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Solar Energy, 2021; 225:60-82

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Final publication at: <http://dx.doi.org/10.1016/j.solener.2021.07.014>

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**18 September 2023**

<http://hdl.handle.net/2440/135511>

# A review of static and dynamic heliostat wind loads

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## Abstract

Accurate estimation of the static and dynamic wind loads on heliostats based on detailed measurement and characterisation of turbulence is crucial to avoid structural failure and reduce the cost of the structural heliostat components. Wind load predictions for heliostats are not specified in design standards for buildings because of a heliostat's non-standard shape and the variations of wind velocity and turbulence in the lowest 10 m of the atmospheric boundary layer (ABL). This paper reviews the static and dynamic wind loads on heliostats in the most unfavourable operating and stow positions, with a focus on the aerodynamic effects related to the heliostat structural component geometry, turbulence parameters in the ABL and field spacing. An increased resolution of field-scale wind measurements at heliostat field sites is recommended to fully characterise the ABL turbulence, as the high-intensity gusts over shorter durations at heights below 10 m lead to high-amplitude displacements with larger frequencies than observed in standard building structures. Increased understanding and development of aerodynamic wind load predictions for heliostats, based on their critical scaling parameters and local wind conditions, would increase the accuracy of annual field efficiency models through an improved resolution of operating load data and reduce the capital cost of structural components in power tower plants.

**Keywords:** heliostat; wind load; aerodynamics; atmospheric boundary layer; turbulence

## Nomenclature

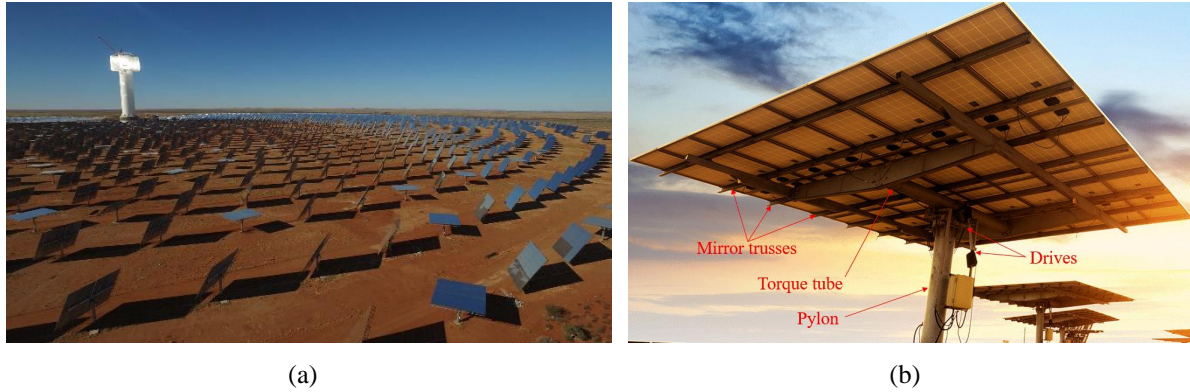
$A$	Surface area of heliostat panel ( $\text{m}^2$ )
$AR$	Aspect ratio (width/height) of heliostat panel = $b/c$
$\alpha_U$	Exponent of power law velocity profile
$\alpha$	Elevation angle of heliostat panel ( $^\circ$ )

29	$\beta$	Angle of attack of wind with respect to heliostat ( $^{\circ}$ )
30	$b$	Width of heliostat panel (m)
31	$c$	Chord length of heliostat panel (m)
32	$c_{Fi}$	Coefficient of force $F_i$ where $i = x, z$
33	$c_{Mi}$	Coefficient of moment $M_i$ where $i = Hy, y, z$
34	$\delta$	Atmospheric boundary layer depth (m)
35	$\delta_{ASL}$	Atmospheric surface layer depth (m)
36	$d_f$	Foundation pile depth (m)
37	$F_x$	Drag force on heliostat (N)
38	$F_z$	Lift force on heliostat (N)
39	$f$	Frequency (Hz)
40	$G_u$	Gust factor of wind velocity
41	$H$	Elevation axis height of heliostat (m)
42	$I_u$	Turbulence intensity of longitudinal velocity component
43	$I_w$	Turbulence intensity of vertical velocity component
44	$k$	Von Karman's constant
45	$l_{px}$	Distance to the centre of pressure from the heliostat elevation axis (m)
46	$L_u^x$	Integral length scale of longitudinal velocity component (m)
47	$L_w^x$	Integral length scale of vertical velocity component (m)
48	$M_{Hy}$	Hinge moment about elevation axis of heliostat (Nm)
49	$M_y$	Overturning moment about base of heliostat pedestal (Nm)
50	$M_z$	Azimuth moment about vertical axis of heliostat pedestal (Nm)
51	$\rho$	Density of air ( $\text{kg/m}^3$ )
52	$p$	Differential pressure between upper and lower surface (Pa)
53	$r$	Displacement (mm)
54	$S_{uu}$	Longitudinal velocity spectrum ( $\text{m}^2/\text{s}$ )
55	$S_{ww}$	Vertical velocity spectrum ( $\text{m}^2/\text{s}$ )
56	$\theta$	Mean potential temperature ( $^{\circ}\text{C}$ )
57	$U_H$	Mean velocity at elevation axis height of heliostat (m/s)
58	$U_{\infty}$	Freestream velocity in the ABL (m/s)
59	$u_{\tau}$	Friction velocity (m/s)
60	$x$	Longitudinal/streamwise direction (m)
61	$y$	Lateral/spanwise direction (m)
62	$z$	Height (m)
63	$z_0$	Logarithmic velocity profile surface roughness height (m)

## 64 1. Introduction

65 The application of concentrating solar thermal (CST) power tower technology is emerging as a  
66 means for industrial process heating and dispatchable renewable electricity production. Thermal energy

67 is collected by a receiver located at the top of a central tower where solar radiation is concentrated by a  
68 large field of heliostats through two-axis tracking of the sun. Cumulative installed capacity of power  
69 tower plants increased by five times to approximately 6.3 GW and their levelised cost of electricity  
70 (LCOE) decreased by 47% to USD \$0.182/kWh between 2010 and 2019 (IRENA 2020). During this  
71 time, the capacity factor of deployed commercial-scale power tower plants increased from 30% to 45%  
72 through increased power cycle efficiencies operating at high temperatures (Mehos *et al.* 2017) and  
73 increased energy storage capacity from 5 hours to 7.7 hours at sites with larger direct solar resources  
74 (IRENA 2020). According to projections by IRENA, the LCOE will further decrease to USD \$0.07-  
75 0.08/kWh for power tower plants commissioned in 2021. One promising opportunity to achieve a  
76 reduction in the LCOE is by reducing the heliostat field cost, which contributes approximately 40-50%  
77 of the total plant cost (Kolb *et al.* 2011; Pfahl *et al.* 2017a). Currently the total cost of industrial scale  
78 heliostats is estimated as USD \$140/m<sup>2</sup> by National Renewable Energy Laboratory (NREL) (Turchi *et*  
79 *al.* 2019), with the 2030 DOE target set at USD \$50/m<sup>2</sup> (Department of Energy 2017). The most typical  
80 heliostat design in the current commercial CST plants, such as the 50 MW Khi Solar One heliostat field  
81 in Figure 1(a), consists of glass mirror facets supported by steel beams and trusses and a T-shaped  
82 pedestal and torque tube with azimuth and elevation drives for tracking (Télliez *et al.* 2014). Techno-  
83 economic analysis by Emes *et al.* (2020a) found that the steel support structure components (Figure 1b)  
84 increased their contribution from 18% to 34% of the total heliostat cost due to increased wind loads  
85 with increasing heliostat size from 25 m<sup>2</sup> to 150 m<sup>2</sup>. Furthermore, the total heliostat cost was reduced  
86 by 40% and the optimal heliostat size increased from 25 m<sup>2</sup> to 50 m<sup>2</sup> by lowering the stow design wind  
87 speed from 20 m/s to 10 m/s (Emes *et al.* 2015). To achieve the cost reduction targets, innovative  
88 designs of the heliostat structural components must be developed to reduce their manufacturing and  
89 installation cost (Pfahl 2014a; Pfahl *et al.* 2017a). This requires a detailed understanding of the flow  
90 field aerodynamics for a reliable estimation of the wind loads on heliostats.



91 Figure 1. Photographs of (a) the 50 MW Khi Solar One heliostat field (Abengoa Solar 2016), and (b) structural  
 92 heliostat components of the Abengoa Solar heliostat, adapted from Advisian Worley Group (2021).

93 Heliostats are exposed to atmospheric wind that imposes unsteady loads on the drives, torque tube,  
 94 pylon, foundation and mirror trusses. Overestimation of the design wind loads increases the capital cost  
 95 of a solar plant. The wind-bearing heliostat components are designed for a serviceability condition with  
 96 stiffness to minimise local deformations of the mirror surface during operation at different elevation  
 97 angles ( $\alpha > 0^\circ$ ), and a survivability condition with strength against the maximum loads during high-  
 98 wind events (e.g. gust front, storm) when the heliostat surface is aligned horizontally ( $\alpha = 0^\circ$ ) in the  
 99 stow position. The aerodynamics of these two conditions vary significantly: operating heliostats are  
 100 characterised by bluff body features including maximum drag forces with increasing surface area with  
 101 respect to the approaching wind and vortex shedding from the sharp edges of rectangular heliostat  
 102 mirrors. Stowed heliostats are characterised by slender streamlined body features including maximum  
 103 lift forces in a highly turbulent flow generated by upstream roughness in the atmospheric boundary  
 104 layer (ABL). Furthermore, the dynamic wind loads induced by coupling between the temporal  
 105 variations of the wind loads and the dynamic properties of the heliostat structure, lead to oscillations of  
 106 the heliostat surface that impacts the tracking (mirror orientation) accuracy and optical performance of  
 107 the heliostat field.

108 Evaluation of the maximum wind loads at the appropriate temporal resolution is essential for the  
 109 cost-effective design of heliostats, since a wide range of sizes and structural designs is currently  
 110 deployed in the CST industry. Historically, design wind loads on industrial-scale heliostats incorporated  
 111 aerodynamic coefficients using scaled models of the heliostats in boundary layer wind tunnel  
 112 experiments. The non-dimensional aerodynamic coefficients for the drag and lift forces on the heliostat

113 surface, and the bending moments about the elevation axis, vertical axis and base of the pylon, were  
114 applied following benchmark wind tunnel studies by Peterka *et al.* on isolated heliostats. Peterka and  
115 Derickson (1992) measured the mean and peak wind load coefficients in a simulated ABL with a  
116 turbulence intensity  $I_u = \sigma_u/\bar{U}_H = 18\%$ , denoted as the root-mean-square of the longitudinal velocity  
117 component to the mean wind speed at the elevation axis height  $H$  of a square-facet heliostat model ( $c =$   
118  $0.27$  m,  $H = 0.13$  m). The forces and moments were calculated using high-frequency base force balance  
119 measurements on the heliostat model (Peterka *et al.* 1988; Peterka *et al.* 1989). The maximum  
120 aerodynamic load coefficients on a scaled model heliostat (Peterka *et al.* 1988; Peterka *et al.* 1989;  
121 Peterka and Derickson 1992) were reported in the simulated ABL representing an open country terrain  
122 ( $z_0 = 0.03$  m) with  $I_u = 18\%$  and  $G_u = 1.6$  at the heliostat elevation axis height. It has been widely  
123 acknowledged that the aerodynamic coefficients in this benchmark study were reported for a single  
124 case, whereas the mean wind speed and turbulence intensity profiles of the ABL approaching the  
125 heliostat vary significantly with height and surface roughness. The unsteady pressure distribution on  
126 the mirror panel due to turbulence in the wind imposes highly fluctuating moments, which can create  
127 maximum loads on the heliostat pedestal, foundation and drives. Assessment of the dynamic response  
128 of the heliostats under unsteady wind loads is necessary for preventing structural failure due to  
129 resonance and buffeting (Pfahl *et al.* 2017a), which may result from the convergence of the dominant  
130 frequency of the wind fluctuations to the natural frequency of heliostat structures in the typical range  
131 of 1.6–3 Hz (Griffith *et al.*, 2011; Gong *et al.*, 2012; Vásquez-Arango *et al.*, 2015). Deformations and  
132 displacements of the heliostat structural elements caused by unsteady pressure distributions and  
133 dynamic amplification of peak wind loads impacts the ability of heliostats to withstand strong wind  
134 gusts in the stow position at high wind speeds (Emes *et al.* 2017; Vasquez Arango *et al.* 2017; Emes *et*  
135 *al.* 2018; Pfahl 2018; Jafari *et al.* 2019a). Numerical methods, such as Large Eddy Simulation (LES),  
136 are generally associated with large computational effort and uncertainties to model the fluctuating wind  
137 loads due to ABL turbulence and the transient response characteristics of heliostat structures. RANS  
138 methods would be less extensive but are not suitable to simulate the upstream turbulence structures.  
139 Hence, experimental data through wind tunnel and field measurements of the ABL turbulence

140 characteristics are usually obtained in the design of a heliostat field, for the assessment of operational  
141 performance models and feasibility analyses of power tower systems.

142 Heliostats in operating positions act as bluff bodies within the ABL, where the interaction of their  
143 wakes with the incoming highly turbulent flow results in the aerodynamics of multiple heliostats  
144 varying significantly from a single body. The vortices shed by an upstream heliostat or the tower can  
145 create vibrations and unsteady loads, due to the fluctuating turbulence component of wind velocity, on  
146 the downstream in-field heliostats positioned in the intermediate wake. Due to a blocking effect caused  
147 by upstream heliostats, wind tunnel measurements on an array of heliostats in multiple rows reveal that  
148 reducing the distance between heliostats decreases the time-averaged loads on the heliostats in the inner  
149 rows (Peterka *et al.* 1986). Peterka *et al.* (1987) In comparison to a heliostat in the first row, the mean  
150 drag force and hinge moment coefficients on an instrumented heliostat in the fourth row of a four-row  
151 array with low and high field densities were decreased by 10% to 50%. In comparison to a heliostat in  
152 the first row, the peak drag force on the heliostat in the fourth row increased by 40% (Peterka *et al.*  
153 1987). Hence, the distance between heliostat rows and the layout of heliostat rows in a field impact the  
154 mean and peak wind loads on heliostats differently throughout a field.

155 This paper presents a review of the literature on the wind loads and aerodynamics of heliostats, with  
156 the aim to highlight the key parameters that impact the accuracy of wind load predictions in the design  
157 and development of industrial-scale azimuth-elevation heliostats. A solid understanding of the wind  
158 loads is a major driver to reduce the structural cost of the heliostat field, without compromising the field  
159 efficiency and power tower plant performance. Section 2 discusses the temporal and spatial distributions  
160 of turbulence, including the state-of-the-art experimental modelling techniques for simulation of the  
161 ABL in a wind tunnel and the similarity requirements for heliostat wind load measurements over the  
162 range of surface roughness at different field sites. Section 3 describes the conventional coordinate  
163 system of an azimuth-elevation heliostat and discusses the effect of the geometry of a heliostat  
164 concentrator and its supporting structure components on the wind loads. Field experiment investigations  
165 focusing on the dynamic wind load effects on heliostat vibration and tracking error due to the  
166 distribution of surface pressures and wind-induced oscillations are outlined in Section 4, followed by a  
167 discussion of the wind loads in a heliostat array representing a section of field and the flow around

168 multiple heliostats in Section 5. The key aspects of the literature that are critical to the development of  
169 wind load design guidelines for heliostats and future research opportunities for wind load reduction are  
170 discussed in Section 6.

## 171 **2. Atmospheric boundary layer modelling**

172 The atmospheric boundary layer (ABL) is the lowest 1-2 km of the troposphere, where the  
173 mechanical properties of the wind are directly influenced by the Earth's surface (Stull 1988). The lower  
174 100 m of the ABL, where heliostats and other physical structures including buildings and bridges are  
175 positioned, is known as the atmospheric surface layer (ASL). Surface friction and vertical temperature  
176 gradient are two important parameters that influence the wind structure in the ASL (Kaimal and  
177 Finnigan 1994). Turbulence in the ASL during near-neutral stability conditions relevant to heliostat  
178 design wind speeds is mechanically generated by shear from the terrain surface roughness, with a  
179 negligible impact of the mean potential temperature gradient  $\partial\theta/\partial z = 0$  and the net vertical heat flux  
180  $\overline{w'\theta'} = 0$  (Stull 2005). The wind velocity profile in a neutral boundary layer is conventionally modelled  
181 as a logarithmic profile in wind engineering applications, such as the ultimate design wind loads on  
182 heliostats at high wind speeds during storms and gust fronts.

### 183 *2.1. Effect of surface roughness on wind speed and turbulence profiles*

184 The aerodynamic surface roughness determines the velocity and turbulence characteristics over a  
185 terrain, based on the height and surface roughness (Simiu and Scanlan 1996). Wind speed is commonly  
186 decomposed into a time-averaged mean component and a fluctuating turbulent component. The mean  
187 velocity profile in the ABL has been modelled to various degrees of accuracy by the logarithmic law  
188 and power law (Kaimal and Finnigan 1994; Xu 2013), respectively:

$$189 \quad U(z) = \frac{u_\tau}{\kappa} \ln\left(\frac{z}{z_0}\right), \quad (1)$$

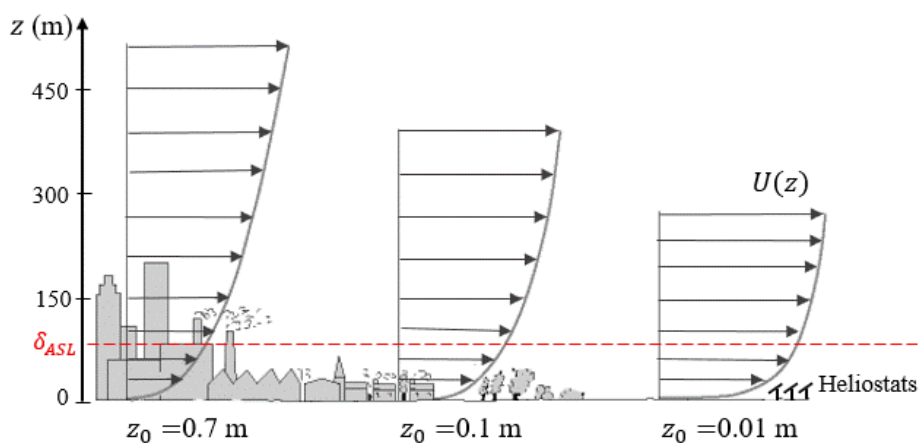
$$190 \quad U(z) = U_\infty \left(\frac{z}{\delta}\right)^{\alpha_U}, \quad (2)$$

191 where  $U_\infty$  (m/s) is the freestream wind speed,  $\delta$  (m) is the boundary layer depth,  $u_\tau$  is the friction  
192 velocity,  $\kappa$  is von Karman's constant equal to 0.4,  $z_0$  is the aerodynamic surface roughness height, and



193  $\alpha_U$  is the power law exponent that characterises the level of surface roughness. The depth  $\delta$  of the  
 194 neutrally stratified ABL can vary between a few hundred metres to several kilometres, depending on  
 195 the surface roughness of the terrain (Xu 2013). Typical values of  $z_0$  for different terrains are shown in  
 196 Figure 2, varying in scale from millimetres in a very flat terrain (e.g. desert) to metres in an urban  
 197 terrain. The zero-plane displacement is negligible for small surface roughness lengths, such as flat and  
 198 open-country terrains (Cook 1985), where heliostats are usually located. With increased surface  
 199 roughness and at lower heights in the ASL, the gradient of the velocity profile increases. . Hence, more  
 200 gusty wind conditions occur due to the increasing fluctuating wind speed component due to turbulence  
 201 close to the surface.

202 The power law has been shown to be suitable for modelling the mean velocity profile at heights  
 203 around 30-300 m, and thus it is most widely used for study of wind loads on tall buildings and other  
 204 large civil structures (Xu 2013). Initially derived from the turbulent boundary layer on a flat plate, the  
 205 logarithmic law has been demonstrated to be most suitable for modelling the mean velocity profile at  
 206 heights below 100 m, representing the average depth  $\delta_{ASL}$  of the atmospheric surface layer (ASL) (Cook  
 207 1997; Li *et al.* 2010; Sun *et al.* 2014). The logarithmic law provides an accurate velocity profile  
 208 independent of atmospheric stability for heights below 10 m very close to the ground (Kaimal and  
 209 Finnigan 1994), and is therefore appropriate for modelling the mean velocity profile for study of wind  
 210 loads on heliostats.



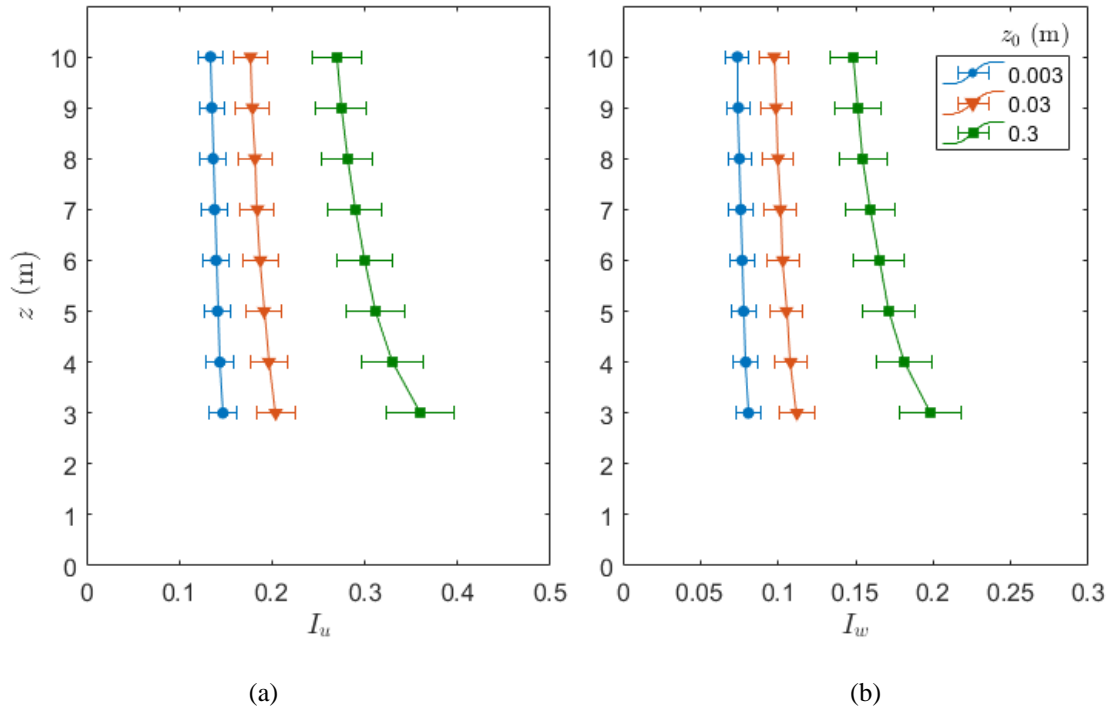
211

212 Figure 2. Effect of surface roughness on wind velocity profiles in the atmospheric boundary layer. Adapted from  
 213 Gilooly and Taylor-Power (2016).

