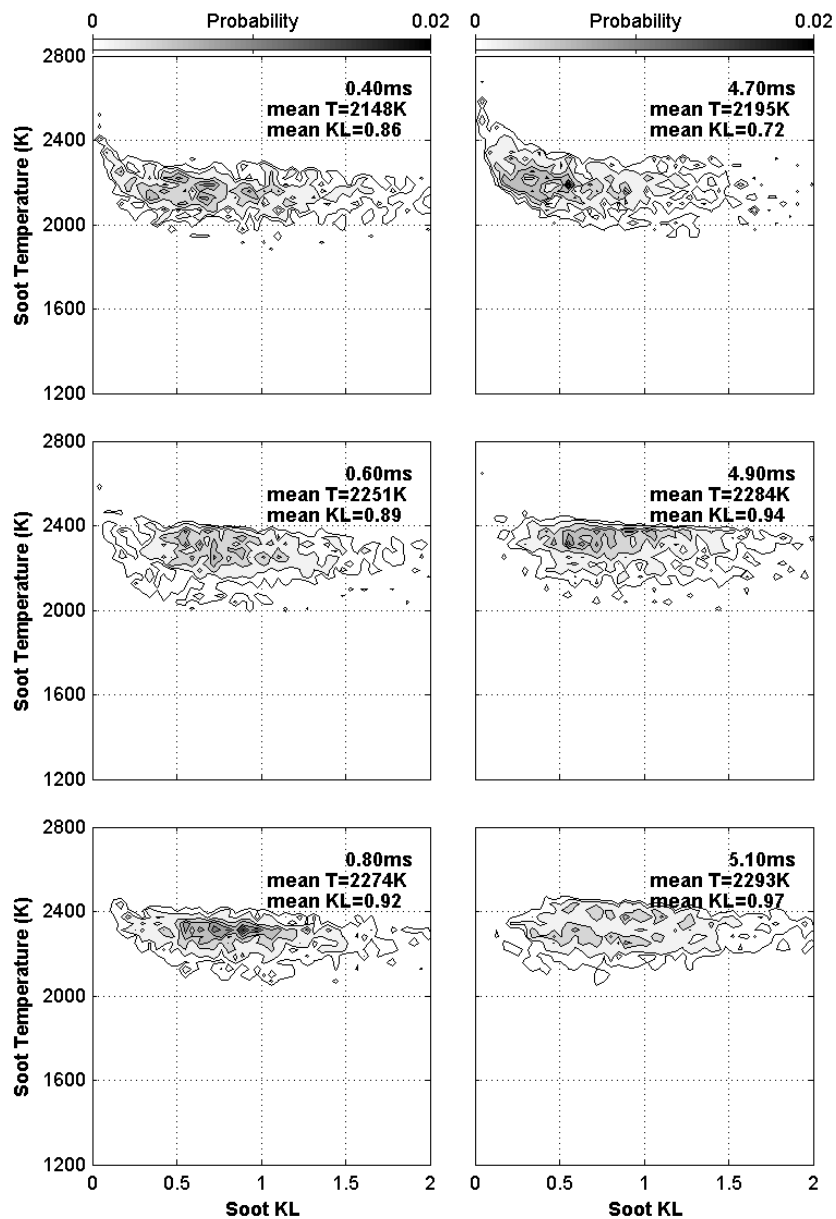


Figure 20: Comparisons of joint PDFs of soot temperature and soot KL of the main (left) and post (right) injections at three selected time steps, for a main-post injection case with a dwell time (DT) of 1.5 ms. All time instants have the same color scale. Ambient temperature: 1100 K.

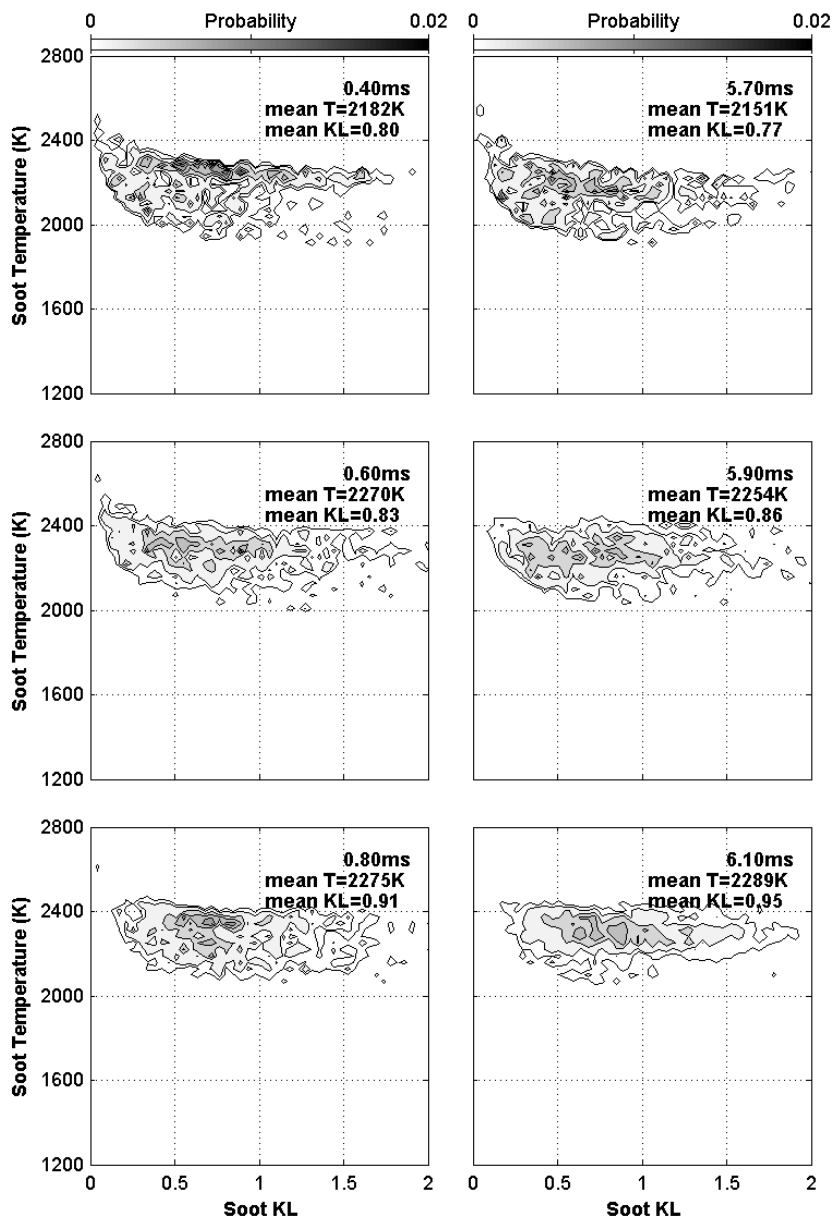
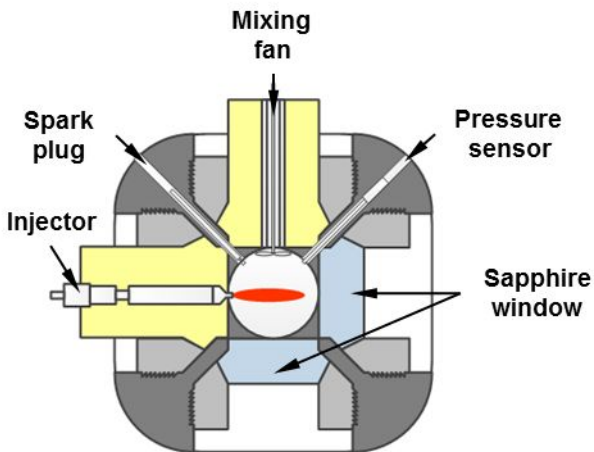
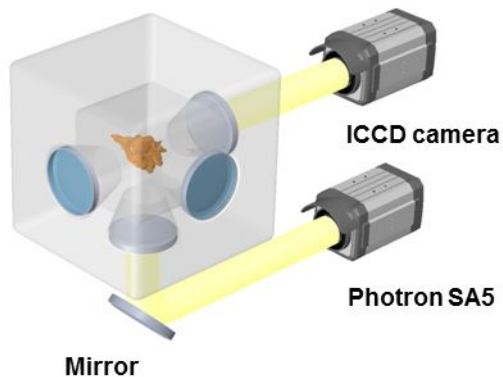
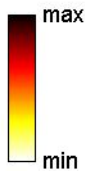
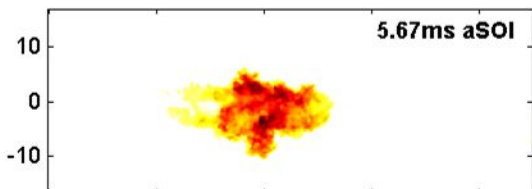
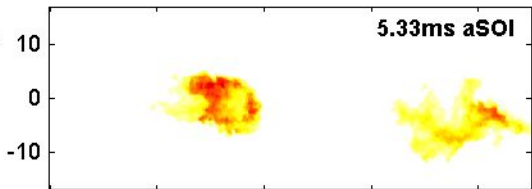
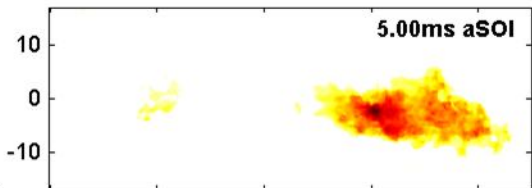