214 Statistical parameters of turbulence in the ABL are typically used to determine the wind velocity  
215 fluctuations. Turbulence intensity is representative of the amplitude of velocity fluctuations compared  
216 to the mean velocity, defined as:

$$217 \quad I_i = \frac{\sigma_i}{U} , \quad (3)$$

218 where  $\sigma_i$  is the standard deviation of the velocity component  $i = u, v, w$  in the longitudinal, lateral, and  
219 vertical directions, respectively. Turbulence in the lowest 10 m of the ASL is anisotropic and the  
220 intensity of the turbulent fluctuations is the largest in the streamwise direction. Figure 3 shows the  
221 dependence of the longitudinal ( $I_u$ ) and vertical ( $I_w$ ) turbulence intensity on the height  $z$  from the  
222 ground, and the aerodynamic surface roughness height  $z_0$  defined in the logarithmic velocity profile in  
223 equation 1. The profiles of turbulence intensity are generated from semi-empirical data in ESDU 85020  
224 (2001) for  $U = 20$  m/s at  $z = 10$  m, with an estimated uncertainty of  $\pm 10\%$  within the full-scale ABL  
225 with uniform terrain roughness for an upwind fetch distance of 30 km. The level of surface roughness  
226 impacts the magnitude and gradient of  $I_u$ , where the intermediate “open country” terrain ( $z_0 \approx 0.01$ -  
227 0.05 m) is commonly defined in wind engineering study of buildings and heliostats. For instance, in  
228 Figure 3(a) at  $z = 6$  m that approximates the hinge height of a 120 m<sup>2</sup> heliostat,  $I_u$  increases from 0.14  
229 in a very flat terrain ( $z_0 = 0.003$  m) to 0.3 in a suburban terrain ( $z_0 = 0.3$  m). According to the empirical  
230 relationships in ESDU 85020 (2001) derived from atmospheric data,  $\sigma_v/\sigma_u$  and  $\sigma_w/\sigma_u$  in the ASL are  
231 approximately equal to 0.78 and 0.55 at lower heights where  $z \ll \delta$ . The average depth  $\delta$  of the  
232 atmospheric boundary layer during neutral stability conditions is typically between 450 m and 600 m,  
233 depending on the terrain roughness (Counihan 1975; Xu 2013). Hence, the vertical turbulence  
234 intensities in Figure 3(b) follow a similar trend and are approximately half the magnitude of the  
235 longitudinal turbulence intensities.

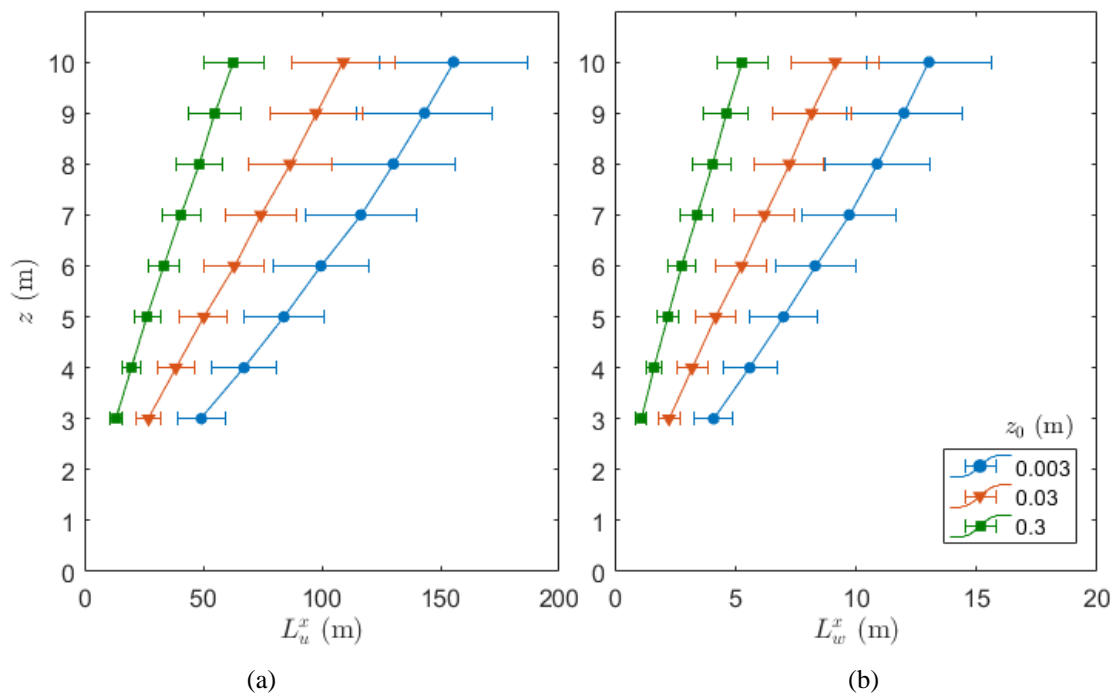


236

237 Figure 3. (a) Longitudinal  $I_u$ , and (b) vertical  $I_w$  turbulence intensity profiles in the lower 10 m of ABL for  
 238 different values of surface roughness height  $z_0$  (ESDU 85020 2001). Error bars indicate  $\pm 10\%$  uncertainty of  
 239 turbulence intensity for equilibrium conditions in the neutral ASL with  $U = 20$  m/s.

240 Turbulence in the atmospheric flow is dependent on the features of the terrain and varies based on  
 241 the site of different heliostat fields. With increasing height from the ground, turbulence intensity  
 242 decreases in Figure 3 while the integral length scale of turbulence increases in Figure 4 (ESDU 85020  
 243 2001). The integral length scale of turbulence represents the average size of the energy-containing  
 244 eddies within a turbulent boundary layer. Therefore, based on the height of the heliostats from the  
 245 ground and the terrain surrounding the heliostat field, the turbulence intensities and length scales show  
 246 a very large variation in the lowest 10 m of the ASL. Commercial-scale heliostats are manufactured  
 247 with hinge heights in a typical range between 3 m and 6 m. ESDU 85020 (2001) predicts the  
 248 longitudinal integral length scale  $L_u^x$  in Figure 4(a) to range from 27 m to 63 m in an open country  
 249 terrain ( $z_0 = 0.03$  m) and from 50 m to 100 m in a very flat terrain ( $z_0 = 0.003$  m) with increasing  $z$   
 250 from 3 m to 6 m. The average longitudinal extent of the energetic eddies is therefore typically the same  
 251 order as the chord length of the heliostat and up to an order of magnitude larger. Eddies that are similar  
 252 in size to the heliostat panel characteristic length are presumably responsible for the peak wind loads  
 253 on heliostats in stow position, as turbulence length scales that are comparable with the length scale of  
 254 the structure create a well correlated pressure distribution on the structure (Mendis *et al.* 2007). This is

255 because smaller eddies do not cause high net pressures that are correlated over the heliostat surface,  
 256 whereas considerably larger eddies have significantly lower vertical velocity fluctuations at the  
 257 elevation axis height of the heliostat (Pfahl *et al.* 2015). Furthermore, the vertical component of the  
 258 fluctuating velocity, defined by the vertical integral length scales  $L_w^x$  in Figure 4(b), increases from  
 259 2.2 m to 5.3 m in an open country terrain ( $z_0 = 0.03$  m) and from 4.1 m to 8.3 m in a very flat terrain  
 260 ( $z_0 = 0.003$  m) with increasing hinge height from 3 m to 6 m. The integral length scales of the vertical  
 261 velocity component are similar in magnitude to the heliostat chord length, which impacts the surface  
 262 pressure distribution and the maximum hinge moment on a heliostat in stow position. The interaction  
 263 of the energetic eddies with similar sizes to the heliostat (i.e.  $L_w^x/c \approx 1$ ) are therefore speculated to be  
 264 responsible for dynamic effects observed in the field, such as aeroelastic flutter and fatigue loads on  
 265 heliostats.



266

267 Figure 4. (a) Longitudinal and (b) vertical integral length scales of turbulence as a function of height  $z$  and  
 268 surface roughness height  $z_0$  (ESDU 85020 2001). Error bars indicate  $\pm 20\%$  uncertainty of integral length scales  
 269 for equilibrium conditions in the neutral ASL with  $U = 20$  m/s.

## 270 2.2. Scaling of heliostat models and turbulence spectra

271 The mismatch of scaling ratios, between the ABL thickness and chord length of the heliostat, is an  
 272 important consideration in wind tunnel modelling of heliostats due to their small dimensions compared

273 to the ABL. It is possible to model heliostats with the same scaling ratio as the ABL, due to the due to  
 274 technological constraints in modelling the structural details and measurement of the pressure and forces  
 275 on a heliostat model. Therefore, heliostats are usually modelled using higher scaling ratios. between  
 276 1:10 to 1:50. This results in violated similarity of the Reynolds number and the turbulence spectra  
 277 between wind tunnel experiments and the full-scale condition. The impact of Reynolds number  
 278 similarity can be overcome on sharp-edged models at Reynolds numbers above 50,000 (Tieleman  
 279 2003). This has been demonstrated by the independence of aerodynamic coefficients of heliostats with  
 280 Reynolds number at freestream velocities between 5 m/s and 35 m/s (Pfahl and Uhlemann 2011b).  
 281 However, the turbulence fluctuations and their spectral distribution with the wide range of frequencies  
 282 in the ABL affect the wind loads significantly (Jafari *et al.* 2019b).

283 Figure 5 schematically presents the range of dimensions of a model heliostat in three sets of wind  
 284 tunnel experiments studies (Peterka *et al.* 1989; Pfahl *et al.* 2011a; Emes *et al.* 2017) and compares the  
 285 geometric scaling of a full-scale heliostat and ABL with their respective models in a wind tunnel. These  
 286 studies measured wind loads, expressed as aerodynamic coefficients of drag,  $c_{Fx}$ , and lift,  $c_{Fz}$ , forces,  
 287 and the moments induced at the hinge,  $c_{MHy}$ , the foundation,  $c_{My}$  and the vertical azimuth axis,  $c_{Mz}$ , as  
 288 shown in Figure 5(b) on heliostat models in stow position and inclined at different elevation angles ( $\alpha$ )  
 289 in operating positions:

$$290 \quad c_{Fx} = \frac{F_x}{1/2\rho U_H^2 A}, \quad (4)$$

$$291 \quad c_{Fz} = \frac{F_z}{1/2\rho U_H^2 A}, \quad (5)$$

$$292 \quad c_{MHy} = \frac{M_{Hy}}{1/2\rho U_H^2 A c}, \quad (6)$$

$$293 \quad c_{My} = \frac{M_y}{1/2\rho U_H^2 A H}, \quad (7)$$

$$294 \quad c_{Mz} = \frac{M_z}{1/2\rho U_H^2 A c}, \quad (8)$$

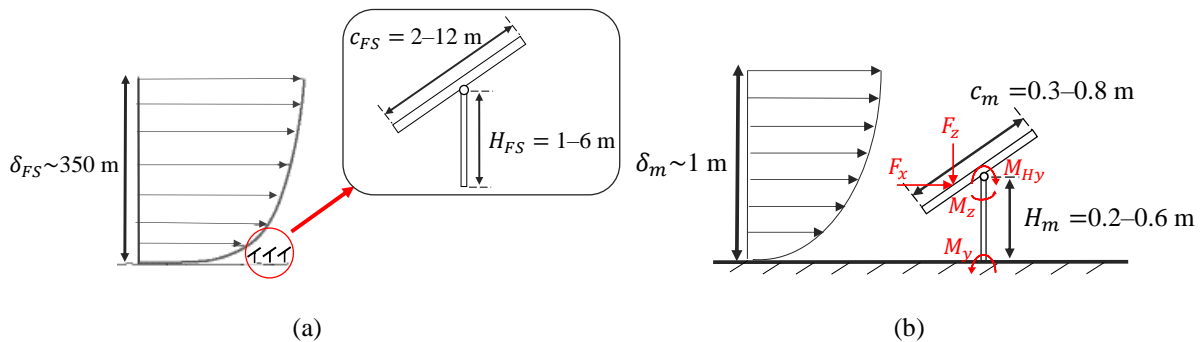
295 where  $c$  is the heliostat chord length in the longitudinal (windward) direction,  $H$  is the elevation axis  
 296 (hinge) height, and  $U_H$  is the time-averaged wind speed at the height of heliostat elevation axis.

297 Standard practice in scale-model simulations determines the geometric scaling ratio of a heliostat  
 298 model considering the effects of both terrain and height, and the spectrum of the simulated boundary

299 layer in a wind tunnel (Cook 1978). Heliostat models were positioned in a simulated boundary layer  
300 with the mean velocity profile and turbulence intensity matched to the ABL in an open-country terrain  
301 in wind tunnel tests. Peterka *et al.* (1989) tested a heliostat model at a scale of 1:40 in the Meteorological  
302 Wind Tunnel of the Fluid Dynamics and Diffusion Laboratory at Colorado State University. The  
303 boundary layer thickness in their wind tunnel simulation was about 1 m, which compared to the average  
304 ABL thickness in open terrains suggests a scaling factor of 1:350 for the ABL. The same scaling  
305 challenge was evident for the German Aerospace Center (DLR) experiments by Pfahl *et al.* (2011a),  
306 where the heliostat model was at a 1:20 scale. A similar heliostat model scaling ratio, which was  
307 considerably larger than the ABL scaling ratio of approximately 1:100, was used in the University of  
308 Adelaide large-scale wind tunnel by Emes *et al.* (2019a). The difference in scaling ratios is speculated  
309 to have led to variations in the reported wind load coefficients for the maximum operational and stow  
310 heliostat configurations at different elevation angles ( $\alpha$ ) with respect to the horizontal in Table 1. This  
311 raises uncertainty of the accuracy of the wind load measurements. The similarity of wind tunnel  
312 experiment simulations for the evaluation of heliostat wind loads can be verified by an instrumented  
313 full-scale heliostat prototype at a field site, however such data has been scarcely reported in the literature  
314 (Jafari *et al.* 2019b).

315 Table 1. Comparison of peak operational and stow wind load coefficients reported in the literature.

Wind tunnel experiment	Operation				Stow $\alpha=0^\circ$				$I_u$ (%)
	$\alpha=90^\circ$ $c_{Fx}$	$\alpha=30^\circ$ $c_{Fx}$	$\alpha=90^\circ$ $c_{My}$	$\alpha=30^\circ$ $c_{MHy}$	$c_{Fx}$	$c_{Fz}$	$c_{My}$	$c_{MHy}$	
Peterka <i>et al.</i> (1989)	4	2.8	4.35	0.6	0.9	0.6	1	0.2	18
Pfahl <i>et al.</i> (2011a), Pfahl <i>et al.</i> (2015)	3.3	2.1	3.2	0.55	0.43	0.38	0.53	0.18	18
Emes <i>et al.</i> (2019a)	2.25	1.89	2.29	0.21	0.39	0.49	0.43	0.13	13



316 Figure 5. A schematic showing the dimensions of: (a) a full-scale heliostat placed in ABL, (b) a model heliostat  
317 in a wind tunnel boundary layer, and the forces and moments on the heliostat model. The dimensions of the

318 model heliostat are based on the studies in the literature (Peterka *et al.* 1989; Pfahl *et al.* 2011a; Emes *et al.*  
 319 2017). The boundary layer thickness is  $\delta$ ,  $c$  defines the chord length of the heliostat mirror panel and  $H$  is the  
 320 heliostat hinge height. The subscripts  $FS$  and  $m$  represent full scale and model scale, respectively.

321 The power spectral density function of the wind speed provides critical information about the scales  
 322 of energy-containing turbulent eddies, which is necessary for evaluation of unsteady wind loads on  
 323 structures. The non-dimensional power spectral density of the velocity fluctuations compares the  
 324 distribution of turbulence energy in the wind tunnel boundary layer with that predicted by ESDU 85020  
 325 (2001) in the ASL through a modified form of the von Kármán (1948) model:

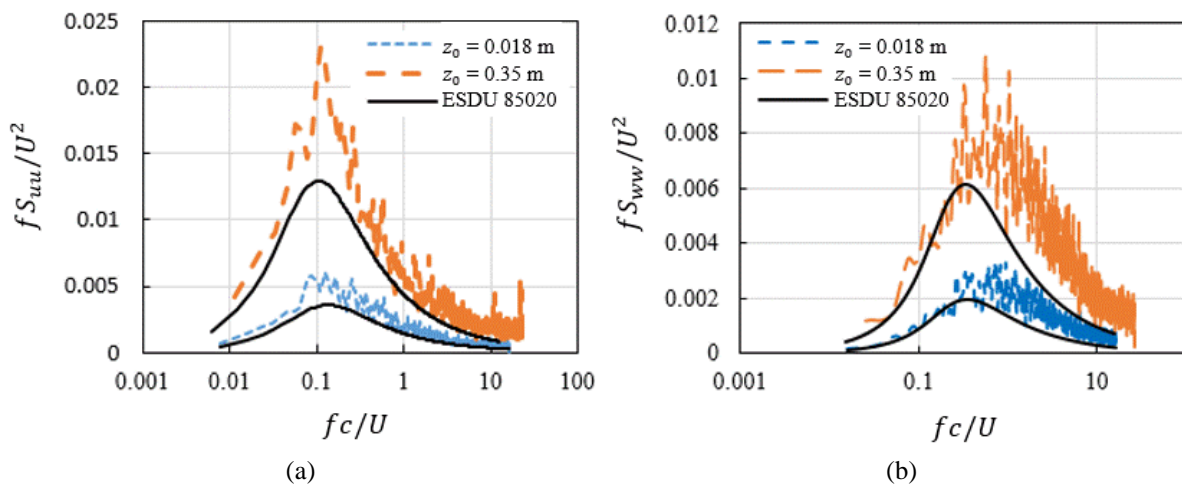
$$\frac{fS_{uu}}{\sigma_u^2} = \frac{4n_u}{(1 + 70.8n_u^2)^{5/6}} \quad (1)$$

$$\frac{fS_{ww}}{\sigma_w^2} = \frac{n_w(1 + 755.2 n_w^2)}{(1 + 283.2 n_w^2)^{11/6}} \quad (2)$$

326 where  $S_{uu}$  and  $S_{ww}$  are the power spectral density functions of the fluctuating streamwise and vertical  
 327 velocity components, respectively, and  $\sigma_u^2$  and  $\sigma_w^2$  are the streamwise and vertical velocity variances.  
 328 The non-dimensional frequency is defined as  $n_i = fL_i^x/U$ , where  $L_u^x$  and  $L_w^x$  are the integral length  
 329 scales of the longitudinal and vertical velocity components, respectively. These represent the average  
 330 size of eddies corresponding to the peak of the turbulence spectrum, which can be determined semi-  
 331 empirically from the peak spectral frequency, or from the auto-correlation of the fluctuating velocity  
 332 component (Farell and Iyengar 1999).

333 Figure 6(a) shows a noticeable shift of the longitudinal power spectra to higher energy levels with  
 334 increasing turbulence intensity at a height of 0.3 m within two different wind tunnel boundary layers  
 335 (Jafari *et al.* 2019a). The shift in the spectral peak to smaller length scales by matching the turbulence  
 336 intensity also indicates that the low-frequency part of the spectra cannot be reproduced, as due to the  
 337 wind tunnel's restricted cross-section and length, the generation of turbulent eddies is limited. (Peterka  
 338 *et al.* 1998; Iyengar and Farell 2001; Banks 2011; Kozmar 2012; De Paepe *et al.* 2016; Leitch *et al.*  
 339 2016). A similar trend is shown for the vertical turbulence spectra in Figure 6(b), with a shift to higher  
 340 frequencies. Pfahl *et al.* (2015) suggested that reproducing the vertical power spectrum is important for  
 341 evaluating the peak wind loads on a stowed heliostat, because of the linear relationship found by  
 342 Rasmussen *et al.* (2010) between the vertical spectra and the lift forces and hinge moments on a

343 horizontal flat plate exposed to small vertical turbulence  $I_w \leq 10\%$ . Jafari *et al.* (2019b) found that  
 344 turbulent length scales of the same order as the heliostat's chord (windward) length and an order of  
 345 magnitude larger, corresponding to a range of reduced frequencies,  $0.1 < fc/U < 1$ , effectively  
 346 contribute to the unsteady wind loads. Hence, it was proposed by Jafari *et al.* (2019b) that this range of  
 347 reduced frequencies of the turbulence spectra should be carefully simulated in wind tunnel studies in  
 348 order to reduce the scaling impact on the measured peak wind loads and provide accurate wind load  
 349 predictions on the full-scale structure.