Figure 21: Comparisons of joint PDFs of soot temperature and soot KL of the main (left) and post (right) injections at three selected time steps, for a main-post injection case with a dwell time (DT) of 2.5 ms. All time instants have the same color scale. Ambient temperature: 1100 K.

Combustion chamber

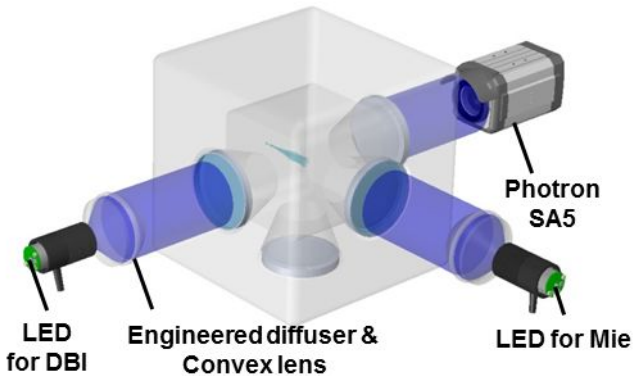


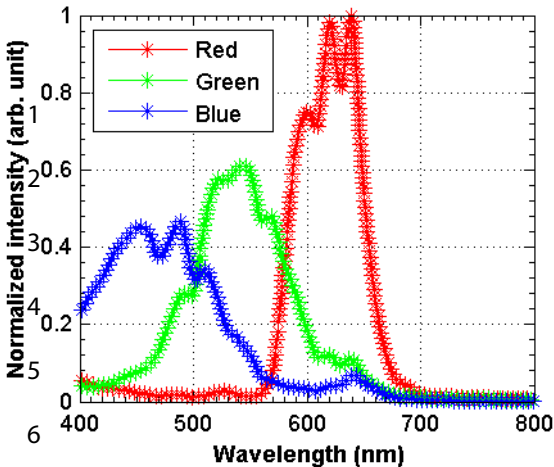
Radial distance (mm)

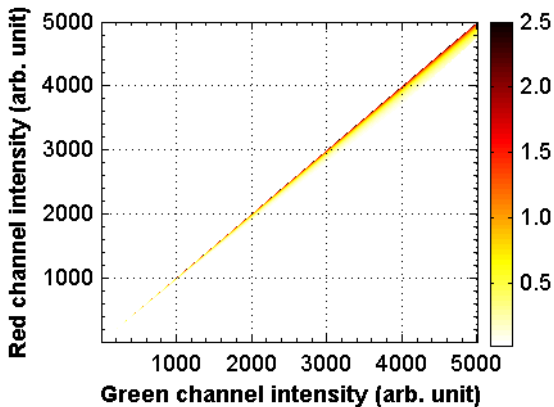


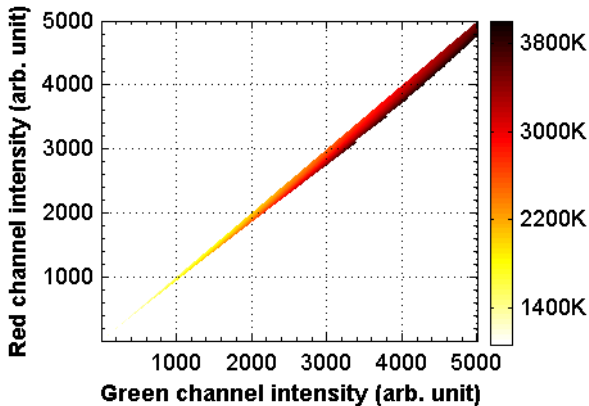
0 20 40 60 80

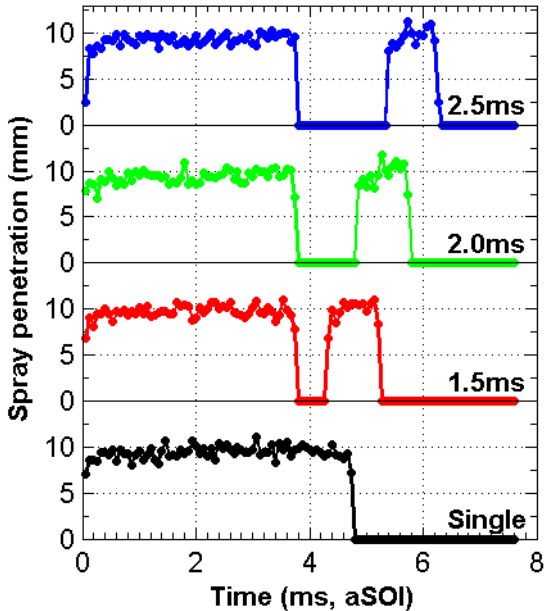
Distance from injector (mm)

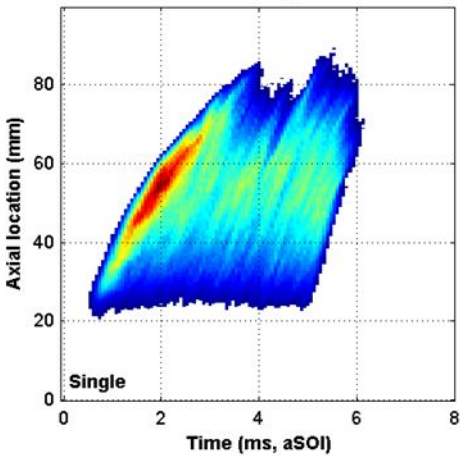
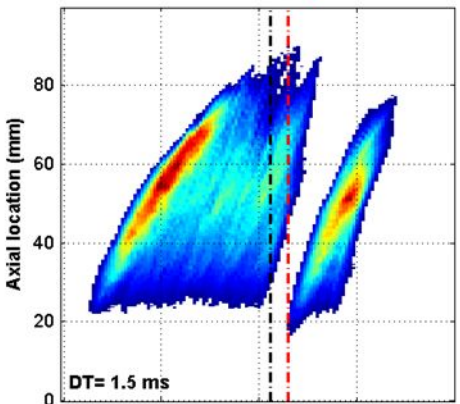
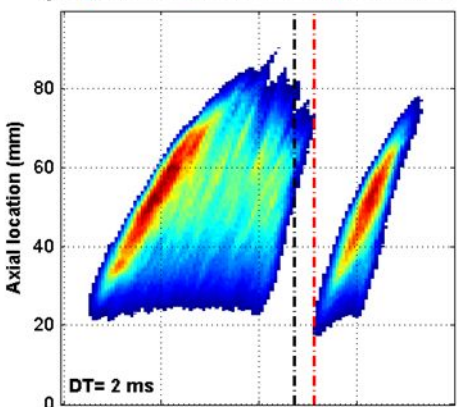
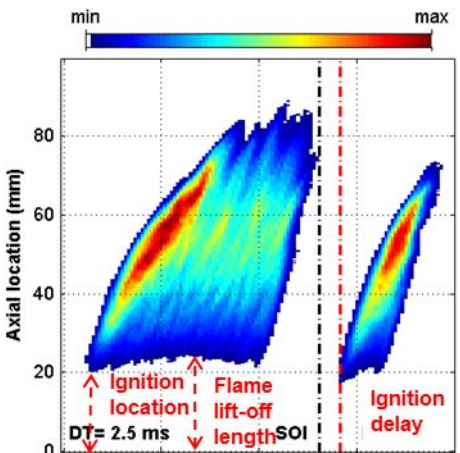