350  
 351 Figure 6. Comparison of wind tunnel measurements in two simulated ABLs (Jafari *et al.* 2019a) with the modified  
 352 von Karman form (ESDU 85020 2001) of non-dimensional turbulence spectra of the (a) longitudinal fluctuating  
 353 component of wind speed  $u$ , (b) vertical fluctuating component of wind speed  $w$ . Simultaneous matching of both  
 354 the longitudinal and vertical spectra in the critical range of reduced frequencies cannot be achieved in scaled  
 355 model wind tunnel experiments. Similarity of turbulence spectra should be applied to the velocity component that  
 356 contributes to the unsteady wind loads on the heliostat configuration being investigated.

357 The discrepancies between wind tunnel and atmospheric turbulence spectra bring into question the  
 358 reliability of wind load measurements and whether they correspond to the wind loads on full-scale  
 359 heliostats. However, the formation of turbulent eddies in a wind tunnel is restricted by the tunnel's  
 360 limiting dimensions, therefore the integral length scales in the full-scale ABL cannot be replicated  
 361 (Jafari *et al.* 2019a). The integral length scales of the vertical velocity component increase with height  
 362 from the ground in wind tunnel and full-scale measurements. In contrast, the longitudinal length scales  
 363 are larger near the surface in a wind tunnel boundary layer, where an increased base width of the spires  
 364 generates large vortices through separation. Regardless of the different mechanisms that create  
 365 turbulence in the wind tunnel and the lowest 20 m of the full-scale ABL, the increase in  $L_u^x$  and the  
 366 decrease in  $L_w^x$  is also seen in the ASL's lower regions due to blocking of the vertical velocity component

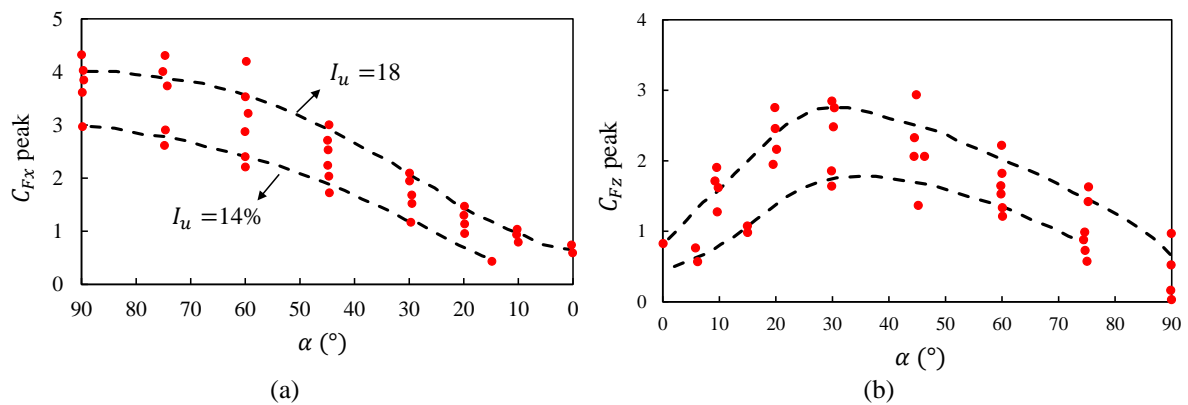


367 near the ground (Jafari *et al.* 2019a). Pfahl (2018) concluded that matching the vertical turbulence  
368 intensity with full-scale standard data, despite a shift of the streamwise turbulence spectrum to higher  
369 frequencies in wind tunnel experiments, was appropriate for determining the lift force and hinge  
370 moment measurements on a model-scale stowed heliostat. Hence, the geometric scaling ratio of a  
371 heliostat model should be determined according to the turbulence spectrum for the corresponding full-  
372 scale structure, considering the effects of both terrain and height, and the spectrum of the simulated  
373 boundary layer in a wind tunnel. The geometric scaling ratios for modelling a prototype heliostat in an  
374 open-country terrain were determined as an example by Jafari *et al.* (2019b). It was found that similarity  
375 of the streamwise velocity spectrum is required to model the unsteady drag force on a vertical heliostat  
376 at  $\alpha = 90^\circ$  and a 1:20 scale model with larger dimensions showed the closest match to the modified  
377 von Karman spectrum (ESDU 85020 2001). In contrast, accurate measurement of the unsteady lift force  
378 on a stowed heliostat requires similarity of the vertical turbulence spectrum, which showed the closest  
379 match to the von Karman spectrum (ESDU 85020 2001) for a 1:60 model with smaller dimensions. The  
380 relative contribution of the longitudinal and vertical components of turbulence, for a stowed heliostat  
381 and over the range of heliostat operating conditions, should be further verified through wind tunnel and  
382 full-scale measurements. Since the unsteady longitudinal and vertical turbulence components are not  
383 generated independently using spires and roughness elements, this would require investigation of active  
384 methods of turbulence generation. Analysis of wind loads on full-scale heliostats with respect to the  
385 incoming wind turbulence measured simultaneously can also verify the scaling effects observed in wind  
386 tunnel experiments to provide a more reliable estimation of wind loads.

### 387 2.3. *Effect of turbulence intensity and length scales on peak wind loads*

388 The impact of turbulence on heliostat wind loads has been widely investigated through systematic  
389 wind tunnel experiments in the literature. Further to the variation of the time-averaged component of  
390 the wind speed with height and surface roughness in the ABL for the determination of design wind  
391 speeds on heliostats, the temporal characteristics are defined by the intensity of the velocity fluctuations  
392 and the spatial variations are characterised by the integral length scale of turbulent eddies. Turbulence  
393 intensity in the approaching flow is a commonly reported parameter that affects the wind loads on

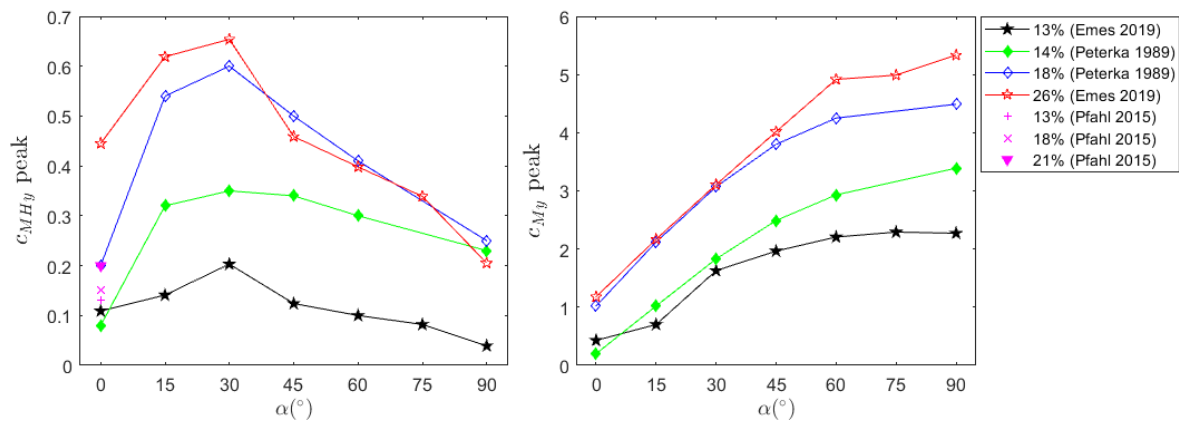
394 operating and stowed heliostats. Peterka *et al.* (1989) studied the mean and peak wind loads on a  
 395 heliostat at different elevation angles in simulated boundary layers at  $I_u = 14\%$  and  $I_u = 18\%$ . It was  
 396 found that with increasing  $I_u$ , the peak lift and drag force coefficients increased for all elevation angles,  
 397  $\alpha$ , of the heliostat panel with respect to the horizontal, with best-fit curves shown by the dashed lines  
 398 in Figure 7. The maximum drag force coefficient at  $\alpha = 90^\circ$  increased from 3 to 4, and the peak lift  
 399 force coefficient at  $\alpha = 30^\circ$  increased from 1.7 to 2.7 by increasing  $I_u$  at the heliostat hinge height from  
 400 14% to 18%. Furthermore, according to Peterka *et al.* (1987), the peak lift force coefficient on a heliostat  
 401 at stow increased from 0.5 to 0.9 when  $I_u$  increased from 14% to 18%. Peterka *et al.* (1989) discussed  
 402 that the reason for the increase in the wind loads was not found in their experiments but it was likely to  
 403 be was linked to the interaction of turbulence and separated shear layers near the plate's edge.



404 Figure 7. (a) Peak drag force and (b) lift force coefficients on a heliostat at different elevation angles,  $\alpha$ , at  $I_u = 14\%$   
 405 and  $I_u = 18\%$ . Reproduced from Peterka *et al.* (1989).

406 Emes *et al.* (2019a) further investigated the effect of turbulence intensity on the peak aerodynamic  
 407 hinge and overturning moment coefficients on a single heliostat model, through an extension of  
 408 turbulent ABLs simulated in previous wind tunnel experiment studies by Peterka *et al.* (1989) and Pfahl  
 409 *et al.* (2015). The percentages in the legend of Figure 8 indicate the longitudinal turbulence intensity at  
 410 the hinge height of the heliostat model for open terrains of a range of roughness heights. Increased  
 411 intensity of turbulence of the approaching ABL flow directly correlated to increases in the peak moment  
 412 coefficients. The quasi-steady peak values of the force and moment coefficients are determined as the  
 413 sum of the mean and three-times the standard deviation of the fluctuating moment, with a 99.7%  
 414 probability of not being exceeded following a Gaussian distribution (Simiu and Scanlan 1996). As

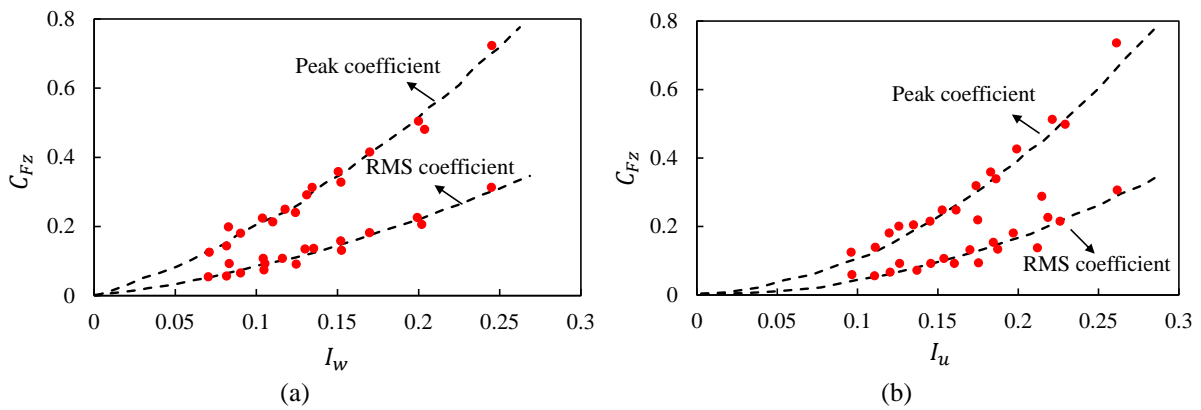
415 reported by Peterka and Derickson (1992), there is an approximately linear increase of the peak  
 416 coefficients with increasing turbulence intensity at  $I_u \geq 10\%$ . The difference between the scaling  
 417 factors of the model-scale ABL and heliostat in wind tunnel experiments with respect to their full-scale  
 418 counterparts led to variations in the peak wind load coefficients. The relative sizes of the heliostat chord  
 419 length and the energy-containing eddies is another important factor influencing the range of frequencies  
 420 that contribute to the generation of fluctuating loads.



421  
 422 Figure 8. Effect of turbulence intensity  $I_u$  (%) and elevation angle  $\alpha$  of a heliostat in wind tunnel experiments  
 423 (Peterka *et al.* 1989; Pfahl *et al.* 2015; Emes *et al.* 2019a) on: (a) peak hinge moment coefficient, and (b) peak  
 424 overturning moment coefficient.

425 Due to the anisotropic nature of atmospheric turbulence and depending on the orientation of the  
 426 heliostat panel, both streamwise and vertical turbulence parameters can be of significance for the wind  
 427 loads. While in the previous experiments by Peterka *et al.* (1989) and Emes *et al.* (2017), all components  
 428 of turbulence intensity varied during the experiments, the observed effects on the wind load coefficients  
 429 were only correlated with longitudinal turbulence intensity and the variations of vertical turbulence  
 430 components were not differentiated. Pfahl (2018) proposed that at stow position, vertical velocity is  
 431 more decisive for the pressure forces on the panel as it acts normal to it and therefore the lift force  
 432 coefficient on a stowed heliostat was suggested to be more closely correlated with vertical turbulence  
 433 intensity,  $I_w$ . The lift force on a stowed heliostat model in a simulated boundary layer was measured in  
 434 a series of tests, where  $I_u$  and  $I_w$  varied in the wake of cylinders of different diameters. Figure 9 shows  
 435 the peak and root mean square (RMS) lift force coefficients as a function of  $I_u$  and  $I_w$ . Pfahl (2018)  
 436 discussed that the curve-fitted coefficients showed a better match as a function of  $I_w$ , and therefore,  $I_w$

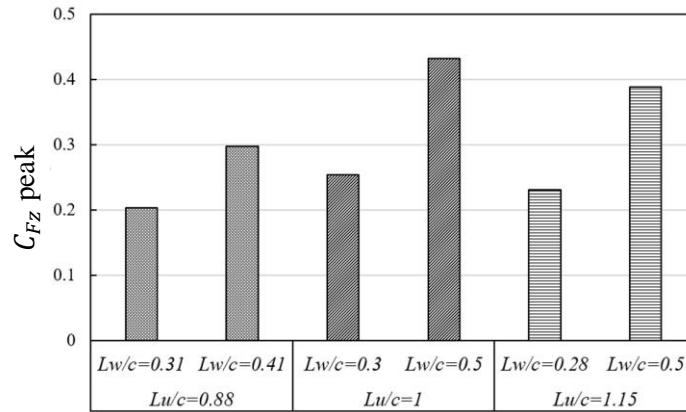
437 has a stronger effect on the lift force than  $I_u$ . This conclusion was drawn from comparison of the lift  
 438 force coefficients for two cases in the cylinder wake with a heliostat model in a simulated boundary  
 439 layer with  $I_w = 10\%$  was identical. However, the turbulence in the wake of a cylinder is dominated by  
 440 quasi-static vortex shedding with different vertical turbulence profiles and spectral properties than in  
 441 the ABL. Pfahl (2018) suggested that the lift force and hinge moment coefficients in stow position were  
 442 largely dependent on the vertical turbulence intensity compared with dissimilarities of the turbulence  
 443 spectra. Despite changes in the shape of the spectra affecting the pressure distribution, it was found that  
 444 the differences in strength and width of the high-pressure suction region near the heliostat mirror panel's  
 445 edge compensate each other regarding these wind load coefficients.



446 Figure 9. Effect of turbulence intensity on peak and RMS lift force coefficients on a stowed heliostat for: (a)  
 447 longitudinal turbulence intensity,  $I_u$ , (b) vertical turbulence intensity,  $I_w$ . Reproduced from Pfahl (2018).

448 Another important parameter which influences the wind loads is the integral length scale of  
 449 turbulence in the boundary layer. The ratio of the integral length scale to the heliostat chord length was  
 450 found to impact the wind loads on a heliostat at stow position. Emes *et al.* (2017) studied the effect of  
 451 changes in  $L_u^x/c$  by measuring the lift force on stowed heliostat models of different chord length  
 452 dimensions in a modelled atmospheric boundary layer. They found that the peak lift force coefficient  
 453 increased with increasing  $L_u^x/c$ , however both  $L_u^x/c$  and  $L_w^x/c$  varied simultaneously by changing the  
 454 chord length dimensions of the heliostat. By stowing a fixed heliostat size with constant  $c$  at different  
 455 heights in a simulated ABL, Jafari *et al.* (2019a) showed that the peak lift coefficient was more strongly  
 456 correlated with  $L_w^x/c$  than  $L_u^x/c$ . As shown in Figure 10, the peak lift coefficient increased by 65%  
 457 when  $L_w^x/c$  increased from 0.3 to 0.5 at a constant  $L_u^x/c = 1$ . In comparison, only a 10% reduction in

458 the lift coefficient was observed with increasing  $L_u^x/c$  from 1 to 1.15 at a constant  $L_w^x/c = 0.5$ . Hence,  
 459 this demonstrates that the vertical component of the fluctuating velocity makes a larger contribution to  
 460 the generation of the lift force on a stowed heliostat. The relative influence of the longitudinal and  
 461 vertical turbulence components on the heliostat wind loads at intermediate elevation angles, such as the  
 462 maximum operating lift force and hinge moment at  $\alpha = 30^\circ$ , should be considered in future  
 463 investigations.



464  
 465 Figure 10. Comparison of peak lift force coefficients in stow position for similar values of  $L_u^x/c$  and different  
 466 values of  $L_w^x/c$  in the ABL with  $z_0 = 0.018$  m (Jafari *et al.* 2019a).

467 The combined effects of intensity and integral length scales of turbulence on the aerodynamic load  
 468 coefficients were studied by measurement of the unsteady wind loads on vertical ( $\alpha = 90^\circ$ ) and stowed  
 469 ( $\alpha = 0^\circ$ ) heliostats in two simulated ABLs by Jafari *et al.* (2018) and Jafari *et al.* (2019a), respectively.  
 470 Heliostat models of different chord length dimensions between 0.3 m and 0.8 m at a fixed height  $H =$   
 471 0.5 m were tested for the maximum drag case on the vertical heliostat. Three chord length dimensions  
 472 ( $c = 0.5, 0.6, 0.7$  m) with  $H/c$  ratios between 0.2 and 1.3 were tested for the maximum lift case on the  
 473 stowed heliostat. The peak drag force coefficient on a vertical heliostat (Figure 11a) followed a  
 474 logarithmic function of the longitudinal turbulence intensity and longitudinal integral length scale:

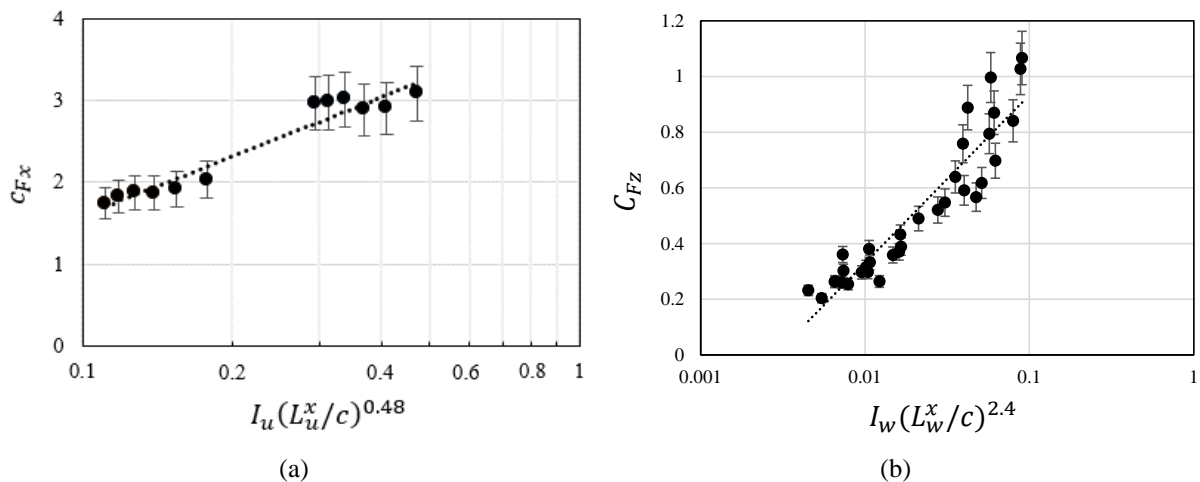
$$475 \quad c_{Fx} = 1.05 \ln \left[ I_u \left( \frac{L_u^x}{c} \right)^{0.48} \right] + 4 \quad (9)$$

476 In contrast, the peak lift force on a heliostat at stow position (Figure 11b) was shown to correlate with  
 477 a logarithmic function of the vertical turbulence intensity and length scale:

$$478 \quad c_{Fz} = 0.267 \ln \left[ I_w \left( \frac{L_w^x}{c} \right)^{2.4} \right] + 1.566 \quad (10)$$

479 The turbulence parameters in equations 9-10 describe the spatial and temporal release of turbulence  
 480 energy and their effect on the fluctuating load coefficients. The larger exponent of 2.4 in the logarithmic  
 481 function in equation 10 shows a larger sensitivity of the peak lift force coefficient to  $L_w^x/c$  than to  $I_w$ .  
 482 As a result, the influence of the vertical velocity turbulent energy's spatial distribution on the lift force  
 483 on a stowed heliostat is greater than the vertical velocity turbulent energy's temporal release. In contrast,  
 484 the smaller exponent of 0.48 indicates that the spatial release of longitudinal energy in the investigated  
 485 range of  $L_u^x/c$  between 1 and 4, has a relatively smaller effect on the peak drag force coefficient on a  
 486 vertical heliostat. Hence, the peak wind loads on heliostats in the ABL can effectively be estimated for  
 487 these two critical load cases using the defined turbulence parameter, in terms of the expected full-scale  
 488 turbulence intensity and length scales that are a function of the surface roughness of the terrain in Figure  
 489 3 and Figure 4, respectively.

490

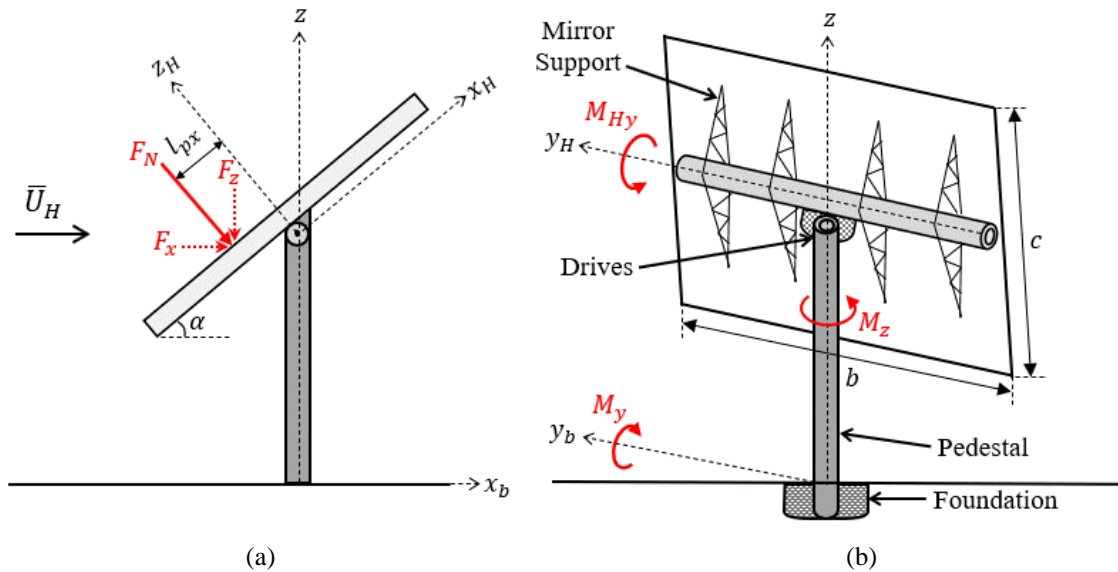


491 Figure 11. Peak wind load coefficients on a heliostat: (a) drag force coefficient at  $\alpha = 90^\circ$  as a function of  
 492 longitudinal turbulence intensity and integral length scale (Jafari *et al.* 2018); (b) lift force coefficient at  $\alpha = 0^\circ$   
 493 as a function of vertical turbulence intensity and integral length scale (Jafari *et al.* 2019a). The dashed lines  
 494 indicate the logarithmic relationships in equations 9-10 based on the longitudinal and vertical turbulence  
 495 parameters, respectively.

### 496 3. Heliostat geometry effects on wind loads

497 The wind effects on heliostats are well represented by the bluff body aerodynamics of the large  
 498 reflecting surface inclined at different elevation and azimuth angles during operation of a power tower  
 499 plant. Figure 12 shows the wind loads on a conventional azimuth-elevation heliostat, consisting of an  
 500 array of rectangular glass facets mounted on tubular steel components in a T-shaped configuration to

501 withstand the maximum bending moments about the hinge and the base of the heliostat pedestal. When  
 502 inclined at different elevation angles, the gap between the lower edge of the heliostat panel and the  
 503 ground which enlarges as  $\alpha$  decreases. The critical scaling parameters that have been investigated in  
 504 the literature include the aspect ratio of the rectangular heliostat panel in section 3.1, the gaps between  
 505 the heliostat facets in section 3.2, and the vertical distance between the elevation axis and the ground  
 506 by the pylon height in section 3.3.

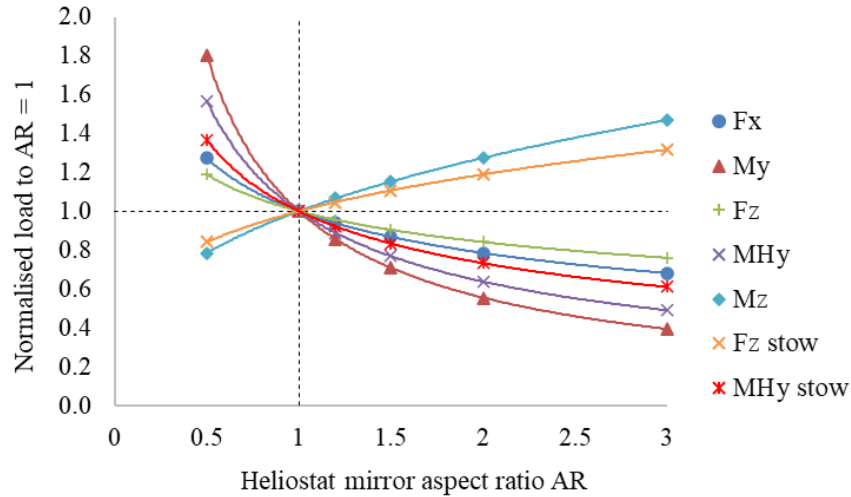


507  
 508 Figure 12. Schematic diagram of the (a) drag and lift forces on the heliostat surface inclined at elevation angle  
 509  $\alpha$ , (b) hinge, overturning and azimuth moments on the heliostat components (Emes *et al.* 2020a).

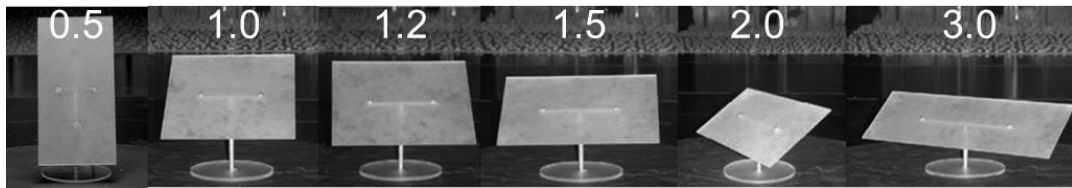
### 510 3.1. Aspect ratio

511 The aspect ratio of the heliostat, defined as the ratio of the width to the height  $AR = b/c$  of the  
 512 panel in Figure 12(b), has a significant but varying impact on the wind load components on a heliostat.  
 513 The main components of the heliostat that are exposed to wind effects are the foundation, the pedestal,  
 514 the panel and the elevation and azimuth drives. Figure 13 shows the impact of the aspect ratio of a  
 515 heliostat panel on the normalised load coefficients for the maximum operating load cases and in stow  
 516 position ( $\alpha = 0^\circ$ ), based on fitted exponential functions of scale-model heliostat measurements in a  
 517 boundary layer wind tunnel (Pfahl *et al.* 2011a). It can be observed that  $M_y$  about the base of the upright  
 518 heliostat at  $\alpha = 90^\circ$  decreases by approximately 30% at  $AR = 1.5$  and by as much as 60% at  $AR = 3$   
 519 relative to a square-shaped heliostat ( $AR = 1$ ). A reduction in  $M_y$  and  $M_{Hy}$  with increasing aspect ratio  
 520 indicates smaller loads on the elevation drive and that the foundation pile depth and pylon diameter can

521 be reduced. However, the  $M_z$  on operating heliostat and  $F_z$  on stowed heliostat increase by 47% and  
 522 30%, respectively, with increasing AR from 1 to 3. Hence, there is a trade-off between the dimensions  
 523 of the pedestal with the elevation drive and the torque tube with the azimuth drive in the heliostat design.



524



525

526

527 Figure 13. Effect of aspect ratio on the normalised heliostat loads for the maximum wind load configurations  
 528 during operation and stow. Reproduced from the best-fit power law exponents in Table 3 of Pfahl *et al.* (2011a).

529 3.2. Facet gap

530 Conventional heliostats are designed with small gaps between the mirror facets. Wu *et al.* (2010)  
 531 found that small gaps have a negligible impact on the force and moment coefficients through wind  
 532 tunnel tests and numerical analysis. However, wider gaps in the mirror panel caused a larger pressure  
 533 difference at the edges of the gap at the windward corners. This led to a 20% increase of the hinge  
 534 moment on a heliostat at  $\alpha = 30^\circ$ , due to a shift of the low-pressure region on the leeward surface away  
 535 from the central elevation axis for wind flow along the gap at  $\beta = 0^\circ$  (Pfahl *et al.* 2011c). The peak  
 536 hinge moment at stow position with a wide gap was also increased due to a similar effect. Peterka and  
 537 Derickson (1992) stated that the area represented by slits in the mirror panel can be considered as a  
 538 solid surface area up to a ratio of 15%. The wind load coefficients were compared with no gap and a  
 539 heliostat with two mirror facets separated by a wide gap mirror facets. The total mirror area ( $30 \text{ m}^2$  at

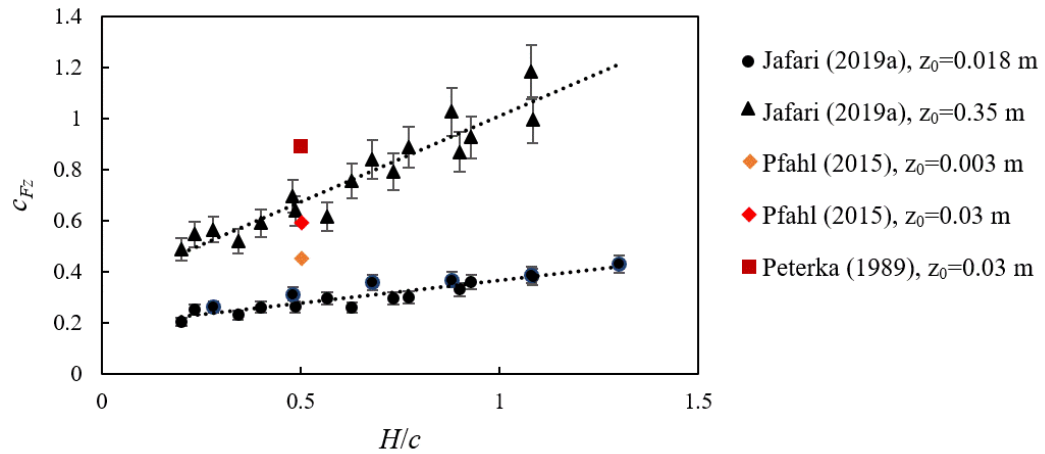


540 full scale, modelling scale 1:20), with a gap width of 0.5 m corresponded to a portion of 8% of the  
541 opening. With the exception of the peak operating hinge moment at  $\alpha = 30^\circ$  increasing by 20%, there  
542 was only a small effect of gap on the wind loads, in agreement with the findings by Peterka and  
543 Derickson (1992). The shielding effect of support structure components contributed to small increases  
544 in the drag force in stow position and operating load cases with wind impacting the back surface of the  
545 heliostat. Hence, the geometry of a heliostat concentrator consisting of facets with narrow gaps can  
546 effectively be modelled as a thin flat plate when considering the aerodynamic wind loads on a heliostat,  
547 whereas accurate prediction of the dynamic wind loads (refer to Section 4) requires similarity of the  
548 structural stiffness and mass distribution of the heliostat support structure.

### 549 3.3. Pylon height

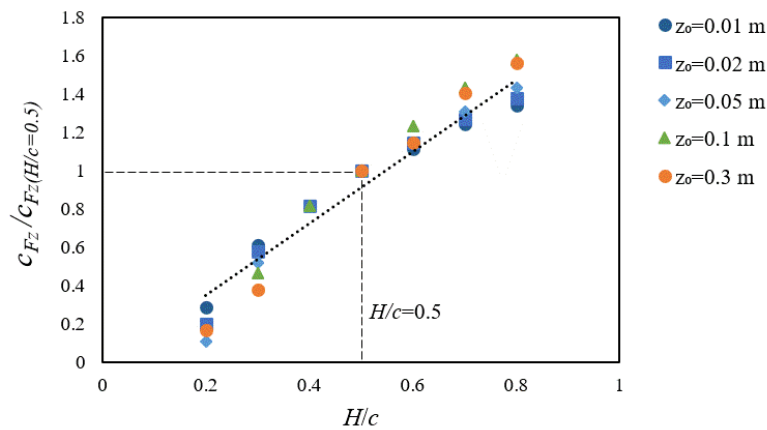
550 Conventional azimuth-elevation heliostats are commonly designed for a ratio of hinge height to  
551 mirror chord length,  $H/c = 0.5$ , increasing to 0.7 for a heliostat with a horizontal primary axis (Téllez  
552 *et al.* 2014). As shown in in Figure 14(a), the peak lift coefficient in stow position at  $H/c = 0.5$  varies  
553 over a range between 0.4 and 0.9, depending on the spectral distribution of ABL turbulence (refer to  
554 Section 2.2) and the ratio of the integral length scales to the scale model heliostat characteristic length  
555 in different wind tunnel experiments (Emes *et al.* 2017). Measurement of the peak lift force on models  
556 with varying pylon heights over a range of  $H/c$  between 0.2 and 0.8 was used to study the effect of  
557 heliostat hinge height on stow loads. Jafari *et al.* (2019a) found that the lift coefficient on a stowed  
558 heliostat followed a linear variation with  $H/c$  from 0.5 to 0.2, such as a reduction from 0.3 to 0.2 at  
559  $I_w = 9\%$  ( $z_0 = 0.018$  m), and from 0.65 to 0.48 at  $I_w = 19\%$  ( $z_0 = 0.35$  m). The rate of reduction of  
560  $c_{Fz}$  with decreasing  $H/c$  is larger in the ABL with  $z_0 = 0.35$  m, such that the slope of the linear function  
561 at  $z_0 = 0.35$  m is three times larger than for  $z_0 = 0.018$  m. Figure 14(b) shows the peak lift force  
562 coefficient on a heliostat at stow, normalised with respect to  $H/c = 0.5$  as a function of  $H/c$  for different  
563 values of aerodynamic roughness length  $z_0$ . The peak  $c_{Fz}$  on a stowed heliostat within the ABL follows  
564 a linear function of  $H/c$  that is relatively independent of  $z_0$ . This relationship indicated that the stow  
565 lift force can be decreased by up to 80% by lowering the stow height of a fixed size panel such that  $H/c$

566 decreases from 0.5 to 0.2 (Jafari *et al.* 2019a). The pylon height is fixed in contemporary heliostat  
 567 designs (Pfahl *et al.* 2017a), nevertheless novel concepts such as a carousel heliostat with spindle drive  
 568 (Pfahl *et al.* 2017b) to lower the heliostat mirror close to the ground in stow during high-wind conditions  
 569 can reduce the maximum wind loads and the cost of a cantilevered heliostat.



570

(a)



(b)

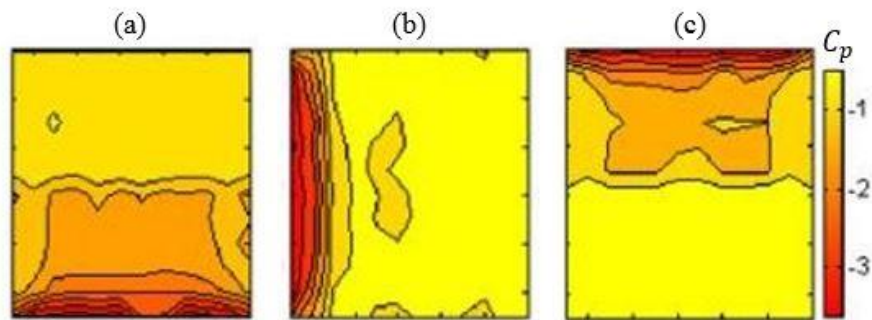
571 Figure 14. Effect of the hinge height to panel chord length ratio  $H/c$  on: (a) the peak lift force coefficient at stow based on  
 572 different wind tunnel studies, (b) peak lift coefficient normalised with respect to heliostat with  $H/c = 0.5$ , as a function of  
 573 ABL aerodynamic roughness height  $z_0$ . Reproduced from Jafari *et al.* (2019a).

#### 574 4. Dynamic wind effects on heliostat vibrations and tracking error

##### 575 4.1. Heliostat surface pressure distributions

576 Dynamic wind load analysis on heliostats has been investigated using transient FEA simulations  
 577 and experimental data from wind tunnel or full-scale measurements, such as through surface pressure  
 578 measurements by Gong *et al.* (2013) on a 1:10 scale model T-shaped heliostat. Gong *et al.* (2013)

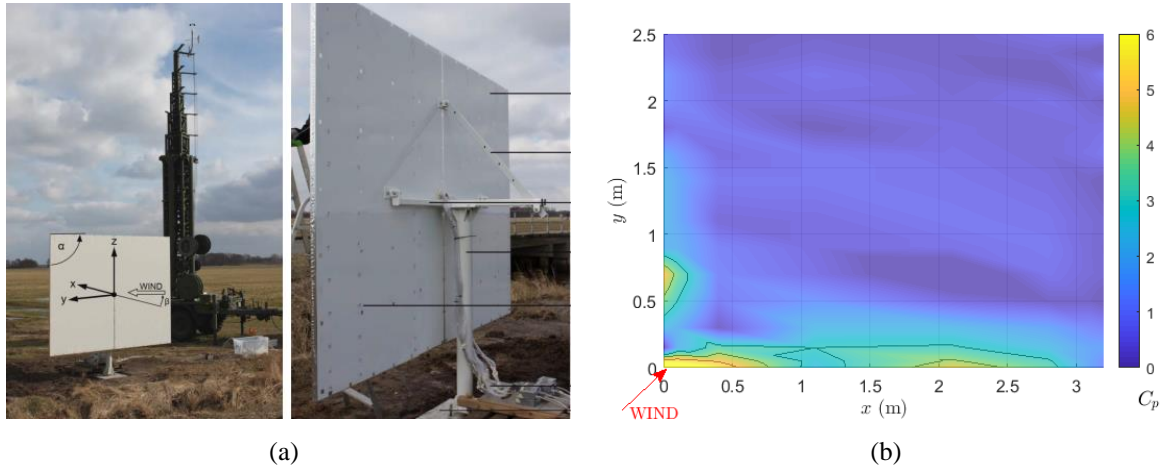
579 showed that at the leading edge of the stowed heliostat mirror surface, substantial negative peak wind  
 580 pressure coefficients occurred. It is presumed that the turbulent eddies associated with the peaks of the  
 581 turbulence spectra that are similar in size to the chord length of the heliostat mirror have a large impact  
 582 on the maximum lift forces and hinge moments on stowed heliostats (Pfahl *et al.* 2015). However, the  
 583 effect of the size of these eddies relative to the size of the heliostat chord length on the unsteady loads  
 584 and non-uniform pressure distributions on stowed heliostats has not previously been investigated.



585  
 586 Figure 15. Peak pressure coefficient contours on a stowed heliostat at different azimuth angles: (a)  $\beta = 0^\circ$ ; (b)  
 587  $\beta = 90^\circ$ ; (c)  $\beta = 180^\circ$ . Reproduced from Gong *et al.* (2013).

588 Pfahl *et al.* (2014b) showed that the temporal variation of the stow hinge moment on an 8 m<sup>2</sup>  
 589 heliostat, instrumented with 84 differential pressure sensors in an open field in Lilienthal in northern  
 590 Germany (Figure 16a), exhibited distinctive peaks over consecutive durations of approximately one  
 591 second. This suggests that the 3-second gust wind speed commonly applied in design codes and  
 592 standards (ASCE 7-02 2002; EN 1991-1.4 2010; AS/NZS 1170.2 2011) and recommended by the World  
 593 Meteorological Organisation (WMO) for wind measurements, can under-estimate the gust wind speed  
 594 and the maximum unsteady wind loads on heliostats. The peak pressure coefficient distribution in  
 595 Figure 16(b) at the instant of the maximum hinge moment, with peak  $c_{MHY} = 0.18$  and  $c_{FZ} = 1.0$  at  
 596  $\beta = 47^\circ$  and  $U = 5$  m/s indicates a significant variation of positive pressure (suction) along the side  
 597 edges. Pfahl (2018) discussed that the peak aerodynamic coefficients showed a general agreement with  
 598 tabulated values derived in controlled wind tunnel experiments by Peterka and Derickson (1992) at  $I_u =$   
 599 18% and  $U = 12.5$  m/s. However, the turbulence characteristics of the ABL flow in the field study by  
 600 Pfahl (2018) were not reported. Notably the spatial similarity of the heliostat chord length ( $c = 2.5$  m)  
 601 and the integral length scale of the energy-containing turbulent eddies was only estimated as  $L_u^x = 3$  m

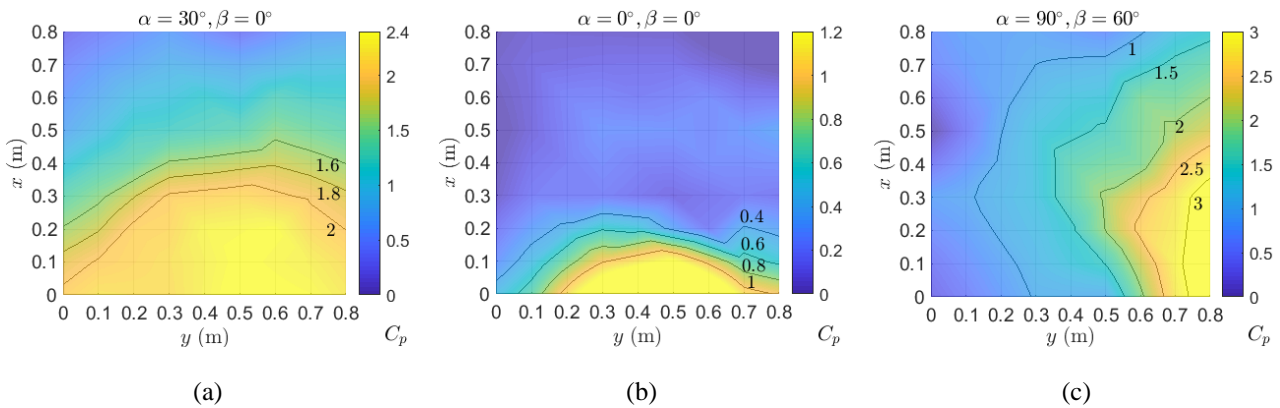
602 at  $z = H = 2$  m, based on extrapolation of semi-empirical data (ESDU 85020 2001) in an open country  
 603 terrain with  $z_0 = 0.03$  m. High-frequency field measurements of wind velocity are thus required to  
 604 validate the turbulence characteristics at heights below 6 m where heliostats are stowed and verify the  
 605 peak wind load coefficients corresponding to the critical operating and stow load cases of heliostats  
 606 established in wind tunnel experiments.



607 Figure 16. (a) Field heliostat instrumented with differential pressure sensors in open country terrain (Pfahl 2014a);  
 608 (b) peak pressure coefficient distribution corresponding to the maximum hinge moment  $c_{MHy} = 0.18$  on the  
 609 stowed heliostat at  $\beta = 47^\circ$ , reproduced from Pfahl (2018).