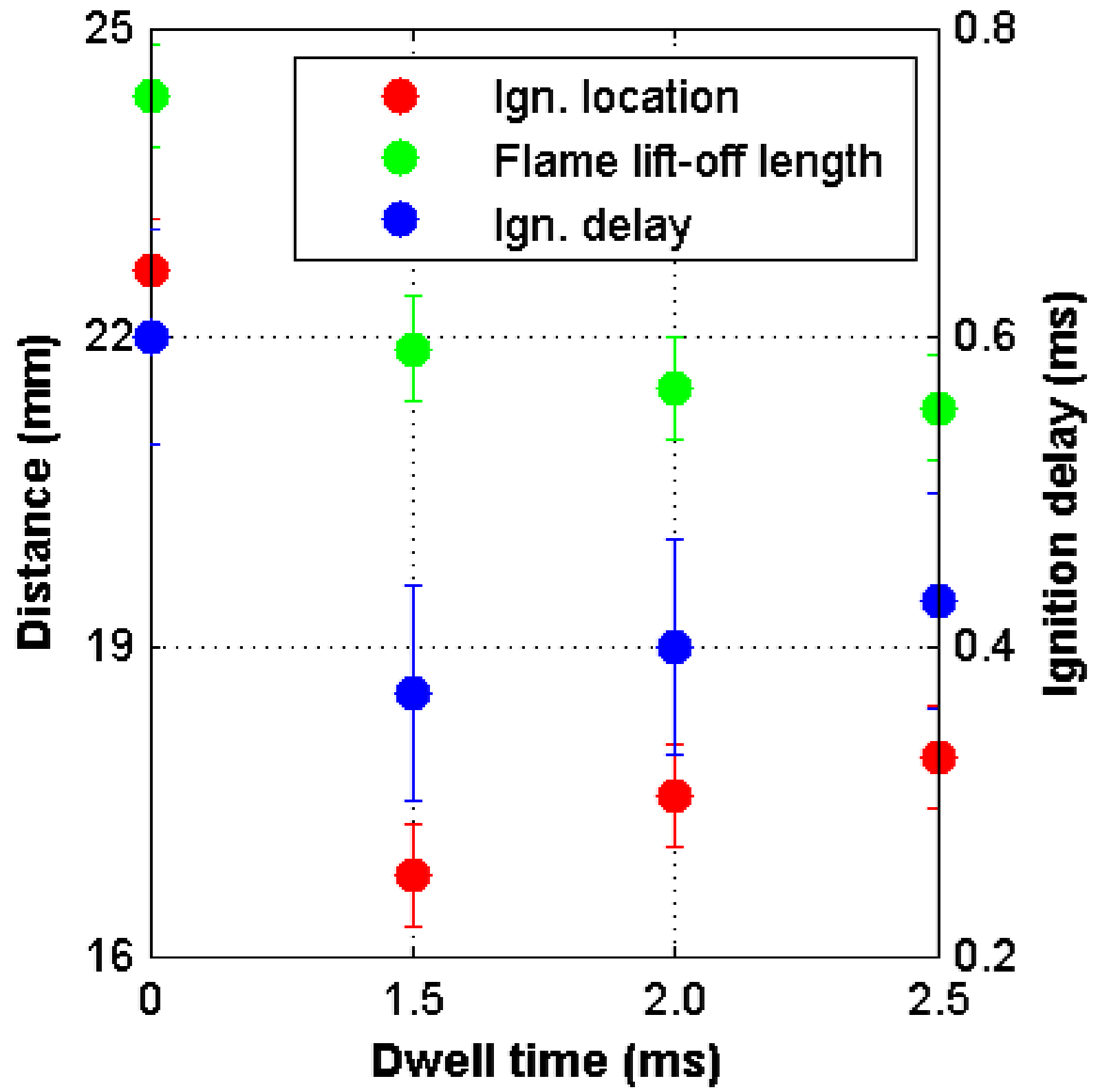


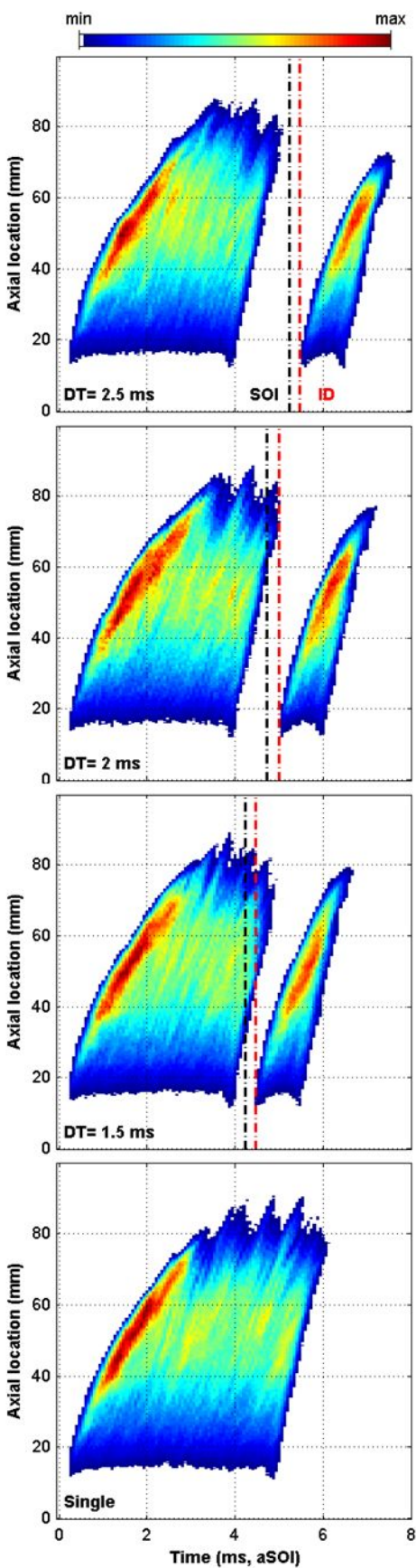


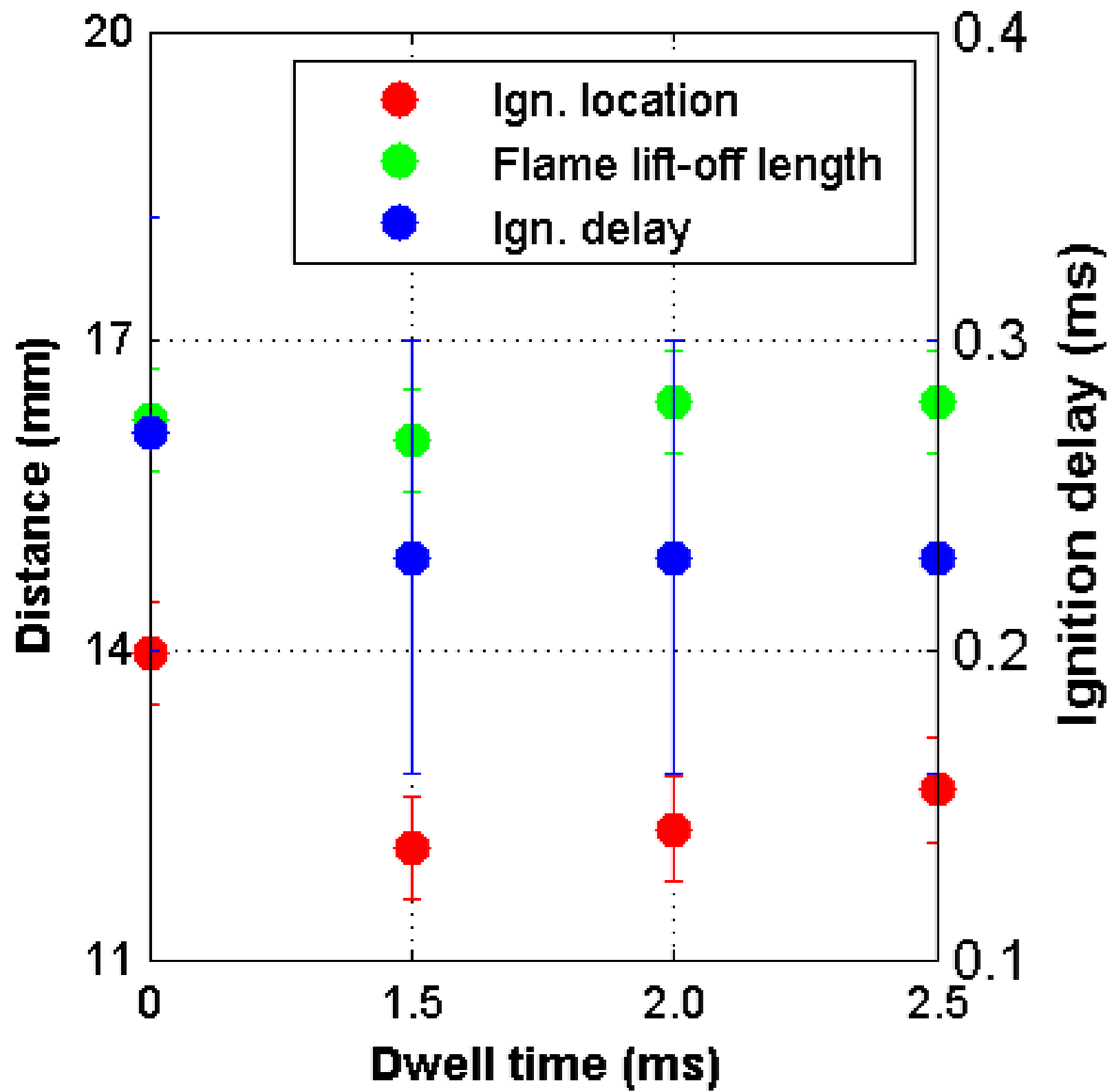


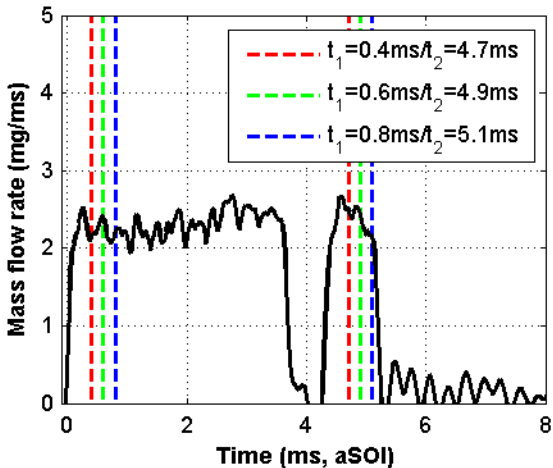




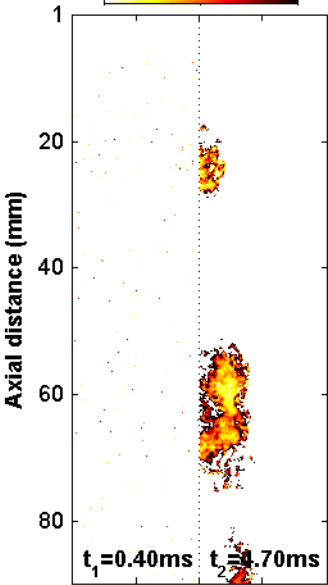




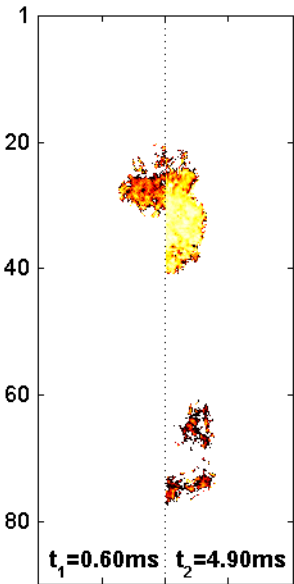




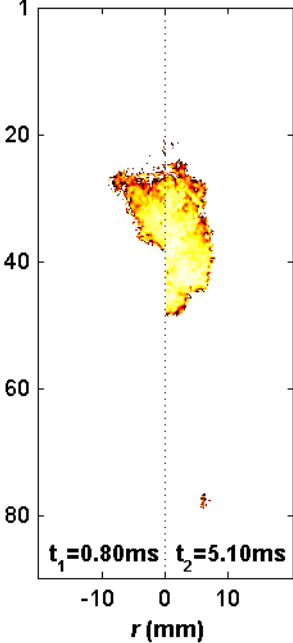
0 Soot KL 1.2



Axial distance (mm)



Axial distance (mm)



1800 Temp. 2600K



1

20

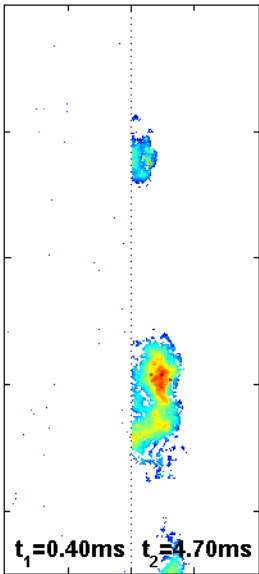
40

60

80

Axial distance (mm)