610 Emes *et al.* (2019a) showed that the hinge moment was highly correlated with the movement of the  
 611 unsteady centre of pressure from the central elevation axis, which increased significantly with  
 612 increasing turbulence intensity and decreasing elevation angle of the heliostat. Through the  
 613 decomposition of the hinge moment into the net normal force and the centre of pressure distance, the  
 614 pressure distributions on the heliostat surface representing the maximum hinge, overturning and  
 615 azimuth moments were determined (Emes *et al.* 2019b). A high-pressure region was observed on the  
 616 operating heliostat surface at  $\alpha = 30^\circ$  in Figure 17(a), leading to the maximum  $c_{Fz} = 2.83$  and  $c_{MHy} =$   
 617  $0.18$ . Despite smaller peak values of  $c_{Fz} = 0.42$  and  $c_{MHy} = 0.11$  on the stowed heliostat at  $\alpha = 0^\circ$  in  
 618 Figure 17(b), there was an increased longitudinal ( $x$ ) movement from the central elevation axis ( $y =$   
 619  $0.4$  m) relative to the operating heliostat. During operation, an area of high-pressure difference on the  
 620 frontal half of the heliostat surface ( $\alpha = 30^\circ$ ) and flow separation at the windward edge of the stowed  
 621 heliostat surface ( $\alpha = 0^\circ$ ) created the highest hinge moment on the torque tube. In contrast, the  
 622 maximum azimuth moment during operation (Figure 17c) corresponded to the maximum drag

623 coefficient  $c_{Fx} = 2.29$  at  $\alpha = 90^\circ$ ) but with wind approaching the heliostat at  $\beta = 60^\circ$ . Probability  
624 distributions of the transient load fluctuations followed a Gaussian distribution for most of the load  
625 cases except the maximum operating azimuth moment (Emes *et al.* 2020a). In contrast, wind tunnel  
626 measurements by Xiong *et al.* (2021) found that the fluctuating shear force at the base of the heliostat  
627 pylon followed a Gaussian distribution at  $\alpha$  between  $0^\circ$  and  $20^\circ$  and the peak value of the base shear  
628 force was most accurately represented by a Generalized Pareto Distribution (GPD) at  $\alpha$  between  $30^\circ$   
629 and  $90^\circ$ . This suggests that the quasi-steady peak wind loads are generally appropriate to predict the  
630 maximum loads in operating and stow configurations, but extreme value analysis of the fluctuating load  
631 distribution should be considered in operating positions. It should be noted that despite the smaller peak  
632 coefficients on a stowed heliostat, the ultimate design loads should consider a larger survival wind speed  
633 compared to the wind speed for calculation of the maximum operating hinge and overturning moments.



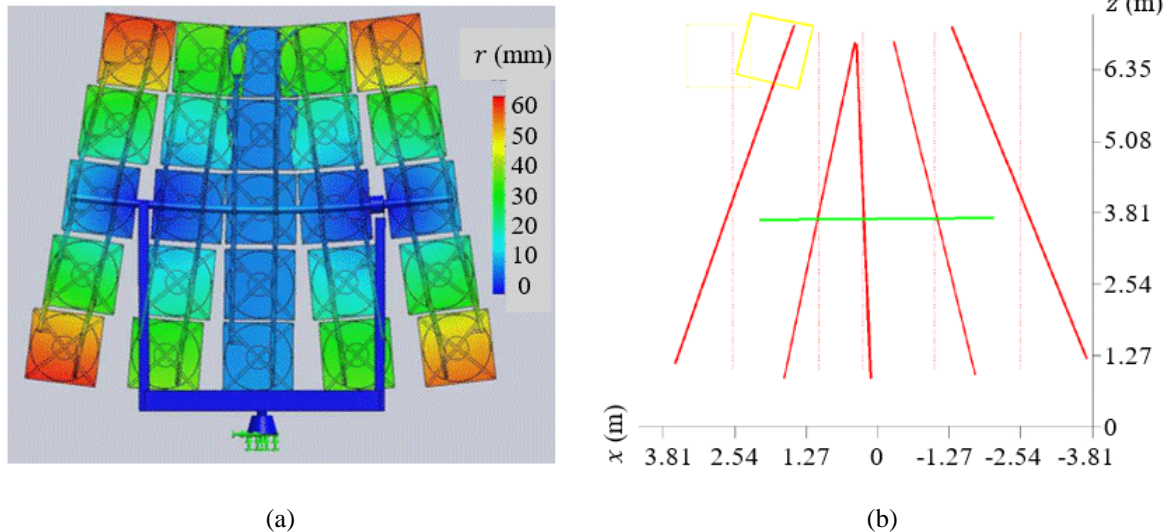
634 Figure 17. Peak pressure distributions on an instrumented heliostat in a boundary layer wind tunnel with  $I_u =$   
635  $13\%$  and  $I_w = 8\%$ , leading to the maximum: (a) operating hinge moment, (b) stow hinge moment, (c) azimuth  
636 moment (Emes *et al.* 2019a).

#### 637 4.2. Modal vibration analysis and fatigue loads

638 The dynamic response of small-scale structures such as heliostats affects their ability to withstand  
639 gusts in the ABL and maintain structural integrity for their expected design life. As heliostats are slender  
640 in shape and have low natural frequencies less than 10 Hz, the structural components of heliostats can  
641 be exposed to flow-induced vibrations from the unsteady fluctuating loads caused by turbulence effects.  
642 Vortex shedding can generate cyclic wind load fluctuations on the elevation and azimuth drives in the  
643 frequency range between 1 and 5 Hz of a conventional heliostat, as well as significant vibration and  
644 resonance effects (Gong *et al.* 2012; Griffith *et al.* 2015). Excessive deflections and stresses caused by

645 wind-induced oscillations can lead to structural failure (Jain *et al.* 1996; Mendis *et al.* 2007). Galloping  
646 and torsional flutter tend to occur at frequencies on the order of 1 Hz where the turbulence integral  
647 length scales are similar in size to the characteristic length of the heliostat components, such as the  
648 pylon, torque tube and mirror structural truss members. A quasi-steady increase in mean velocity occurs  
649 when the turbulence scale is increased beyond the order of magnitude of the body scale (Nakamura  
650 1993) and the galloping effect becomes negligible when the turbulence scale is decreased below the  
651 size of the structural member as smaller eddies cannot cause high net pressures over the surface (Pfahl  
652 *et al.* 2015).

653 The equivalent static wind loads have been the subject of most experimental studies, however the  
654 dynamic loads due to wind-induced displacements are important for determining the heliostat drive  
655 units and support structure components. Dynamic testing of full-scale heliostats was undertaken by  
656 Sandia National Laboratories at the National Solar Thermal Test Facility (NSTTF) on a 37 m<sup>2</sup> heliostat  
657 instrumented with triaxial accelerometers, strain gauges and anemometers to evaluate the modal shapes  
658 and frequencies (Andraka *et al.* 2013). Modal tests of the NSTTF heliostat using hammer excitation  
659 identified a number of modes of vibration, including bending of the support structure in modes 1 and 2,  
660 bending of the torque tube in modes 3 (Figure 18) and 4, and in-plane and out-of-plane bending of the  
661 mirror-truss assemblies (Griffith *et al.* 2012; Ho *et al.* 2012). The natural frequencies derived from  
662 experimental measurements showed good agreement with finite element analysis (FEA) predictions of  
663 the wind-excited dynamic response, such as a modal frequency of 3 Hz corresponding to the first torque  
664 tube bending mode 3 in Figure 18. However, higher order modes with dependence on the stiffness  
665 properties of joints and drive mechanisms, such as out-of-plane support structure bending modes, were  
666 not accurately predicted by the FEA model. Furthermore, the low-frequency modes of vibration showed  
667 increased damping by 24-120% due to aerodynamic damping excited by the wind at speeds of 5-15 m/s  
668 compared with the calm winds during the hammer-excited tests. Comparison of the modal frequencies  
669 on different heliostat sizes and elevation angles showed that the azimuth drive modal frequency  
670 increased from 1.28 Hz to 2.28 Hz at  $\alpha = 90^\circ$  and from 1.04 Hz to 1.75 Hz at  $\alpha = 0^\circ$  with increasing  
671 heliostat size from 37 m<sup>2</sup> to 60 m<sup>2</sup> (Ho *et al.* 2012).

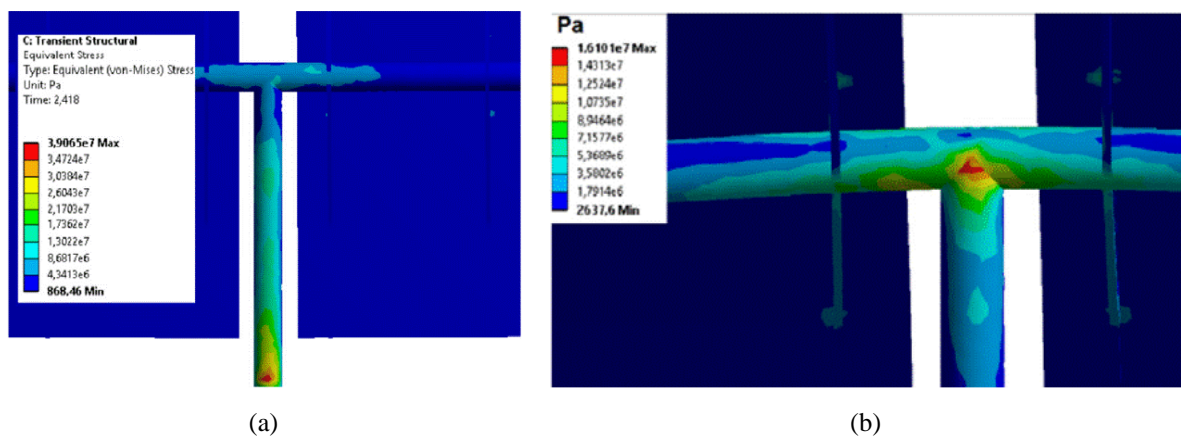


672 Figure 18. Heliostat deformed shape for torque tube bending mode 3: (a) FEA simulation of displacement contours  
 673 with modal frequency of 3.002 Hz, and (b) experimental hammer excitation test with modal frequency of 3.034  
 674 Hz. Adapted from Menicucci *et al.* (2012). The red lines represent the deformed experimental mode shape of the  
 675 five columns from the undeformed reference geometry, the yellow box represents the instrumented facet, and the  
 676 green line represents the yoke with measurement locations at the endpoints.

677 Vázquez-Arango *et al.* (2015) validated a finite element analysis (FEA) model with hammer-excited  
 678 experimental modal data, which showed that the shapes of vibration corresponding to rigid body modes  
 679 of the mirror frame, such as the oscillation about the elevation axis, were excited by fluctuating wind  
 680 loads. Admittance functions were applied using spectral analysis of the transient velocity, load and  
 681 displacements following a normal distribution to predict peak values and standard deviations of  
 682 moments about principal axes of mirror frame and displacements in the normal direction of the mirror  
 683 surface. Structural failure through overstressing was evaluated by estimating the maximum stresses on  
 684 support structure components, such that the maximum displacements due to the dynamic response were  
 685 calculated to be less than 1% of the heliostat chord length (Vasquez Arango *et al.* 2017).

686 Dynamic wind loads on heliostats have been investigated by fluid-structure interaction (FSI),  
 687 combining transient CFD, FEA simulations and modal analysis to link the resolved flow field with the  
 688 structural response. A FSI analysis by Vasquez Arango *et al.* (2017) showed a pronounced peak at  $f =$   
 689 3.8 Hz in the spectral distribution of the overturning moment coefficients on a 2.5 m  $\times$  3.22 m heliostat  
 690 model. In comparison, spectral analysis of the fluctuating azimuth and overturning moments on a 0.8  
 691 m square heliostat model by Emes *et al.* (2020b) in a boundary layer wind tunnel experiment showed a  
 692 clearly defined peak at  $f = 7$  Hz. Wolmarans and Craig (2019) performed a one-way FSI modal

693 analysis with scale resolving CFD simulation of a full-scale heliostat to determine the location of  
 694 maximum stress at two elevation angles. As shown in Figure 19(a), the maximum von Mises stress  
 695 occurred near the base of the LH-2 heliostat on the back face of the pylon. The dynamic behaviour  
 696 consisted of back-and-forth motion of the concentrator due to the large bending moment caused by the  
 697 maximum frontal area to the oncoming wind at  $\alpha = 90^\circ$ . In contrast, the maximum induced stress  
 698 decreased and was located at the T-joint between the torque tube and the pylon at  $\alpha = 30^\circ$  in Figure  
 699 19(b). Spectral analysis of the fluctuating stresses indicated dominant frequencies in the 6 Hz range  
 700 corresponding to the modal frequencies, with increasing side-to-side and flexural motions of the  
 701 concentrator at  $\alpha = 30^\circ$  caused by the peak hinge moment about the torque tube. Although coupled or  
 702 two-way FSI using LES is a promising method to investigate dynamic wind loads on heliostats, the  
 703 computational effort with increased accuracy models is very high (Pfahl *et al.* 2017a; Wolmarans and  
 704 Craig 2019). Consideration of the dynamic amplification of the load fluctuations on the heliostat  
 705 components requires further investigation to understand the conditions that promote the coupling effects  
 706 between ABL turbulence and modal frequencies of the structure.



707 Figure 19. Maximum von Mises stress contour from a one-way FSI modal analysis of the LH-2 heliostat at (a)  
 708  $\alpha = 90^\circ$ , and (b)  $\alpha = 30^\circ$  (Wolmarans and Craig 2019).

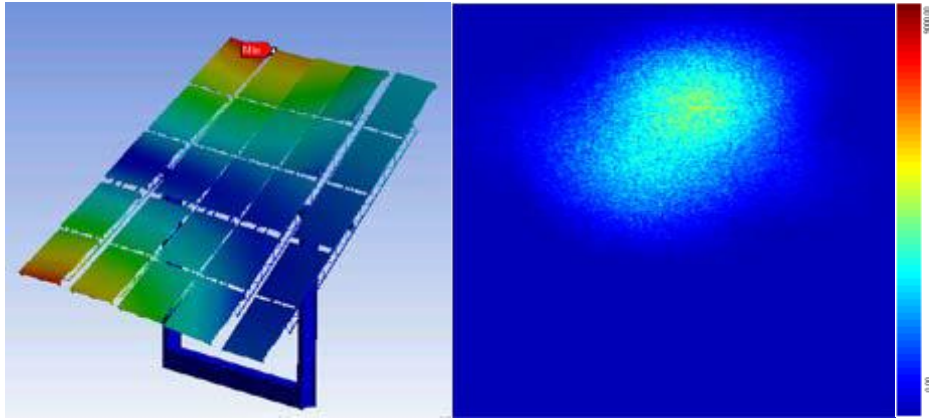
709 **4.3. Wind-induced tracking error and operational performance**

710 Ho *et al.* (2012) investigated two rigid-body vibrational modes at 1-2 Hz of the 37 m<sup>2</sup> NSTTF  
 711 heliostat correlating to backlash of the elevation and azimuth drives in a field experiment test at Sandia  
 712 National Laboratories (Ho *et al.* 2012; Griffith *et al.* 2015). Furthermore, hammer-excited experimental  
 713 modal analysis showed that the truss member to torque tube interfaces due to out-of-plane bending



714 modes (Figure 20) were most vulnerable to wind-induced stresses. Maximum beam deviations of 0.17  
715 m and 1.58 m in the horizontal and vertical directions were observed on the tower target, compared  
716 with deviations of 0.1 m and 0.25 m due to gravity in the absence of wind (Ho *et al.* 2012).

717



718

719 Figure 20. Heliostat deformed shape for out-of-plane bending mode 2 due to wind excitation that can impact  
720 optical performance through deviation of the beam centroid (Ho *et al.* 2012).

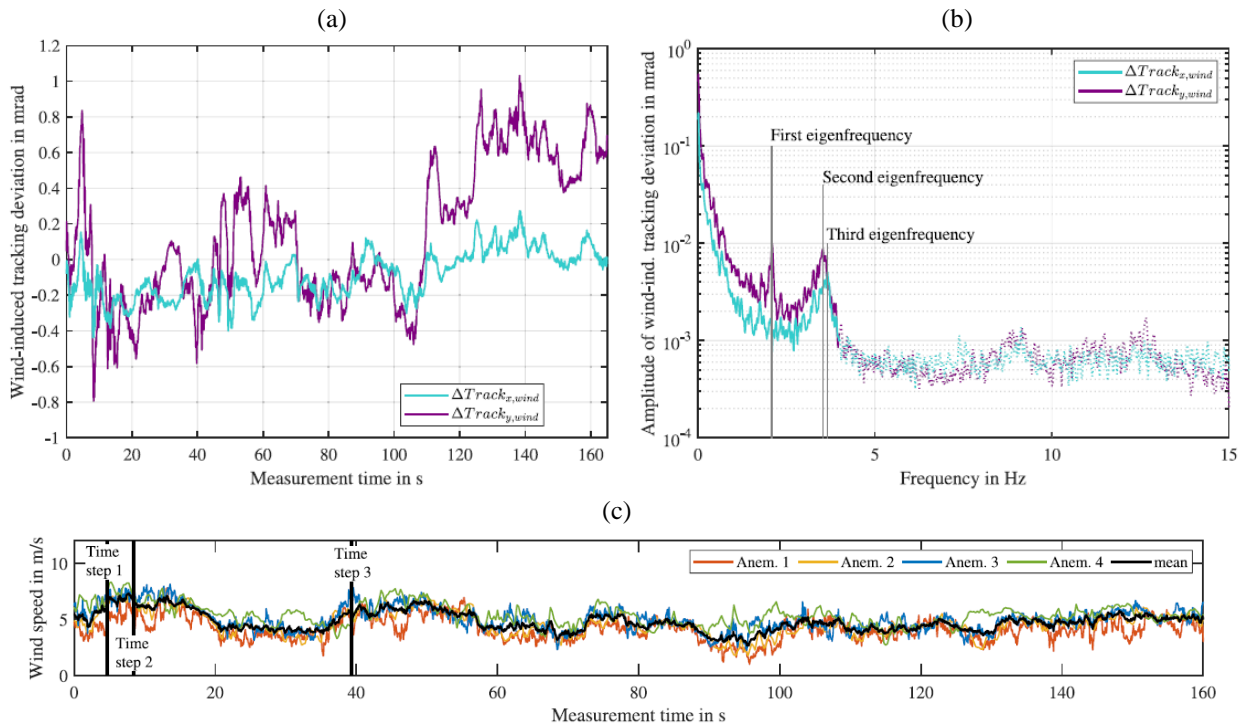
721 Dynamic photogrammetry measurements on the 48.5 m<sup>2</sup> Stellio heliostat by Blume *et al.* (2020)  
722 revealed that the wind-induced tracking deviation of 0.44 mrad RMS (Figure 21a) contained a resonant  
723 component RMS value an order of magnitude smaller than the combined RMS values of the mean and  
724 background components. This tracking deviation caused by the wind contributed to approximately one  
725 third of the typical total tracking deviation of heliostats. Wind-induced oscillations and deformations at  
726 frequencies below 4 Hz in the amplitude spectra (Figure 21b) most significantly impacted the optical  
727 performance of the heliostat at a mean wind speed of 4.8 m/s and turbulence intensity of 26% (Figure  
728 21c). To complement the relationships between quasi-static peak wind loads and ABL turbulence in  
729 Section 2, spectral analysis correlations between the fluctuating components of the wind velocity and  
730 the resonant component of the tracking deviations in field investigations would provide a further insight  
731 into the wind-induced oscillations that impact the operational performance of a range of full-scale  
732 heliostat prototypes.

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740 Figure 21. (a) Time history of the wind-induced tracking deviation in the lateral ( $x$ ) and longitudinal ( $y$ ) directions  
 741 of the Stello heliostat concentrator at  $\alpha = 45^\circ$  and  $\beta = 76^\circ$ ; (b) amplitude spectra of the wind-induced tracking  
 742 deviations with a low-pass filter and cut-off frequency of 4 Hz; (c) time history of wind speed averaged over four  
 743 ultrasonic anemometers on measurement mast at the Jülich DLR field site (Blume *et al.* 2020).

## 744 5. Aerodynamics of a heliostat field

745 Heliostat fields are arranged in rows in a radial (Figure 22a) or polar (Figure 22b) configuration  
 746 surrounding a central tower. For an optimum optical performance, the radial distance between the rows  
 747 in a heliostat field typically ranges between a value larger than the chord length of the mirror panel,  
 748  $x/c > 1$  in the inner field rows, to  $x/c=8$  at the perimeter of the field(Hui 2011). Heliostats close to the  
 749 tower have field densities greater than 40% with smaller shading effects and are typically spaced less  
 750 than 20 m apart for a typical heliostat mirror area of 120 m<sup>2</sup> (Noone *et al.* 2012). With increasing  
 751 distance from the central tower, the field density decreases to less than 20% and spacing between  
 752 heliostats of up to 45 m at the outer boundary of the field (Pfahl *et al.* 2011c; Noone *et al.* 2012). The  
 753 layout of heliostat fields in power tower plants has been optimised disregarding of wind load and  
 754 primarily with respect to the optical efficiency of the field. However, static wind loads on tandem  
 755 heliostats are strongly dependent on the spacing between the heliostat mirrors, defined by the gap ratio  
 756  $x/c$  and the heliostat field density defined as the ratio of mirror area to land area. As wind flows over a  
 757 heliostat, a region of disturbed flow is created downstream in its wake. Within the field, the mean flow

758 and turbulence characteristics might be significantly different from the incoming ABL and thus alter  
759 the wind loads on heliostats in the field from those on a single heliostat. Hence, wind loads on heliostats  
760 at different in-field positions could be evaluated given knowledge of differences in flow and turbulence  
761 characteristics within a field. This provides a chance to optimise the design and cost of a heliostat field,  
762 with respect to the inner flow field aerodynamics represented by a combination of ABL turbulence and  
763 upstream heliostat wake-generated turbulence.