$t_1 = 0.40\text{ms}$ $t_2 = 4.70\text{ms}$

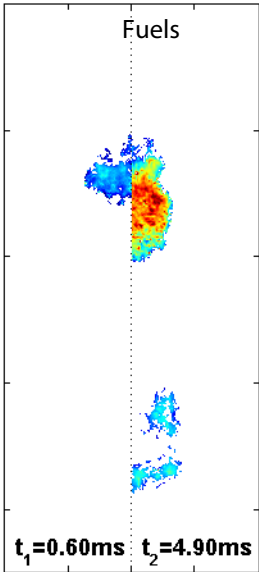


Axial distance (mm)

1
20
40
60
80

Fuels

$t_1 = 0.60\text{ms}$ $t_2 = 4.90\text{ms}$



1

20

40

60

80

10

0

-10

10

1

20

40

60

80

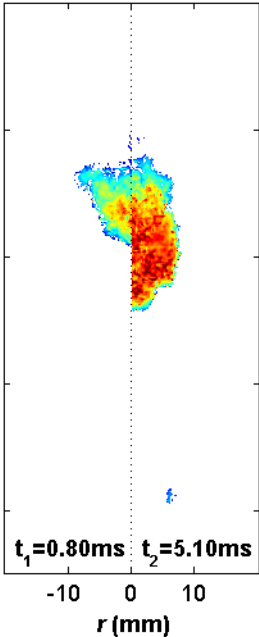
10

0

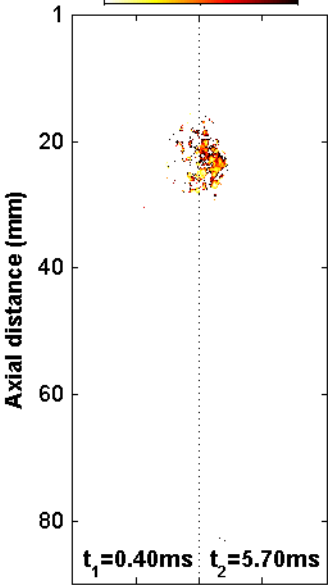
-10

10

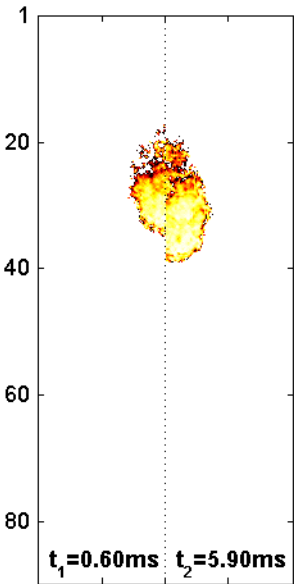
Axial distance (mm)



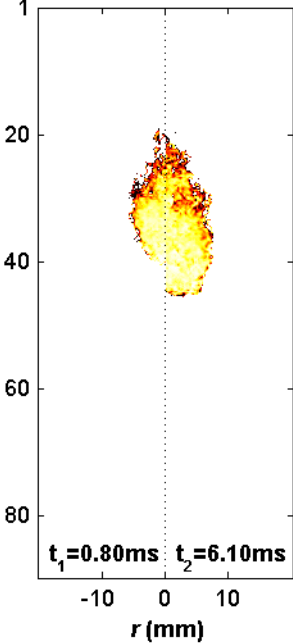
0 Soot KL 1.2



Axial distance (mm)



Axial distance (mm)



1800 Temp. 2600K



1

20

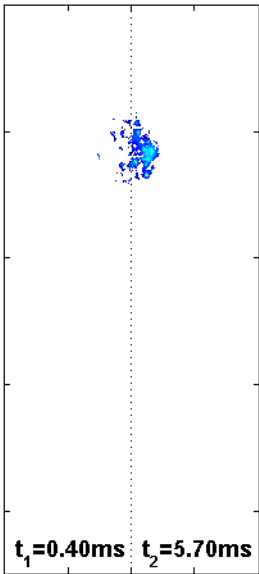
40

60

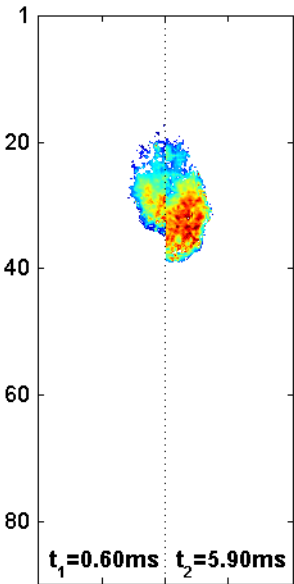
80

Axial distance (mm)

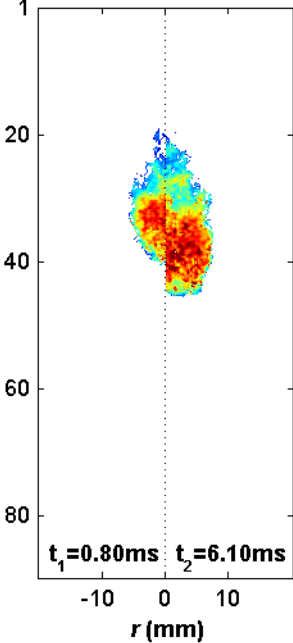
$t_1=0.40\text{ms}$ $t_2=5.70\text{ms}$



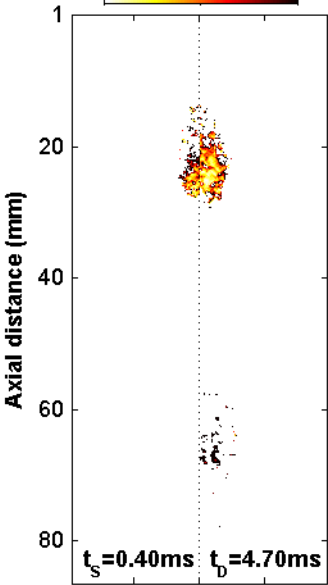
Axial distance (mm)



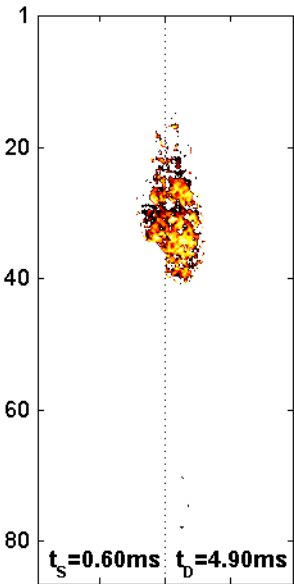
Axial distance (mm)



0 Soot KL 1.2



Axial distance (mm)



Axial distance (mm)

20

40

60

80

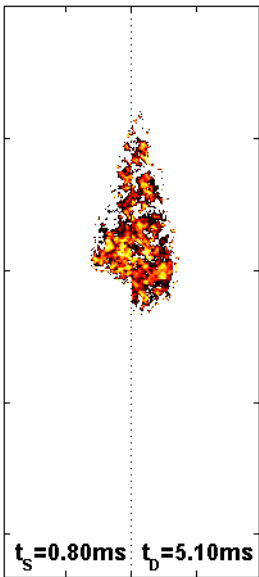
$t_s = 0.80\text{ms}$ $t_D = 5.10\text{ms}$

-10

0

10

r (mm)