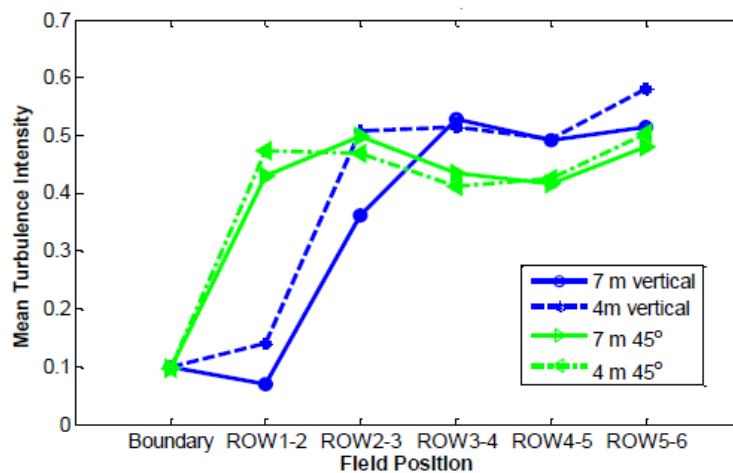
764 Figure 22. Different layouts of a heliostat field. (a) A radial heliostat field, Noor III in Morocco. Image from  
765 [www.masen.ma](http://www.masen.ma), (b) a polar heliostat field, PS10 in Spain. Image from [www.eusolaris.eu](http://www.eusolaris.eu).

### 766 5.1. Heliostat wake measurements

767 Flow around a heliostat, in the absence of the support structure and the pylon, is resembled by flow  
768 around a thin flat plate. As flow passes around a thin flat plate, it separates from the plate at its edges  
769 and a low-pressure region is formed in its immediate downstream. The separated shear layers then roll  
770 up into large scale vortices shedding into the wake. Blockage of the flow by the plate and vortex  
771 shedding in the wake lead to a reduction of mean velocity and an increase in turbulence intensity. The  
772 alternate shedding of the rolled-up shear layers into the wake creates oscillations in the flow,  
773 characterised by the dominant frequency of vortex shedding. The aerodynamics of multiple heliostats  
774 differ from a single heliostat due to the interference of their wakes with each other and the interaction  
775 of the downstream heliostats depending on their arrangement and spacing between them.

776 The profiles of mean velocity and turbulence intensity of the approaching boundary layer were  
777 characterised by Sment and Ho (2014) using three tri-axial ultrasonic anemometers mounted on a  
778 weather tower upstream of a row of instrumented heliostats. Anemometers were also mounted on the  
779 heliostats and on portable towers between five rows of the NSTTF heliostat field to measure of the

780 turbulence statistics of the flow in the vicinity of the heliostats. Figure 23 shows that an increase of  
 781 turbulence intensity to more than 50% downstream of the first and second row of heliostats at  $\alpha = 90^\circ$   
 782 (vertical) and  $45^\circ$ . For the heliostats in stow (not shown) however, turbulence intensities showed only  
 783 a small variation in downstream rows and remained below the maximum turbulence intensity of 20%  
 784 approaching the outer row of the field (Sment and Ho 2014).



785  
 786 Figure 23. Turbulence intensity in different rows of a heliostat field as a function of heliostat elevation angle.  
 787 Sment and Ho (2014).

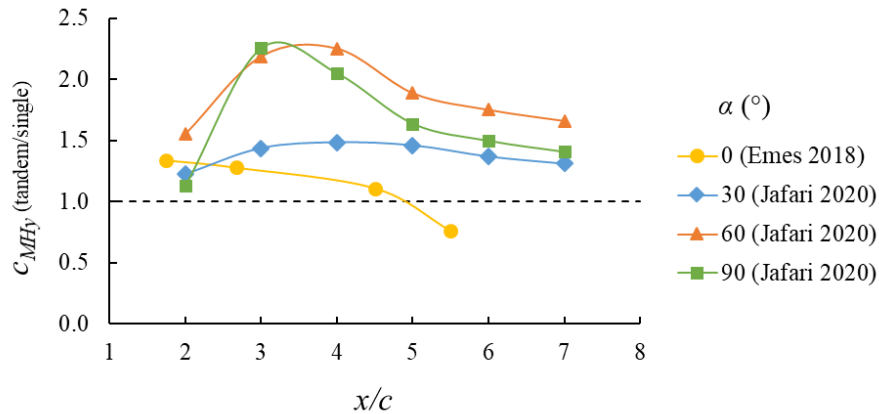
788 Within the boundary layer, the variable shear and turbulence in affect the development of the wake  
 789 of a heliostat and the turbulence structure in its wake significantly. Jafari *et al.* (2020a) conducted  
 790 velocity measurements in the wake of a heliostat model placed in simulated atmospheric boundary  
 791 layers in the wind tunnel to characterise the turbulence variations in the heliostat wake. It was found  
 792 that in the wake of a heliostat, the turbulence properties were significantly different from the  
 793 atmospheric boundary layer. The results showed a reduction in mean velocity in the wake, which did  
 794 not recover over the measured downstream distance up to  $x/c = 8$ . This was accompanied by an  
 795 increase in turbulence intensity up to  $x/c = 4$ , with a peak at approximately  $x/c = 1.5$  where the  
 796 streamwise and vertical turbulence intensities increased by more than 12-times their incoming values  
 797 at elevation angles of  $60^\circ$  and  $90^\circ$ . Furthermore, it was found that in the wake immediately downstream  
 798 of the heliostat, the length scales of turbulence were significantly smaller as the large inflow turbulence  
 799 length scales were broken into smaller scales.

800 The variations of turbulence intensity in the heliostat wake at different streamwise distances  
801 indicates the impact of field density on heliostat wind loads. For example, due to the higher turbulence  
802 intensity caused by the heliostat wake, the unsteady wind loads in high-density zones of a heliostat field  
803 at  $x/c = 1 - 3$  are greater than in low-density zones. This shows the impact of dynamic wind loads for  
804 design of heliostats as they are likely to influence the dominant frequencies of the unsteady and dynamic  
805 loads on heliostats in dense zones of a field. Furthermore, despite the reduced mean wind speed within  
806 the field, static wind loads such as the hinge moment may increase within the field depending on the  
807 field density and the elevation angle of heliostats during operation.

## 808 5.2. Loads in heliostat field arrays

809 The review of the aerodynamics of tandem flat plates and side-by-side flat plates shows that the  
810 wake flow around multiple heliostats and thus the wind loads on in-field heliostats can differ from those  
811 on a single heliostat. One of the critical parameters that influences the wind loads is the non-dimensional  
812 gap in the longitudinal direction with respect to the mirror chord length,  $x/c$ , between the heliostats in  
813 an array. Emes *et al.* (2018) investigated the variation of the stow wind loads on two tandem heliostats  
814 and showed that the peak lift force coefficient on the second tandem heliostat in stow was up to 7%  
815 larger than that for the single stowed heliostat for  $x/c > 1.5$ . As shown in Figure 24, Jafari *et al.* (2020b)  
816 found that the peak hinge moment coefficient on a tandem heliostat increased to 1.5-times that on a  
817 single heliostat at elevation angles of  $30^\circ$  and more than double at elevation angles of  $60^\circ$  and  $90^\circ$ .  
818 Despite the lower mean pressure coefficient on the tandem heliostat, a region of large-magnitude peak  
819 pressure existed at the leading edge of the panel. Furthermore, analysis of the unsteady pressure  
820 distributions showed an increased unsteady centre of pressure variation on the second tandem heliostat,  
821 specifically at elevation angles of  $30^\circ$  and  $60^\circ$ . The unsteady variations of the position of the centre of  
822 pressure as a result of the larger turbulence intensity in the wake were found increase the mean and peak  
823 hinge moment coefficients on the second heliostat. The large increase of the hinge moment coefficient  
824 can outweigh the reduced wind speed in the wake with respect to the gap between the heliostats and the  
825 elevation angle of the heliostat panel. For example, at an elevation angle of  $30^\circ$  and  $x/c$  between 4 to  
826 8, the mean wind speed reduced by less than 10%, while the hinge moment coefficient was 50% larger

827 than the single heliostat, leading to an increase of between 20% and 50% in the peak hinge moment.  
 828 Hence, the results highlight an opportunity to modify the heliostat design for in-field heliostats  
 829 compared to field-edge heliostats.

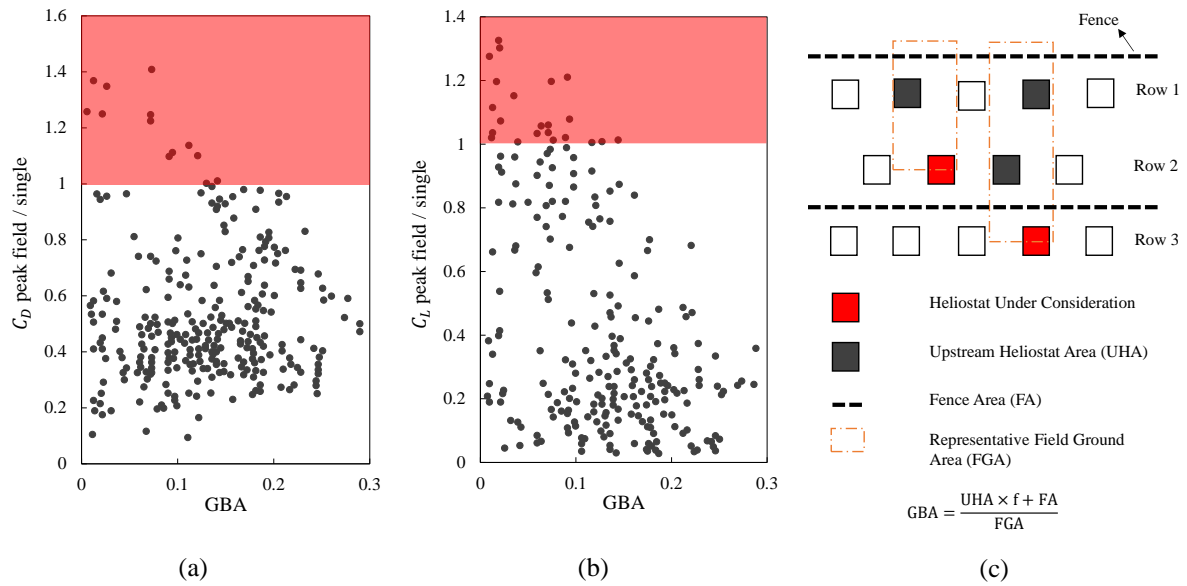


830 Figure 24. Peak hinge moment coefficient on a tandem heliostat normalised to a single heliostat as a function of  
 831 longitudinal gap spacing  $x/c$  between tandem heliostats at elevation angle  $\alpha$  (Emes *et al.* 2018; Jafari *et al.*  
 832 2020b).  
 833

834 In the literature, wind tunnel studies have been performed to study the influence of fences on the  
 835 wind loads on heliostats in field arrangements. . Peterka *et al.* (1986) measured the wind loads on a  
 836 heliostat placed in an array with perimeter and in-field fences. The configuration of the heliostat array  
 837 was chosen based on different regions of a field with different densities. Fences with porosities of 0.4,  
 838 0.5 and 0.6 and two heights, equal to 0.9 and 1.35 times the heliostat hinge height, were investigated.  
 839 They found that with addition of the fence, the mean drag force coefficient on a heliostat at  $\alpha = 90^\circ$  and  
 840 a wind direction of  $250^\circ$  in the third row of an array was reduced from approximately 1 to 0.45. The  
 841 results in Figure 25(c) were presented as a function of generalised blockage area (GBA), defined as the  
 842 ratio of the area of upstream blockage projected to wind direction, including external and internal fences  
 843 and upstream heliostats, over the field ground area. Peterka *et al.* (1989) reports the ratio of the peak  
 844 drag and lift force coefficients in a field as a function of GBA as shown in Figure 25(a–b). The results  
 845 show cases where the peak coefficients are larger than a single heliostat, shaded by red in Figure 25(a–  
 846 b). The reason for increase of wind loads was not explained by Peterka *et al.* (1986). Furthermore, the  
 847 elevation angles and heliostat configurations for the presented results were not provided, and it is not  
 848 clear for which conditions the wind loads were larger than a single heliostat. Moreover, the results were

849 only presented as a function of GBA, which includes the effects of both the fence and blockage by  
850 upstream heliostats. Hence, the influence of the fence on the wind loads was not distinguished.

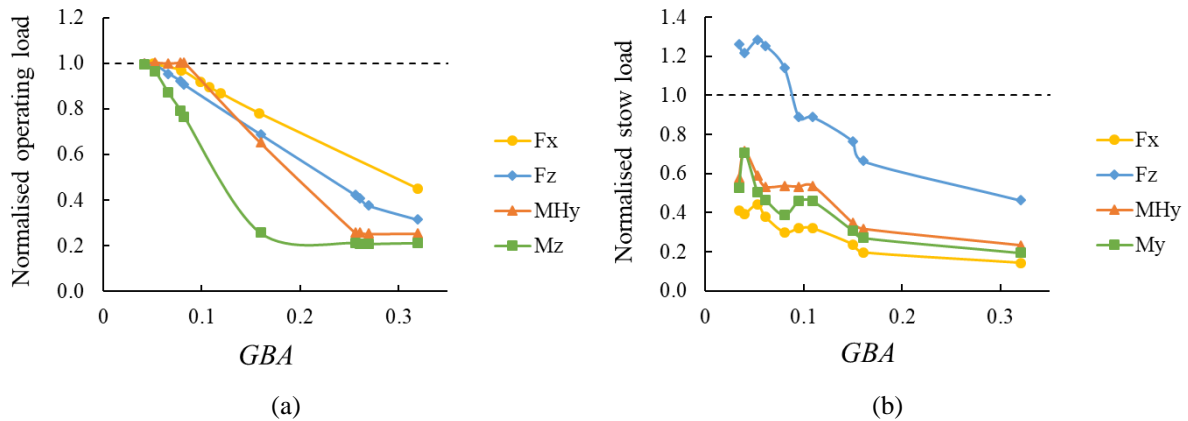
851 Peterka *et al.* (1987) measured the wind loads on 1:60 scale-model heliostats in the fourth row of a  
852 four-row arrangement for two different gap ratios between consecutive rows,  $x/c = 6.4$  and  $x/c = 3.07$ ,  
853 representing low- and high-density zones of a heliostat field. The mean drag force coefficient of a  
854 fourth-row heliostat was found to be 12% lower than that of a front-row heliostat at  $x/c = 3.07$ . For a  
855 higher field density, the reduction in the mean drag coefficient increased to only 32% of that in the first  
856 row. In contrast, the peak drag force coefficient on of a fourth-row heliostat with  $x/c = 6.4$  was found  
857 to be 40% larger than that of a front-row heliostat. Pfahl *et al.* (2011c) measured the wind loads on 1:20  
858 scale-models of a four-row tandem arrangement with 30 m<sup>2</sup> mirror area for field densities of 10% and  
859 50% corresponding to gap ratios ( $x/c$ ) between the mirrors of 5.5 and 1.5, respectively. Peterka *et al.*  
860 (1987) and Pfahl *et al.* (2011c) found up to 50% reduction in peak drag and lift forces on a second  
861 heliostat at  $\alpha = 90^\circ$  compared to the front-row heliostat in a tandem arrangement at a field density of  
862 50%. The larger peak drag coefficient may be correlated with an increase in longitudinal turbulence  
863 intensity of the flow, however the relative contribution of the longitudinal and vertical turbulence  
864 components to the lift and hinge moment coefficients on operating heliostats has not been determined.  
865 This highlights the importance of characterisation of turbulence in the wake of heliostats and its effect  
866 on the wind loads, and measurement of wind loads in a field. Understanding the variations of wind  
867 loads within a heliostat field can help to improve the field design with respect to the wind loads. For  
868 regions of a field with reduced wind speed and increased turbulence intensity, the structural stiffness  
869 and foundation depth of heliostats can be decreased if the dynamic loads are not overcompensated by  
870 an increase in unsteady wind loads.



871 Figure 25. (a) Peak drag and (b) peak lift force coefficients in an array with perimeter and in-field fences  
 872 normalised with the peak force coefficients on a single heliostat as a function of generalised blockage area, GBA.  
 873 The red shaded regions show cases where the peak wind load coefficients are larger compared to a single heliostat.  
 874 (c) A schematic of the heliostat array demonstrating the calculation of GBA. Reproduced from Peterka *et al.*  
 875 (1989).

876 In a similar experiment, Pfahl (2018) measured the wind loads on a heliostat in the fourth row of  
 877 an array in presence of a fence upstream of the first row. The fence had a porosity of 40% and height  
 878 equal to 1.25 times the heliostat hinge height. Different cases with varied distances between the heliostat  
 879 rows and between the fence and the front row were investigated, through which GBA varied between  
 880 0.053 and 0.46. Their results in general showed that the maximum wind load coefficients at operating  
 881 elevation angles were less than a single heliostat for the investigated range of GBA. As shown in Figure  
 882 26, the peak lift force coefficient on a stowed heliostat was up to 25% larger than a single heliostat for  
 883 GBA values less than 0.1. The increase in the stow lift force coefficient was suggested to be related to  
 884 an increase in vertical velocity component downstream of the fence. If the entire field is to have a  
 885 consistent heliostat design, according to Pfahl (2018), application of fences therefore may not be  
 886 beneficial due to the increase of the lift force in stow position and the negligible impact of the fence on  
 887 low density regions of the field. As the results were presented as a function of GBA, the effect of fence  
 888 was not differentiated from the effect of blockage by heliostats at the upstream rows. Pfahl (2018)  
 889 discussed that the uncertainty in the reported results was large due to the limited measurement cases.





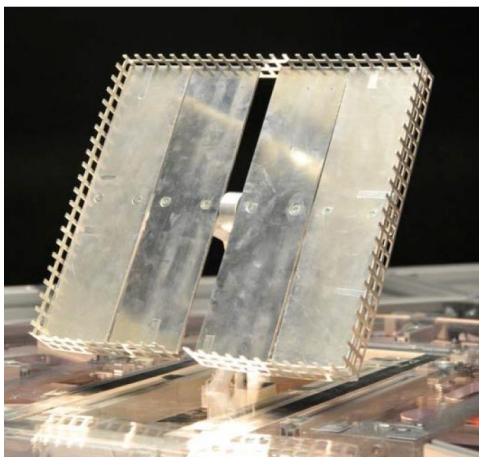
890 Figure 26. Peak aerodynamic coefficients as a function of GBA, normalised with respect to  $GBA = 0$  for an  
 891 isolated heliostat in (a) maximum operating position (Peterka and Derickson 1992); (b) stow position (Pfahl 2018).

892 5.3. Wind load mitigation techniques

893 The wind load reduction on in-field heliostats in wind tunnel experiments by Peterka *et al.* (1986)  
 894 and Pfahl (2018) compared to a single heliostat were presented as a function of GBA, such that the  
 895 effects of both the fence and blockage by upstream heliostats were not distinguished. Hence, the  
 896 manipulation of inflow ABL turbulence by the fence and its effectiveness in wind load reduction were  
 897 not reported. Turbulence properties downstream of mesh fences (Figure 27b) of various mesh opening  
 898 widths and porosities were determined from experimental measurements in a wind tunnel (Jafari *et al.*  
 899 2021). It was found that with application of fences with porosities between 0.46 and 0.75, an inflow  
 900 streamwise turbulence intensity of 12.5% could be reduced to between 8.8% and 9.9%. Furthermore, a  
 901 significant reduction in the integral length scale of turbulence was shown immediately downstream of  
 902 the fences and grew afterwards with increasing the downstream distance, with the longitudinal length  
 903 scale remaining 25% and the vertical length scale remaining 21% below the inflow level for the fences  
 904 with porosities between 0.46 and 0.64. Through comparison of the turbulence reduction behind wire  
 905 mesh fences with different porosities and mesh opening widths, it was found that porosity was the main  
 906 factor which determined the reduction in turbulence intensity and length scales. Based on the variation  
 907 of mean velocity, turbulence intensity and integral length scale behind the fences, it was estimated that  
 908 the peak drag force on a heliostat at the vertical position could be reduced by 48% with utilisation of a  
 909 wire mesh fence with a porosity of 0.46 using the developed relationships in Jafari *et al.* (2018). it was  
 910 predicted that the peak lift force on a stowed heliostat could be reduced by 53% behind a wire mesh

911 fence with a porosity of 0.46 based on the correlation given in Jafari *et al.* (2019a), as shown in Figure  
912 27(b). With increasing the porosity of the wire mesh fence to 0.75, the reduction in peak drag and lift  
913 forces could only reach 19% and 15%, respectively. The measurement of forces on a heliostat behind  
914 the fence can further verify these estimated peak load reductions derived from the turbulence intensities  
915 and length scales reductions due to the fence. For such a method to be employed in a heliostat field,  
916 further study is necessary in the future. to determine the optimum geometric parameters of the mesh  
917 fence, including its height and distance to the heliostats.