1800 Temp. 2600K



1

20

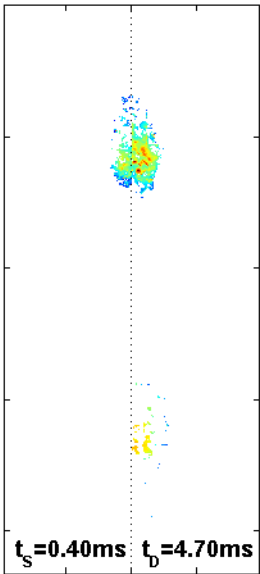
40

60

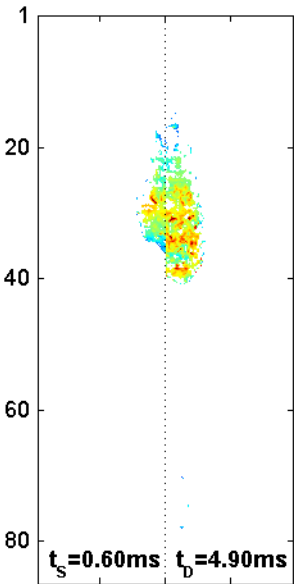
80

Axial distance (mm)

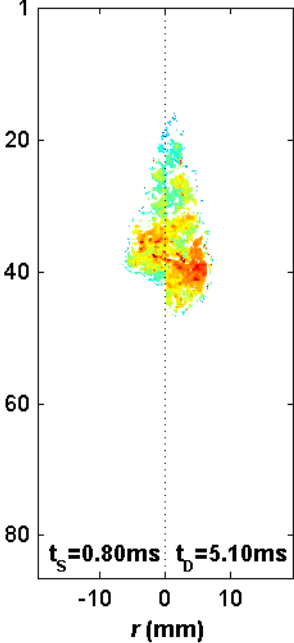
$t_s = 0.40\text{ms}$ $t_D = 4.70\text{ms}$



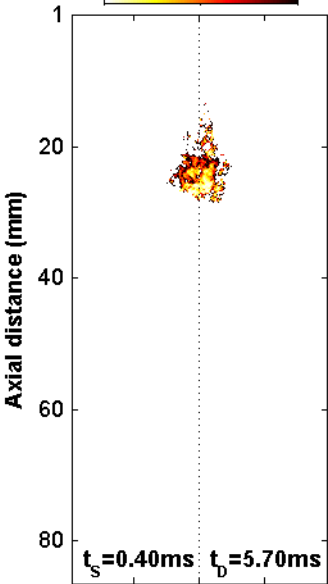
Axial distance (mm)



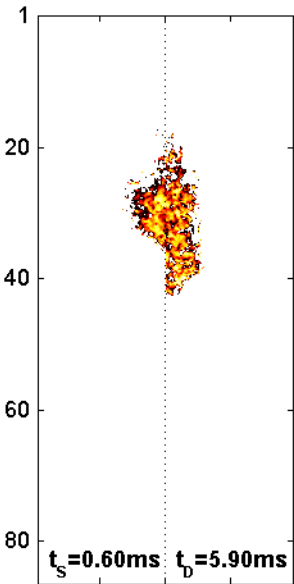
Axial distance (mm)



0 Soot KL 1.2



Axial distance (mm)



1

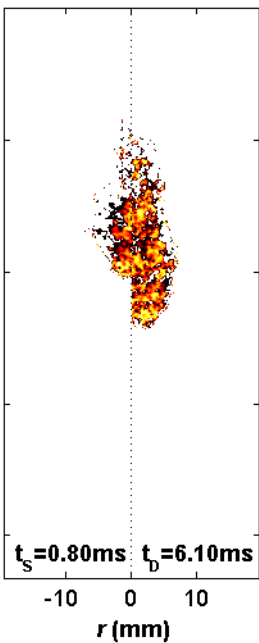
20

40

60

80

Axial distance (mm)



1800 Temp. 2600K



1

20

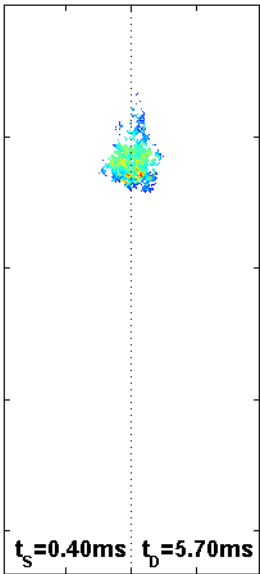
40

60

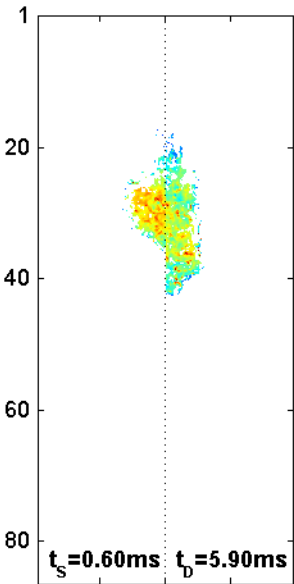
80

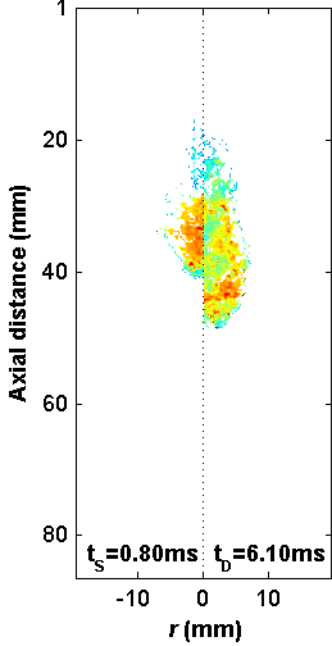
Axial distance (mm)

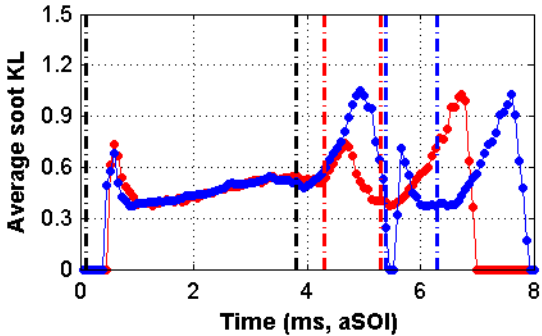
$t_s = 0.40\text{ms}$ $t_D = 5.70\text{ms}$

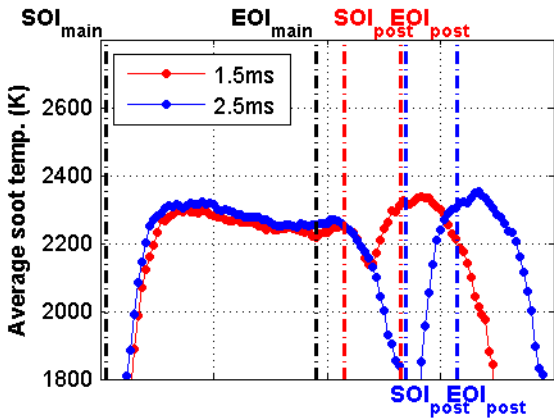


Axial distance (mm)









0 Probability 0.02

Soot Temperature (K)