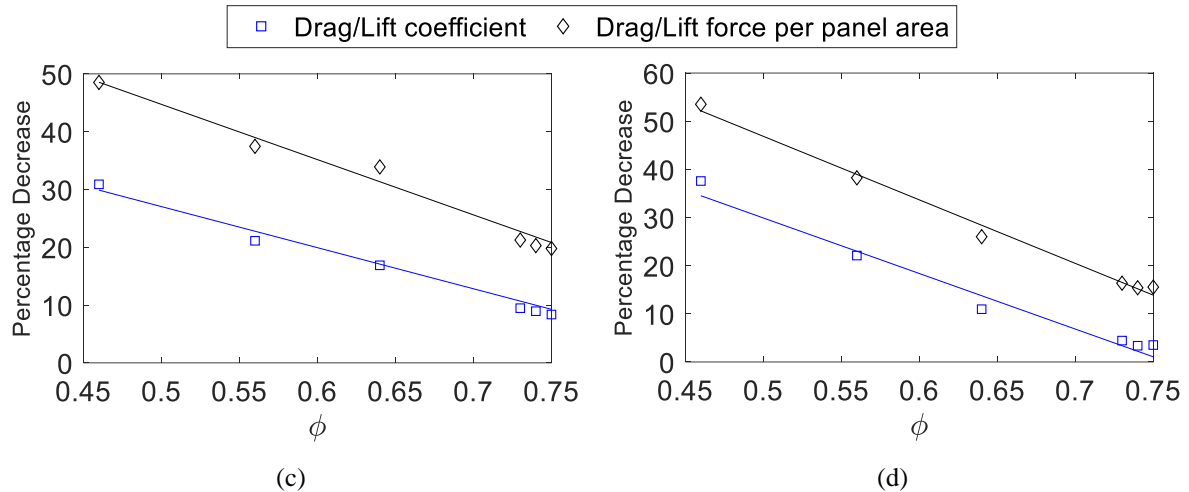
918 Wind load reduction by fences may be more appropriate for heliostats of smaller dimensions, due  
919 to the increased material cost of larger fences that would be required for a field of large-scale heliostats.  
920 Although fences at the perimeter of the field have been shown to have negligible impact on the forces  
921 on heliostats with increasing distance into the field, a modification in the design of perimeter fences to  
922 heliostat edge-mounted devices may reduce the wind loads on in-field heliostats. The high overturning  
923 moments on a stowed heliostat are due to the vertical velocity component of the turbulent flow  
924 separating at the leading edge, which creates suction on the other side of the mirror and a high-pressure  
925 difference between the upper and lower heliostat surfaces. Wind tunnel experiments by ToughTrough  
926 indicated that fence-like “spoilers” (Figure 27a) can reduce separation and suction near the leading edge  
927 in stow position, leading to 40% wind load reduction and 30% weight reduction of heliostat support  
928 structure (Pfahl *et al.* 2014b). A disadvantage of such flow manipulator devices is the additional  
929 maintenance cost to clean the mirrors and the shading of the mirrors.



(a)



(b)



930 Figure 27. Wind load mitigation techniques using (a) heliostat edge-treatment devices (Pfahl *et al.* 2013), and (b)  
 931 a heliostat field perimeter porous wire mesh fence (Jafari *et al.* 2021). The plots show the effect of wire mesh  
 932 fence porosity on the predicted reduction of (c) the peak drag force/coefficient on a heliostat at  $\alpha = 90^\circ$ , (d) the  
 933 peak lift force/coefficient on a heliostat at  $\alpha = 0^\circ$  (Jafari *et al.* 2021).

## 934 6. Discussion

### 935 6.1. Resolution of heliostat field measurements in plant performance models

936 Typical meteorological year (TMY) data contains wind and solar radiation data averaged over a  
 937 duration of one hour as an input to annual solar field efficiency models. In practice during operation of  
 938 a power tower field, however, heliostats are stowed based on a 3-second gust wind speed (Price *et al.*  
 939 2020). Second-generation heliostats were defined by Murphy (1980) with specifications for gust wind  
 940 speeds of 22 m/s and 40 m/s at a 10-m height for the maximum operational and stow survival design  
 941 conditions, respectively. This is the same as the 3-second gust wind speed stated in design wind  
 942 guidelines and norms for buildings and other physical structures with natural frequencies smaller than  
 943 1 Hz at a height of 10 metres. Standard wind velocity data at automatic weather stations (Bureau of  
 944 Meteorology 2020; National Climatic Data Center 2020) are not obtained at a sufficient frequency to  
 945 reliably determine the longitudinal and vertical turbulence intensities that impact the maximum heliostat  
 946 wind loads (Blackmon 2014). Long-span cable-supported bridges are sensitive to peak gusts of a  
 947 duration of the order of 2-3 seconds (Xu 2013), whereas stowed heliostats are exposed to shorter  
 948 duration gusts of approximately 1 second (Pfahl 2018). Hence, it is expected that the relevant gust  
 949 period for a heliostat is shorter than that of a building and thus the dynamic response and vibrational

950 mode shapes of heliostats are different. The collection of high frequency (i.e. second) wind velocity and  
951 solar radiation data at concentrating solar power plant sites over an extended duration (e.g. years) would  
952 increase the accuracy of annual field efficiency models through an improved resolution of operating  
953 load data. The transient nature of the ABL should therefore be accounted for in the design of a heliostat  
954 field, including the wind load predictions and the assessment of operational performance models.

## 955 6.2. *Assessment of critical aerodynamic load cases of a heliostat*

956 Design wind load codes and standards provide aerodynamic shape factors, external pressure  
957 coefficient and design external pressure, aerodynamic (drag) force coefficient  $c_F$  and the centre of  
958 pressure distance  $l_{px}/c$  from the windward edge of simple-shaped structures based on a characteristic  
959 length  $c$  of the structure. For example, *Chapter 5 - Wind Loads* of ASCE 7-02 (2002) provides a range  
960 of tables containing the design pressures for solid freestanding walls, solid signs and monoslope roofs  
961 with tilt angles 10-30° (in increments of 5°) and aspect ratio of the cross-sectional roof area varying  
962 between 1/5 and 5. Furthermore, the IEC 61400-1 (2005) wind turbine design standard provides  
963 guidance on the static and dynamic loads on wind turbine components, considering the effects of  
964 turbulence intensity and length scales and the variation of average and gust wind speeds across the rotor  
965 plane. However, heliostats have a non-standard shape that does not conform to conventional shapes of  
966 buildings (ASCE 7-02 2002; EN 1991-1.4 2010; AS/NZS 1170.2 2011) and rooftop solar panels  
967 (ASCE/SEI 7-16 2016) associated with corner vortices and separation at the leading edge of the building  
968 roof (Kopp *et al.* 2012). The thin plate and tubular geometries of heliostat facets, support beams, torque  
969 tube and pedestal are not applicable to the design procedures outlined for buildings and wind turbines  
970 in terms of their size, shape and position within the lowest 10 m of the ABL. This can lead to under-  
971 estimation of the peak loads on heliostats, such as in stow position due to the large dynamic response  
972 caused by near-surface gust events (Durst 1960; Mendis *et al.* 2007).

973 Table 2 shows the maximum operating wind load configurations, in terms of the elevation and  
974 azimuth angles that result in the peak wind load coefficients reported in wind tunnel measurements in  
975 Table 1 (refer to Section 2.2). For wind approaching an upright heliostat at  $\alpha = 90^\circ$  from the front

976 ( $\beta = 0^\circ$ ) or back ( $\beta = 180^\circ$ ), the maximum drag force  $F_x$  on the concentrator leads to the maximum  
977 overturning moment  $M_y$  at the base of the heliostat pylon for design of the foundation. Similarly, on a  
978 heliostat inclined at  $\alpha = 30^\circ$ , the maximum lift force on the heliostat panel leads to a maximum hinge  
979 moment  $M_{Hy}$  about the elevation axis of the heliostat in operation that impacts the design of the torque  
980 tube and elevation drive. The maximum load case for the azimuth drive is the moment about the vertical  
981 axis of an upright operating heliostat ( $\alpha = 90^\circ$ ) with wind approaching from an oblique angle  $\beta = 60^\circ$   
982 and  $120^\circ$ . The wind load coefficients found by Peterka *et al.* (1989) apply to one case of the ABL with  
983 limited information on the turbulence spectra and length scales, particularly in the vertical turbulence  
984 component that is crucial to the maximum wind loads in stow position. The maximum wind loads on  
985 heliostats often considered wind impacting the front of the heliostat at  $\beta = 0^\circ$ , however the maximum  
986 wind loads on a heliostat at  $\beta = 180^\circ$  can be larger and the presence of an upstream heliostat influences  
987 the spectral peak of pressure variations in operating positions. (Yu *et al.* 2019). The number of working  
988 conditions for azimuth-elevation heliostat configurations can be reduced from 130 to 13 through the  
989 application of uniform design method and regression analysis to all wind load coefficients (Xiong *et al.*  
990 2019). The contribution of spectral energy in the turbulent eddies to wind loads and the resulting  
991 aerodynamic effects on heliostat geometry over a larger range of orientations has been investigated in  
992 more detail in recent wind tunnel experiments (Pfahl *et al.* 2015; Emes *et al.* 2017; Emes *et al.* 2019a;  
993 Jafari *et al.* 2019a).

994 Table 2. Critical operating load cases of an azimuth-elevation heliostat.

Maximum aerodynamic coefficient	$\alpha$ ( $^\circ$ )	$\beta$ ( $^\circ$ )
$F_x, M_y$	90	0, 180
$F_z, M_{Hy}$	30	0, 180
$M_z$	90	60, 120

995 Prediction of the design loads on heliostats should allow for the maximum operating cases and stow  
996 cases, due to both the scaling parameters of individual components and the level of ABL turbulence  
997 represented by the surrounding terrain. The influence of the heliostat concentrator aspect ratio (Pfahl *et al.*  
998 *et al.* 2011a) and the pylon height (Emes *et al.* 2017; Jafari *et al.* 2019a) have a large effect on the  
999 maximum aerodynamic coefficients, whereas small gaps between mirror facets have a negligible impact

1000 on the pressure distribution and the wind loads (Wu *et al.* 2010). Structural reliability of the heliostat  
1001 components through stress analysis by (Benammar and Tee 2019) suggested that the thickness of the  
1002 pedestal and torque tube can be reduced for operating conditions at low wind speed sites, whereas the  
1003 torque tube is a critical component that can lead to structural failure in stow position at increased wind  
1004 speeds. Wind tunnel experiments have shown that for measurement of the unsteady drag force on a  
1005 heliostat at  $\alpha = 90^\circ$ , similarity of the streamwise velocity spectrum is required and a model with larger  
1006 dimensions (i.e. smaller scaling ratio) can be used. In contrast, accurate measurement of the unsteady  
1007 lift force on a stowed heliostat requires similarity of the vertical turbulence spectrum, which can only  
1008 be achieved for a model with smaller dimensions or larger scaling ratio (Jafari *et al.* 2019b). The relative  
1009 contribution of the longitudinal and vertical components of turbulence, for a stowed heliostat and over  
1010 the range of heliostat operating conditions with varying gap between the lower heliostat edge and the  
1011 ground, should be further verified through wind tunnel and full-scale measurements. Analysis of wind  
1012 loads on full-scale heliostats with respect to the incoming wind turbulence measured simultaneously  
1013 can verify the scaling effects observed in wind tunnel experiments to provide a more reliable estimation  
1014 of wind loads.

### 1015 6.3. *Modal analysis of heliostat vibrations and wind-induced displacements*

1016 Measurements of local deformations and displacements on full-scale heliostats have provided an  
1017 insight into the dynamic wind loads, such as vibrations and fatigue loads on drive units and support  
1018 structure components. Modal analyses have been conducted in the literature both computationally and  
1019 experimentally to determine the mode shapes and frequencies of a heliostat structure. Low-frequency  
1020 vibrational modes corresponding to quasi-static sway motion of the heliostat subjected to time-averaged  
1021 loads can be accurately reproduced by numerical simulations. However, modes that are dependent on  
1022 the stiffness and damping of joints, such as elevation and azimuth drives, are most accurately  
1023 characterised through full-scale experiments and two-way fluid-structure interaction that captures the  
1024 gust spectrum range ( $\sim 1$ -2 Hz) of the fluctuating load distribution caused by backlash or slop in the gear  
1025 drives (Griffith *et al.* 2012; Ho *et al.* 2012). High-amplitude dynamic response of the pylon and support  
1026 structure was less likely to be impacted by the shedding of vortices from the heliostat structure

1027 (Wolmarans and Craig 2019), although this applies to a broad range of frequencies depending on the  
1028 wind speed and the heliostat size (Ho *et al.* 2012). Hence, the heliostat structure should be designed to  
1029 avoid wind loads that cause high-amplitude or high-cycle counts in the drive components that result  
1030 from resonant effects due to convergence of the modal frequencies with the gust frequencies of energy-  
1031 containing eddies in the approaching wind and the vortex shedding frequency from upstream heliostats.  
1032 Further work is still necessary to examine dynamic wind loads on heliostats positioned inside the  
1033 heliostat field. For instance, field measurements can provide validation points to complement numerical  
1034 studies to investigate load amplification factors associated with different operational wind speeds and  
1035 turbulence characteristics over an increasing range of heliostat orientations and structural designs.

#### 1036 6.4. *Dynamic wind effects on operational heliostat tracking error*

1037 Wind engineering design standards do not account for the dynamic effects of heliostats, such as a  
1038 dynamic response or amplification factor in AS/NZS 1170.2 (2011) for slender buildings and large  
1039 permanent structures ( $H \leq 200$  m) with natural frequencies less than 1 Hz. To avoid structural excitation  
1040 due to buffeting and torsional galloping, the natural frequency of a long inclined flat plate (i.e. solar  
1041 array) is recommended to be greater than 5 Hz. Hence, the essential scaling parameters of the heliostat  
1042 structure and the aerodynamic loads on the tubular components were shown to be very sensitive to the  
1043 high turbulence in the ABL. Although square-mirrored heliostats are less likely to be exposed to  
1044 torsional vibrations, the ratio  $L^x/c$  of the integral length scales in the longitudinal and vertical directions  
1045 to the heliostat chord length significantly affects the peak wind loads on heliostats in operating and stow  
1046 positions (Emes *et al.* 2017; Jafari *et al.* 2019a). Based on the common sizes of heliostat mirrors that  
1047 are currently manufactured,  $L_u^x/c \approx 6.5$  in an open country terrain with  $z_0 = 0.03$  m (ESDU 85020  
1048 2001). However,  $L_u^x/c$  decreases with increasing surface roughness to  $L_u^x/c = 5.5$  at  $z_0 = 0.05$  m and  
1049  $L_u^x/c = 4.5$  at  $z_0 = 0.1$  m. To reduce the maximum wind loads as  $L_u^x/c$  and  $L_w^x/c$  approach unity, a  
1050 heliostat of fixed mirror chord length can be stowed at a lower elevation axis height  $H$  that is closer to  
1051 the ground (Pfahl *et al.* 2017b) through a reduction of  $H/c$  and  $L_u^x/c$ .

1052 6.5. *Variation of wind loads on heliostats throughout a field*

1053 Due to the variation in heliostat orientations across a field with respect to the wind, the aerodynamic  
1054 loads on some heliostats in favourable orientations can be reduced with respect to the maximum load  
1055 cases in the field. Statistical correlation of wind speed and DNI data with heliostat tracking angles at  
1056 the Plataforma Solar de Almeria (PSA) CESA-I field by Emes *et al.* (2020c) indicated that a stowing  
1057 strategy based on wind speed and direction can increase the annual operating time of the heliostat field  
1058 by 6% with increasing stow design wind speed from 6 m/s to 12 m/s. For an assumed 10-minute stow  
1059 transition from operating positions of the heliostat field, a stowing strategy that allowed “protected”  
1060 heliostats with reduced wind loads at  $\beta = 90 \pm 15^\circ$  to continue to operate at wind speeds larger than 10  
1061 m/s was investigated. Emes *et al.* (2020c) found to achieve an additional 280 MWh of thermal energy  
1062 collected by heliostat field operation during periods that would conventionally stow the entire field with  
1063 24 GWh of annual thermal energy captured. It is therefore apparent that there is a potential to increase  
1064 the operating performance through consideration of wind load distributions and “smart” stowing  
1065 strategies of the heliostat field to maximise the energy yield of a power tower plant.

1066 Porous fences were found by Jafari *et al.* (2021) to reduce the turbulence intensity and integral  
1067 length scales by 20-25% relative to the incoming ABL, but the material cost of perimeter fences for  
1068 large heliostats and their area of influence into a heliostat field remained a research question. Other  
1069 methods to reduce the wind loads on heliostats positioned at the inner rows of a field include the  
1070 attachment of “edge treatment” devices to the heliostat, such as to mitigate the impact of vortex  
1071 shedding from the leading and trailing edges. Alternatively, the installation of a series of slender plate  
1072 or rod large-eddy break-up (LEBU) devices at the perimeter of a heliostat field can reduce the effect of  
1073 the energetic turbulent eddies in the ABL on the heliostat field operation. Characterisation of the flow  
1074 and wind loads using these methods are required for an improved understanding of their effectiveness.  
1075 A techno-economic analysis of the cost-effectiveness of fences in heliostat fields is required to assess  
1076 the sensitivity of reduced loads and heliostat capital cost with respect to the increased land area and  
1077 material cost of the fence construction.



## 1078 **7. Conclusions**

1079 There has been an extensive range of studies on heliostat aerodynamic wind loads in the literature.  
1080 The aerodynamic coefficients form a basis for the design wind loads on isolated heliostats, which were  
1081 shown to depend on the geometric parameters of the heliostat, along with wind speed and turbulence  
1082 parameters in the atmospheric boundary layer (ABL). The following major conclusions can be drawn  
1083 from the literature to further develop the understanding of the aerodynamic wind loads on heliostats:

1084 1) In wind standards, turbulence intensity and integral length scale profiles are only given for  
1085 heights above three metres. However, there is demand for smaller heliostats as they are  
1086 advantageous for high-temperature applications, such as hydrogen production due to lower  
1087 astigmatism losses. Therefore, field investigations of the wind characteristics between one  
1088 and three metres height for typical solar sites would be beneficial.

1089 2) The maximum operational loads and the stow survival loads have been defined by the  
1090 heliostat orientation with respect to the wind. It is most important to model the range of  
1091 reduced frequencies of the turbulence spectrum that contribute to the unsteady forces on  
1092 heliostats in wind tunnel experiments in order to reduce the scaling effect on the measured  
1093 peak wind loads and accurately reproduce the wind loads on the full-scale structure. These  
1094 maximum heliostat load cases were referenced to design wind speeds and turbulence  
1095 intensities at a constant height, such as the standard reference height of 10 m in wind load  
1096 codes and standards. An increased resolution of field-scale wind measurements is essential  
1097 to understand the effect of surface roughness on the peak aerodynamic coefficients at a range  
1098 of heliostat field sites to fully characterise the longitudinal and vertical turbulence intensities  
1099 and length scales that impact the maximum wind loads for operating serviceability and stow  
1100 survivability considerations.

1101 3) Scaling factors and relationships have been derived in scale-model wind tunnel experiments  
1102 that account for the variation in wind loads due to geometry effects, such as the aspect ratio,  
1103 mirror chord length and pylon height from a baseline square-mirror azimuth-elevation  
1104 heliostat. Further investigations should focus on the influence of wind direction and heliostat

1105 shape due to changes in aspect ratio, and the effect of the gap between the lower heliostat  
1106 edge and the ground on the aerodynamic coefficients.

1107 4) Dynamic wind loads and modal analysis of local deformations of heliostat components was  
1108 most effectively investigated in field environments with the mechanical and structural  
1109 properties of a full-scale heliostat. Due to the large range of heliostat sizes and structural  
1110 types, the design wind loads are commonly estimated using a combination of peak  
1111 aerodynamic coefficients and appropriate load-response correlations from finite element  
1112 models at the relevant design wind speeds. Dynamic amplification factors for alternative  
1113 heliostat designs to a conventional azimuth-elevation tracking configuration (e.g. spinning  
1114 axis, tilt-roll) should be further investigated, such as the lowering of the mirror closer to the  
1115 ground in stow position and resonance effects in the transition to stow due to increases of  
1116 wind speed at intermediate operating angles.

1117 5) Systematic experimental studies in small-scale boundary layer wind tunnel measurements  
1118 have effectively simulated the aerodynamics and quasi-static wind loads through  
1119 investigation of the critical scaling parameters of isolated, tandem and arrays of heliostats  
1120 over a range of wind turbulence conditions in the ABL. Wind loads on the structural heliostat  
1121 components, such as bending moment reactions to be resisted by the drives, torque tube and  
1122 foundation, have been characterised through scale-model testing in wind tunnel experiments.  
1123 The variation of wind-induced displacements due to operational wind loads on in-field  
1124 heliostats has been related to the vortex shedding and vibrational modes, but simultaneous  
1125 load and wake measurements can provide understanding on how the field spacing and  
1126 orientation affects the operational performance of individual heliostats throughout the field.  
1127 Instrumenting arrays of heliostats in different rows within a field would also be highly  
1128 beneficial to better understand the relative contribution of heliostat-generated wake  
1129 turbulence and incoming ABL turbulence on the heliostat field aerodynamics, wind load  
1130 distributions and wind-induced tracking errors during operation of a field.

1131 6) It is postulated that the total cost of the heliostat field is conservative as all heliostats are  
1132 designed based on the maximum wind load coefficients on a single heliostat, while the loads

1133 on heliostats in various rows vary across the field. Heliostat wind loads in arrays have  
1134 presented wind load reductions on in-field heliostats based on the concept of GBA, however  
1135 the fence's independent effect was not distinguished from the impact of upstream heliostat  
1136 blockage. Understanding the variation of wind loads within a heliostat field through the  
1137 systematic analysis of independent wind load reduction methods can help to improve the  
1138 field design with respect to the wind loads. Characterisation of the flow and wind loads using  
1139 favourable methods to reduce heliostat wind loads, such as perimeter and in-field fences and  
1140 edge treatment devices, should independently assess their cost-effectiveness and feasibility  
1141 in power tower plants.

1142 There is a strong case for the development of design guidelines for wind load predictions on full-  
1143 scale heliostats that account for the effects of ABL turbulence based on the scaling of the heliostat  
1144 structural components and field layout. Such guidelines can benefit the operational performance of the  
1145 plant and the material costs of manufacturing based on the local wind conditions below heights of 10  
1146 metres at different sites. Accurate prediction of the maximum wind loads in real-scale operating  
1147 conditions provide greater confidence in field efficiency and power tower plant performance models,  
1148 which enhances the reliability of techno-economic analyses of the solar field operation and structural  
1149 design of the heliostat components.

## 1150 **Acknowledgements**

1151 The authors acknowledge the support from the Australian Solar Thermal Research Institute  
1152 (ASTRI) and funding provided by the Australian Renewable Energy Agency (ARENA) Grant 1-  
1153 SRI002.

## 1154 **References**

1155 Abengoa Solar (2016), Abengoa, IDC and Khi Community Trust commence commercial operation of  
1156 Khi Solar One, the first solar tower plant in Africa,  
1157 [https://www.abengoa.com/web/en/noticias\\_y\\_publicaciones/noticias/historico/2016/02\\_febrero/ab](https://www.abengoa.com/web/en/noticias_y_publicaciones/noticias/historico/2016/02_febrero/abg_20160205.html)  
1158 [g\\_20160205.html](https://www.abengoa.com/web/en/noticias_y_publicaciones/noticias/historico/2016/02_febrero/abg_20160205.html), Last Accessed 19 March 2021.