2800

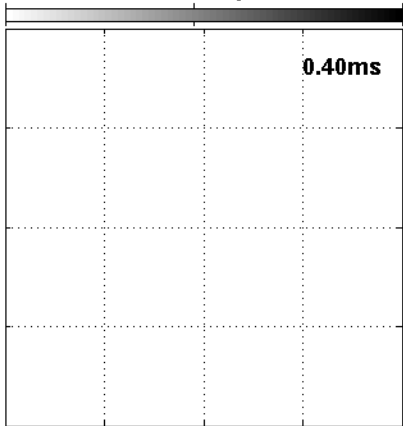
2400

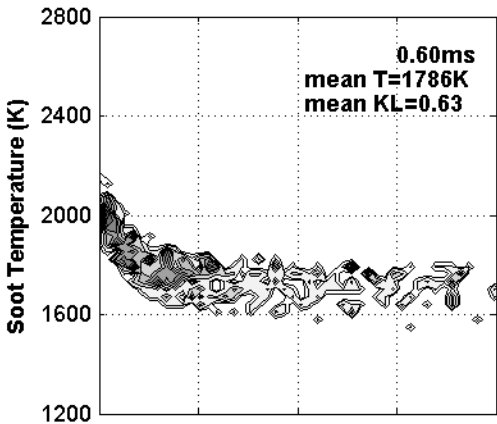
2000

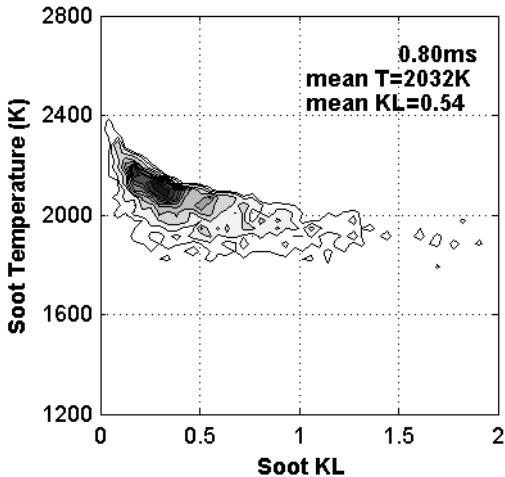
1600

1200

0.40ms



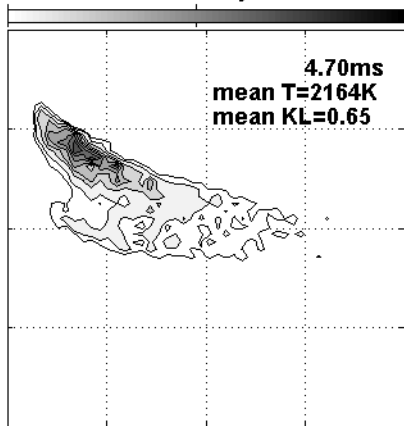




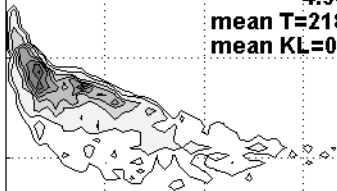
0

Probability

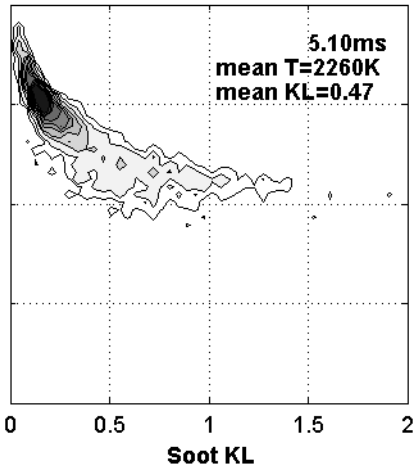
0.02



4.90ms
mean T=2188K
mean KL=0.52



ACS Paragon Plus Environment



0 Probability 0.02

Soot Temperature (K)

2800

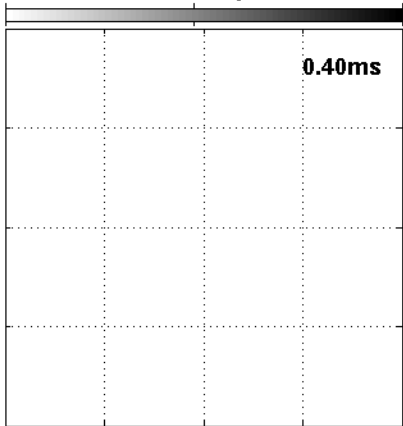
2400

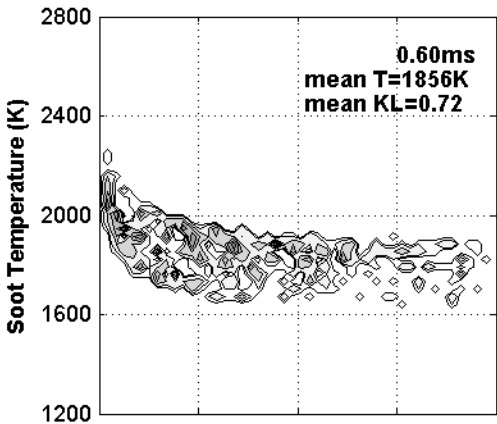
2000

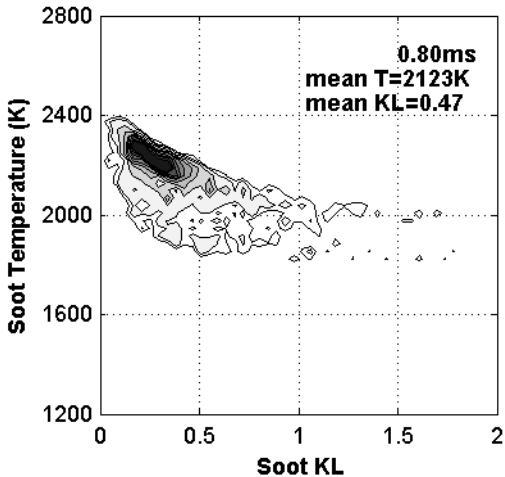
1600

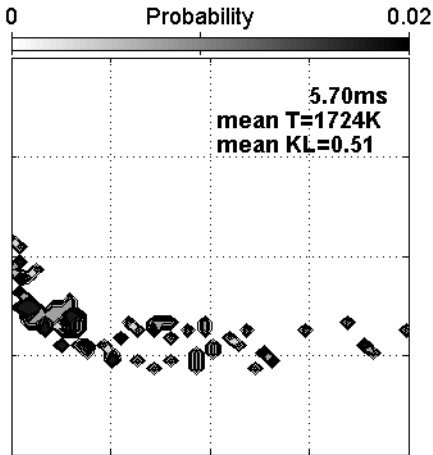
1200

0.40ms

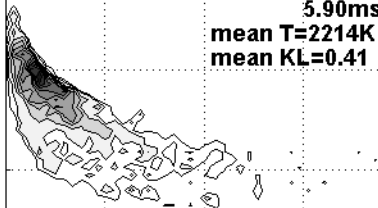


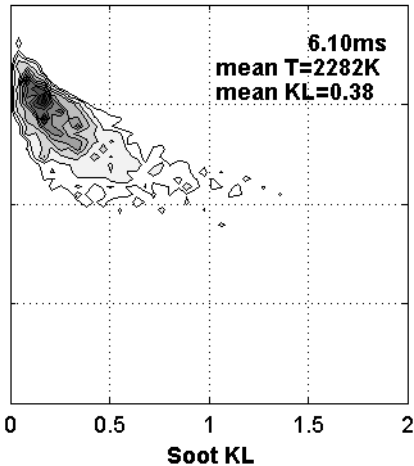


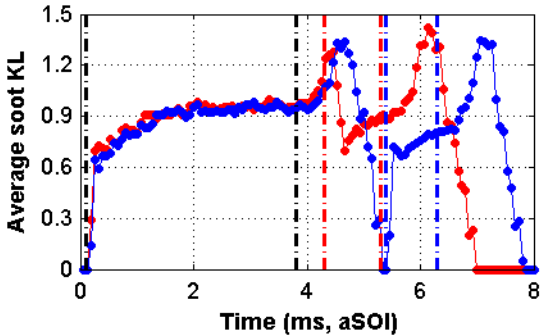


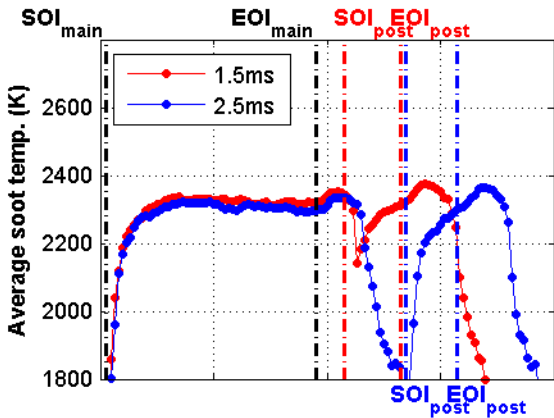


5.90ms
mean T=2214K
mean KL=0.41









0 Probability 0.02

Soot Temperature (K)

2800

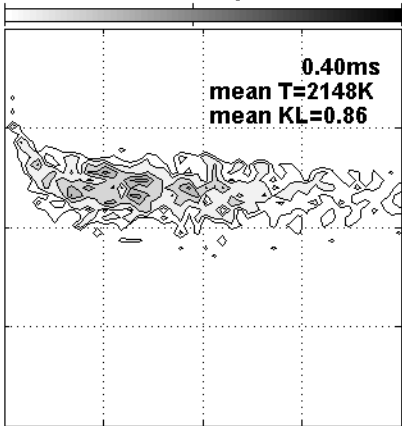
2400

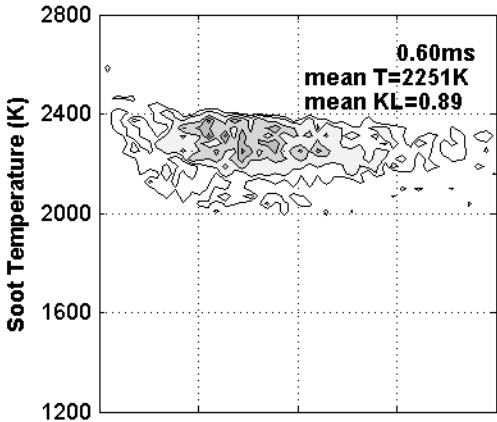
2000

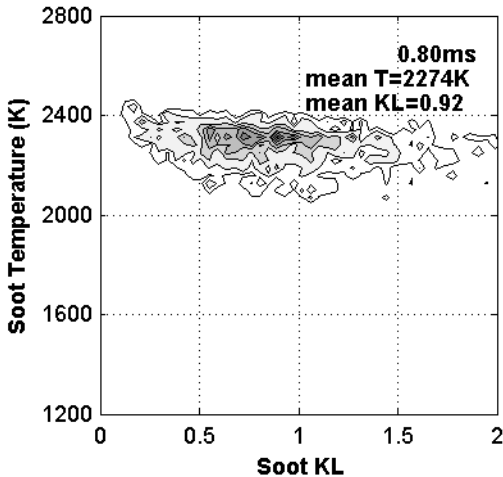
1600

1200

0.40ms
mean T=2148K
mean KL=0.86

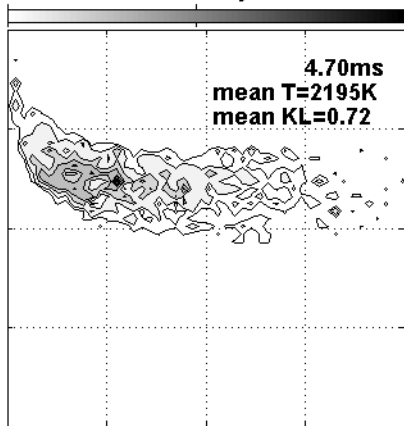






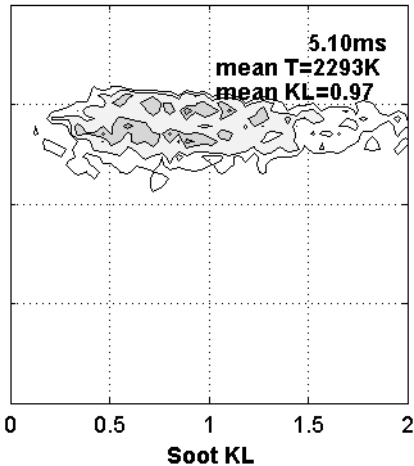
0 Probability

0.02

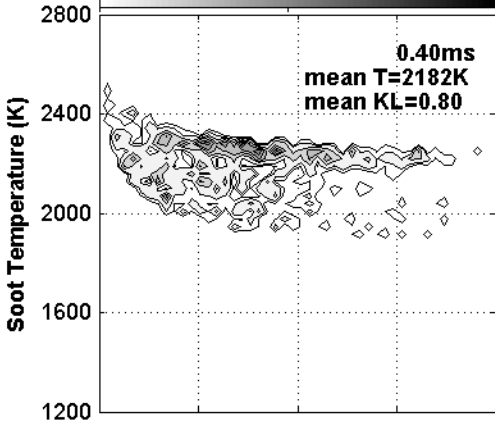


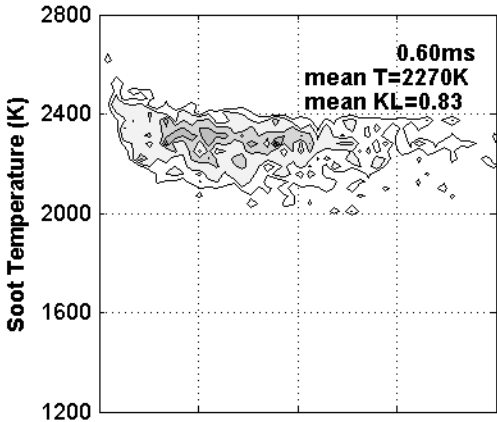
4.90ms
mean T=2284K
mean KL=0.94

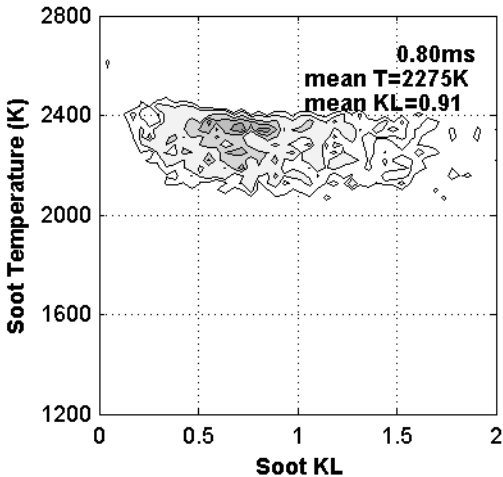




0 Probability 0.02

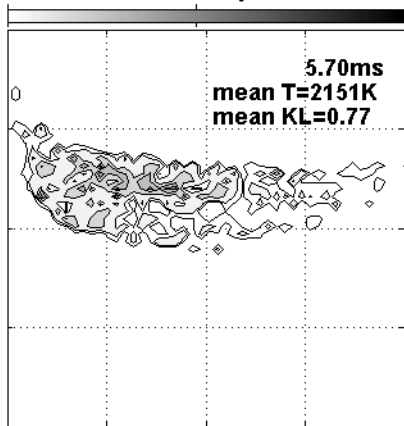






0 Probability

0.02



5.90ms
mean T=2254K
mean KL=0.86