1159 Advisian Worley Group (2021), Khi Solar One 50MW solar power tower plant,  
1160 <https://www.advisian.com/en/case-studies/khi-solar-one-50mw-solar-power-tower-plant>, Last  
1161 Accessed 19 March 2021.

1162 Andraka, C.E., Christian, J.M., Ghanbari, C.M., Gill, D.D., Ho, C.K., Kolb, W.J., Moss, T.A., Smith,  
1163 E.J. and Yellowhair, J. (2013), “Sandia Capabilities for the Measurement, Characterization, and  
1164 Analysis of Heliostats for CSP”, Sandia National Lab.(SNL-NM), Albuquerque, NM (United  
1165 States),

1166 Arbes, F., Wöhrbach, M., Gebreiter, D. and Weinrebe, G. (2017) Towards high efficiency heliostat  
1167 fields. In: Proc., AIP Conference Proceedings,

1168 AS/NZS 1170.2 (2011), “Structural Design Actions - Part 2: Wind actions”, Standards Australia and  
1169 Standards New Zealand, Sydney.

1170 ASCE 7-02 (2002), Minimum design wind loads for buildings and other structures, American Society  
1171 of Civil Engineers, Reston, Virginia.

1172 ASCE/SEI 7-16 (2016), “Wind loads on building appertenances and other structures: main wind force  
1173 resisting system (directional procedure)”, American Society of Civil Engineers, Reston, Virginia.

1174 Banks, D. (2011) Measuring peak wind loads on solar power assemblies. In: Proc., 13th International  
1175 Conference on Wind Engineering,

1176 Benammar, S. and Tee, K.F. (2019), Structural reliability analysis of a heliostat under wind load for  
1177 concentrating solar power, *Solar Energy*, 181, 43-52.

1178 Blackmon, J.B. (2014), Heliostat drive unit design considerations–Site wind load effects on projected  
1179 fatigue life and safety factor, *Solar energy*, 105, 170-180.

1180 Blume, K., Röger, M., Schlichting, T., Macke, A. and Pitz-Paal, R. (2020), Dynamic photogrammetry  
1181 applied to a real scale heliostat: Insights into the wind-induced behavior and effects on the optical  
1182 performance, *Solar Energy*, 212, 297-308.

1183 Bureau of Meteorology (2020), Climate data services, <http://www.bom.gov.au/climate/data/>, Last  
1184 Accessed 1 April 2020.

1185 Cook, N.J. (1978), Determination of the model scale factor in wind-tunnel simulations of the adiabatic  
1186 atmospheric boundary layer, *Journal of Wind Engineering and Industrial Aerodynamics*, 2(4), 311-  
1187 321.

1188 Cook, N.J. (1985), “The designer's guide to wind loading of building structures, Part 1: Background,  
1189 damage survey, wind data and structural classification”, Building Research Establishment, Garston,  
1190 UK.

1191 Cook, N.J. (1997), The Deaves and Harris ABL model applied to heterogeneous terrain, *Journal of*  
1192 *Wind Engineering and Industrial Aerodynamics*, 66, 197-214.

1193 Counihan, J. (1975), Adiabatic atmospheric boundary layers: a review and analysis of data from the  
1194 period 1880–1972, *Atmospheric Environment*, 9(10), 871-905.

1195 De Paepe, W., Pindado, S., Bram, S. and Contino, F. (2016), Simplified elements for wind-tunnel  
1196 measurements with type-III-terrain atmospheric boundary layer, *Measurement*, 91, 590-600.

1197 Department of Energy (2017), “The SunShot 2030 Goals”, DOE/EE-1501; Solar Energy Technologies  
1198 Office, USA.

1199 Durst, C.S. (1960), Wind speeds over short periods of time, *Meteorological Magazine*, 89(1960), 181-  
1200 186.

1201 Emes, M., Jafari, A. and Arjomandi, M. (2020b), Wind load design considerations for the elevation and  
1202 azimuth drives of a heliostat, *AIP Conference Proceedings*, 2303(1), 030013.

1203 Emes, M., Jafari, A., Collins, M., Wilbert, S., Zarzalejo, L., Siegrist, S. and Arjomandi, M. (2020c)  
1204 Stowing Strategy for a Heliostat Field Based on Wind Speed and Direction. In: *Proc., Proceedings*  
1205 *of the 26th SolarPACES 2020 International Conference*,

1206 Emes, M.J., Arjomandi, M., Ghanadi, F. and Kelso, R.M. (2017), Effect of turbulence characteristics  
1207 in the atmospheric surface layer on the peak wind loads on heliostats in stow position, *Solar Energy*,  
1208 157, 284-297.

1209 Emes, M.J., Arjomandi, M., Kelso, R.M. and Ghanadi, F. (2019c), Turbulence length scales in a low-  
1210 roughness near-neutral atmospheric surface layer, *Journal of Turbulence*, 20:9, 545-562.

1211 Emes, M.J., Arjomandi, M. and Nathan, G.J. (2015), Effect of heliostat design wind speed on the  
1212 levelised cost of electricity from concentrating solar thermal power tower plants, *Solar Energy*, 115,  
1213 441-451.

1214 Emes, M.J., Ghanadi, F., Arjomandi, M. and Kelso, R.M. (2018), Investigation of peak wind loads on  
1215 tandem heliostats in stow position, *Renewable Energy*, 121, 548-558.

1216 Emes, M.J., Jafari, A., Coventry, J. and Arjomandi, M. (2020a), The influence of atmospheric boundary  
1217 layer turbulence on the design wind loads and cost of heliostats, *Solar Energy*, 207, 796-812.

1218 Emes, M.J., Jafari, A., Ghanadi, F. and Arjomandi, M. (2019a), Hinge and overturning moments due to  
1219 unsteady heliostat pressure distributions in a turbulent atmospheric boundary layer, *Solar Energy*,  
1220 193, 604-617.

1221 Emes, M.J., Jafari, A., Ghanadi, F. and Arjomandi, M. (2019b), A method for the calculation of the  
1222 design wind loads on heliostats, *AIP Conference Proceedings*, 2126(1), 030020.

1223 EN 1991-1.4 (2010), *Actions on structures, Part 1-4: General actions - Wind actions*, Eurocode,  
1224 Brussels.

1225 ESDU 85020 (2001), *Characteristics of atmospheric turbulence near the ground, Part II: single point*  
1226 *data for strong winds (neutral atmosphere)*, Engineering Sciences Data Unit, London.

1227 Farell, C. and Iyengar, A.K. (1999), Experiments on the wind tunnel simulation of atmospheric  
1228 boundary layers, *J Wind Eng Ind Aerodyn*, 79(1), 11-35.

1229 Gilooly, S. and Taylor-Power, G. (2016), *Physical Modeling of the Atmospheric Boundary Layer in the*  
1230 *University of New Hampshire's Flow Physics Facility*,

1231 Gong, B., Li, Z., Wang, Z. and Wang, Y. (2012), Wind-induced dynamic response of Heliostat,  
1232 *Renewable Energy*, 38(1), 206-213.

1233 Gong, B., Wang, Z., Li, Z., Zang, C. and Wu, Z. (2013), Fluctuating wind pressure characteristics of  
1234 heliostats, *Renewable energy*, 50, 307-316.

1235 Griffith, D.T., Moya, A.C., Ho, C.K. and Hunter, P.S. (2012) *Structural Dynamics Testing and Analysis*  
1236 *for Design Evaluation and Monitoring of Heliostats*. In: *Proc., ASME 2011 5th International*  
1237 *Conference on Energy Sustainability*,

1238 Griffith, D.T., Moya, A.C., Ho, C.K. and Hunter, P.S. (2015), Structural dynamics testing and analysis  
1239 for design evaluation and monitoring of heliostats, *Journal of Solar Energy Engineering*, 137(2),  
1240 021010.

1241 Ho, C.K., Griffith, D.T., Sment, J., Moya, A.C., Christian, J.M., Yuan, J.K. and Hunter, P.S. (2012)  
1242 Dynamic Testing and Analysis of Heliostats to Evaluate Impacts of Wind on Optical Performance  
1243 and Structural Fatigue. In: *Proc., SolarPACES*,

1244 Hui, T.M. (2011), Design and optimization of heliostatt field using spinning-elevation sun tracking  
1245 method based on computational analysis, Master of Engineering, Universiti Tunku Abdul Rahman,  
1246 IEC 61400-1 (2005), Wind turbines–part 1: Design requirements, Geneva.

1247 IRENA (2020), “Renewable power generation costs in 2019”, International Renewable Energy Agency,  
1248 Abu Dhabi.

1249 Iyengar, A.K.S. and Farell, C. (2001), Experimental issues in atmospheric boundary layer simulations:  
1250 Roughness length and integral length scale determination, *Journal of Wind Engineering and*  
1251 *Industrial Aerodynamics*, 89(11), 1059-1080.

1252 Jafari, A., Emes, M., Cazzolato, B., Ghanadi, F. and Arjomandi, M. (2020a), Turbulence characteristics  
1253 in the wake of a heliostat in an atmospheric boundary layer flow, *Physics of Fluids*, 32(4), 045116.

1254 Jafari, A., Emes, M., Cazzolato, B., Ghanadi, F. and Arjomandi, M. (2020b), An experimental  
1255 investigation of unsteady pressure distribution on tandem heliostats, *AIP Conference Proceedings*,  
1256 2303(1), 030022.

1257 Jafari, A., Emes, M., Cazzolato, B., Ghanadi, F. and Arjomandi, M. (2021), Wire mesh fences for  
1258 manipulation of turbulence energy spectrum, *Experiments in Fluids*, 62(2), 30.

1259 Jafari, A., Ghanadi, F., Arjomandi, M., Emes, M.J. and Cazzolato, B.S. (2019a), Correlating turbulence  
1260 intensity and length scale with the unsteady lift force on flat plates in an atmospheric boundary layer  
1261 flow, *Journal of Wind Eng and Ind Aero*, 189, 218-230.

1262 Jafari, A., Ghanadi, F., Emes, M.J., Arjomandi, M. and Cazzolato, B.S. (2018) Effect of Free-stream  
1263 Turbulence on the Drag Force on a Flat Plate. In: *Proc., AFMC*,

1264 Jafari, A., Ghanadi, F., Emes, M.J., Arjomandi, M. and Cazzolato, B.S. (2019b), Measurement of  
1265 unsteady wind loads in a wind tunnel: scaling of turbulence spectra, *Journal of Wind Eng and Ind*  
1266 *Aero*, 193, 103955.

1267 Jain, A., Jones, N.P. and Scanlan, R.H. (1996), Coupled flutter and buffeting analysis of long-span  
1268 bridges, *Journal of Structural Engineering*, 122(7), 716-725.

1269 Kaimal, J.C. and Finnigan, J.J. (1994), *Atmospheric Boundary Layer Flows: Their Structure and*  
1270 *Measurement*, Oxford University Press.

1271 Kolb, G.J., Ho, C.K., Mancini, T.R. and Gary, J.A. (2011), “Power Tower Technology Roadmap and  
1272 Cost Reduction Plan”, SAND2011-2419; Sandia National Laboratories, Albuquerque, USA.

1273 Kopp, G.A., Farquhar, S. and Morrison, M.J. (2012), Aerodynamic mechanisms for wind loads on  
1274 tilted, roof-mounted, solar arrays, *Journal of Wind Engineering and Industrial Aerodynamics*, 111,  
1275 40-52.

1276 Kozmar, H. (2012), Physical modeling of complex airflows developing above rural terrains,  
1277 *Environmental Fluid Mechanics*, 12(3), 209-225.

1278 Leitch, C.J., Ginger, J. and Holmes, J. (2016), Wind loads on solar panels mounted parallel to pitched  
1279 roofs, and acting on the underlying roof, *Wind and Structures*, 22(3), 307-328.

1280 Li, Q.S., Zhi, L. and Hu, F. (2010), Boundary layer wind structure from observations of a 325 m tower,  
1281 *Journal of Wind Engineering and Industrial Aerodynamics*, 98, 818-832.

1282 Mehos, M., Turchi, C., Vidal, J., Wagner, M., Ma, Z., Ho, C., Kolb, W., Andraka, C. and Kruiuzenga,  
1283 A. (2017), “Concentrating solar power Gen3 demonstration roadmap”, National Renewable Energy  
1284 Lab.(NREL), Golden, CO (United States),

1285 Mendis, P., Ngo, T., Haritos, N., Hira, A., Samali, B. and Cheung, J. (2007), Wind loading on tall  
1286 buildings, *EJSE Special Issue: Loading on Structures*, 3, 41-54.

1287 Menicucci, A.R., Ho, C.K. and Griffith, D.T. (2012) High Performance Computing for Static and  
1288 Dynamic Analyses of Heliostats for Concentrating Solar Power. In: *Proc., Proceedings of the World*  
1289 *Renewable Energy Forum (WREF 2012)*, Denver, CO, May,

1290 Murphy, L.M. (1980), “Wind loading on tracking and field-mounted solar collectors”, SERI-TP-632-  
1291 958; Solar Energy Research Institute, Golden, USA.



1292 Nakamura, Y. (1993), Bluff-body aerodynamics and turbulence, *J Wind Eng Ind Aerodyn*, 49(1), 65-  
1293 78.

1294 National Climatic Data Center (2020), Climate data online, [http://www.ncdc.noaa.gov/cdo-  
1295 web/datasets](http://www.ncdc.noaa.gov/cdo-<br/>1295 web/datasets), Last Accessed 1 April 2020.

1296 Noone, C.J., Torrilhon, M. and Mitsos, A. (2012), Heliostat field optimization: A new computationally  
1297 efficient model and biomimetic layout, *Solar Energy*, 86(2), 792-803.

1298 Peterka, J.A., Bienkiewicz, B., Hosoya, N. and Cermak, J.E. (1987), Heliostat mean wind load  
1299 reduction, *Energy*, 12(3-4), 261-267.

1300 Peterka, J.A. and Derickson, R.G. (1992), “Wind load design methods for ground-based heliostats and  
1301 parabolic dish collectors”, SAND92-7009; Sandia National Laboratories, Albuquerque, New  
1302 Mexico.

1303 Peterka, J.A., Hosoya, N., Bienkiewicz, B. and Cermak, J.E. (1986), “Wind load reduction for  
1304 heliostats”, SERI/STR-253-2859; Colorado State University, Fort Collins, USA.

1305 Peterka, J.A., Hosoya, N., Dodge, S., Cochran, L. and Cermak, J.E. (1998), Area-average peak pressures  
1306 in a gable roof vortex region, *Journal of Wind Engineering and Industrial Aerodynamics*, 77-78,  
1307 205-215.

1308 Peterka, J.A., Tan, L., Bienkiewicz, B. and Cermak, J.E. (1987), Mean and peak wind load reduction on  
1309 heliostats, Technical Report for Colorado State University,

1310 Peterka, J.A., Tan, Z., Bienkiewicz, B. and Cermak, J. (1988), “Wind loads on heliostats and parabolic  
1311 dish collectors: Final subcontractor report”, SERI/STR-253-3431; Solar Energy Research Institute,  
1312 Golden, Colorado.

1313 Peterka, J.A., Tan, Z., Cermak, J.E. and Bienkiewicz, B. (1989), Mean and peak wind loads on  
1314 heliostats, *Journal of Solar Energy Engineering*, 111(2), 158-164.

1315 Pfahl, A. (2014a), Survey of heliostat concepts for cost reduction, *Journal of Solar Energy Engineering*,  
1316 136(1),

1317 Pfahl, A. (2018), *Wind loads on heliostats and photovoltaic trackers*, PhD thesis, Technische  
1318 Universiteit Eindhoven.

1319 Pfahl, A., Brucks, A. and Holze, C. (2014b), Wind load reduction for light-weight heliostats, *Energy*  
1320 *Procedia*, 49, 193-200.

1321 Pfahl, A., Buselmeier, M. and Zschke, M. (2011a), Wind loads on heliostats and photovoltaic trackers  
1322 of various aspect ratios, *Solar Energy*, 85, 2185-2201.

1323 Pfahl, A., Buselmeier, M. and Zschke, M. (2011c) Determination of wind loads on heliostats. In: *Proc.*,  
1324 *Proceedings of the 17th SolarPACES Conference*,

1325 Pfahl, A., Coventry, J., Röger, M., Wolfertstetter, F., Vásquez-Arango, J.F., Gross, F., Arjomandi, M.,  
1326 Schwarzbözl, P., Geiger, M. and Liedke, P. (2017a), Progress in heliostat development, *Solar*  
1327 *Energy*, 152, 3-37.

1328 Pfahl, A., Gross, F., Liedke, P., Hertel, J., Rheinländer, J., Mehta, S., Vásquez-Arango, J.F., Giuliano,  
1329 S. and Buck, R. (2017b) Reduced to Minimum Cost: Lay-Down Heliostat with Monolithic Mirror-  
1330 Panel and Closed Loop Control. In: *Proc.*, *SolarPACES 2017, Santiago*.

1331 Pfahl, A., Randt, M., Holze, C. and Unterschütz, S. (2013), Autonomous light-weight heliostat with rim  
1332 drives, *Solar Energy*, 92, 230-240.

1333 Pfahl, A., Randt, M., Meier, F., Zschke, M., Geurts, C. and Buselmeier, M. (2015), A holistic approach  
1334 for low cost heliostat fields, *Energy Procedia*, 69, 178-187.

1335 Pfahl, A. and Uhlemann, P. (2011b), Wind loads on heliostats and photovoltaic trackers at various  
1336 Reynolds numbers, *Journal of Wind Engineering and Industrial Aerodynamics*, 99, 964-968.

1337 Price, H., Mehos, M.S., Cable, R., Kearney, D., Kelly, B., Kolb, G. and Morse, F. (2020) CSP plant  
1338 construction, start-up, and O&M best practices study. In: *Proc.*, *AIP Conference Proceedings*,

1339 Rasmussen, J.T., Hejlesen, M.M., Larsen, A. and Walther, J.H. (2010), Discrete vortex method  
1340 simulations of the aerodynamic admittance in bridge aerodynamics, *Journal of Wind Engineering*  
1341 *and Industrial Aerodynamics*, 98(12), 754-766.

1342 Simiu, E. and Scanlan, R.H. (1996), *Wind effects on structures: fundamentals and applications to*  
1343 *design*, John Wiley & Sons.

1344 Sment, J. and Ho, C. (2014), Wind patterns over a heliostat field, *Energy Procedia*, 49, 229-238.

1345 Stull, R.B. (1988), *An introduction to boundary layer meteorology*, Kluwer Academic, Dordrecht,  
1346 Netherlands.

1347 Stull, R.B. (2005), *The Atmospheric Boundary Layer*, University of British Columbia, Vancouver,  
1348 Canada.

1349 Sun, H., Gong, B. and Yao, Q. (2014), A review of wind loads on heliostats and trough collectors,  
1350 *Renewable and Sustainable Energy Reviews*, 32, 206-221.

1351 Téllez, F., Burisch, M., Villasente, Sánchez, M., Sansom, C., Kirby, P., Turner, P., Caliot, C., Ferriere,  
1352 A., Bonanos, C.A., Papanicolas, C., Montenon, A., Monterreal, R. and Fernández, J. (2014), “State  
1353 of the Art in Heliostats and Definition of Specifications”, 609837; STAGE-STE Project, Madrid.

1354 Tieleman, H.W. (2003), Wind tunnel simulation of wind loading on low-rise structures: A review,  
1355 *Journal of Wind Engineering and Industrial Aerodynamics*, 91(12), 1627-1649.

1356 Turchi, C.S., Boyd, M., Kesseli, D., Kurup, P., Mehos, M.S., Neises, T.W., Sharan, P., Wagner, M.J.  
1357 and Wendelin, T. (2019), “CSP Systems Analysis-Final Project Report”, National Renewable  
1358 Energy Laboratory (NREL), Golden, Colorado.

1359 Vásquez-Arango, J.F., Buck, R. and Pitz-Paal, R. (2015), Dynamic Properties of a Heliostat Structure  
1360 Determined by Numerical and Experimental Modal Analysis, *Journal of Solar Energy Engineering*,  
1361 137(5), 051001.

1362 Vasquez Arango, J.F., Pitz-Paal, R. and Breuer, M. (2017), *Dynamic wind loads on heliostats*, PhD  
1363 Thesis, Lehrstuhl für Solartechnik (DLR).

1364 von Kármán, T. (1948), Progress in the Statistical Theory of Turbulence, *Proceedings of the National*  
1365 *Academy of Sciences*, 34(11), 530-539.

1366 Wolmarans, J.R. and Craig, K. (2019), One-way fluid-structure interaction of a medium-sized heliostat  
1367 using scale-resolving CFD simulation, *Solar Energy*, 191, 84-99.

1368 Wu, Z., Gong, B., Wang, Z., Li, Z. and Zang, C. (2010), An experimental and numerical study of the  
1369 gap effect on wind load on heliostat, *Renewable Energy*, 35(4), 797-806.

1370 Xiong, Q., Li, Z., Luo, H. and Zhao, Z. (2019), Wind tunnel test study on wind load coefficients  
1371 variation law of heliostat based on uniform design method, *Solar Energy*, 184, 209-229.

1372 Xiong, Q., Li, Z., Luo, H., Zhao, Z. and Jiang, A. (2021), Study of probability characteristics and peak  
1373 value of heliostat support column base shear, *Renewable Energy*, 168, 1058-1072.

1374 Xu, Y.L. (2013), *Wind Effects on Cable-Supported Bridges*, John Wiley & Sons, Singapore.

1375 Yu, J.S., Emes, M.J., Ghanadi, F., Arjomandi, M. and Kelso, R.M. (2019), Experimental investigation  
1376 of peak wind loads on tandem operating heliostats within an atmospheric boundary layer, Solar  
1377 Energy, 183, 248-259.  
1378