

Low-Cost Small-Scale Wind Power Generation

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Dedicated to my late grandmother, Χρυσούλα Ηλιάδου (Chryssoula Pliadis)

Table of Contents

| | |
|---|----------|
| Table of Contents | v |
| Abstract | xi |
| Statement of Originality | xiii |
| Acknowledgements | xv |
| List of Publications | xvii |
| Conventions | xix |
| Nomenclature | xxi |
| List of Figures | xxxix |
| List of Tables | xxxix |
| 1 Introduction | 1 |
| 1.1 Wind Energy | 1 |
| 1.1.1 Electricity Usage and Conventional Generation | 2 |
| 1.1.2 Alternative Energy Sources | 3 |
| 1.1.3 Large and Small-Scale Turbine Classification | 4 |
| 1.1.4 Small-Scale Turbine Development | 5 |
| 1.1.5 Technology Improvement | 6 |
| 1.1.6 Market Growth | 6 |
| 1.2 Principles of Wind Power | 7 |
| 1.2.1 Wind and Turbine Power | 7 |
| 1.2.2 Coefficient of Performance | 8 |

| | | |
|-------|--|----|
| 1.2.3 | Principles of Turbine Operation | 9 |
| 1.3 | Small-Scale Wind Turbines | 11 |
| 1.3.1 | Applications | 11 |
| 1.3.2 | Turbine Properties | 12 |
| 1.3.3 | Generator Varieties | 13 |
| 1.3.4 | Current Trends | 15 |
| 1.3.5 | Inductance Classification of PM Generators | 16 |
| 1.4 | Standalone Power Converters | 18 |
| 1.4.1 | Common Power Converters | 18 |
| 1.4.2 | Uncontrolled Rectifier Operation | 21 |
| 1.4.3 | Switched-Mode Rectifier | 23 |
| 1.4.4 | Inverter Operation | 25 |
| 1.4.5 | Power Comparison of Standalone Converters | 27 |
| 1.5 | Grid-Connected Inverters | 29 |
| 1.5.1 | Introduction | 29 |
| 1.5.2 | Line-Commutated Inverters | 30 |
| 1.5.3 | Self-Commutated Inverters | 32 |
| 1.5.4 | Transformer Type | 35 |
| 1.5.5 | Voltage Source Topologies | 37 |
| 1.5.6 | Current Source Topologies | 40 |
| 1.5.7 | Current Trends | 42 |
| 1.5.8 | Proposed Grid-Connected Inverter | 43 |
| 1.6 | Thesis Overview | 44 |
| 1.6.1 | Aim of Research | 44 |
| 1.6.2 | Justification for Research | 44 |
| 1.6.3 | Original Contributions | 45 |
| 1.6.4 | Thesis Structure | 45 |

I Investigation of Switched-Mode Rectifier for Standalone Power Converter 49

2 High Inductance PM Generator Characteristics 51

| | | |
|-------|---|----|
| 2.1 | Introduction | 51 |
| 2.1.1 | Ideal Machine Model and Current vs. Voltage Locus | 54 |

| | | |
|----------|--|-----------|
| 2.1.2 | Inductance Classification | 55 |
| 2.2 | Machine Characterisation | 57 |
| 2.2.1 | Realistic Machine Model and Effect on Loci | 57 |
| 2.2.2 | Test Arrangement | 58 |
| 2.2.3 | Open-Circuit Test | 60 |
| 2.2.4 | Short-Circuit Test | 62 |
| 2.2.5 | Machine Losses | 65 |
| 2.2.6 | Machine Properties | 66 |
| 2.3 | Machine Modelling | 67 |
| 2.3.1 | Analytical Model | 67 |
| 2.3.2 | PSIM® Model | 70 |
| 2.3.3 | Power Maximisation | 72 |
| 2.3.4 | Model Comparison | 73 |
| 2.4 | Resistive Load Testing | 74 |
| 2.4.1 | 3ph Resistive Loading | 74 |
| 2.4.2 | DC Resistive Loading | 77 |
| 2.5 | Chapter Summary | 83 |
| 3 | Switched-Mode Rectifier Operation | 85 |
| 3.1 | Introduction | 85 |
| 3.1.1 | Switched-Mode Rectifier Model | 86 |
| 3.1.2 | SMR Operation | 88 |
| 3.1.3 | SMR Properties | 90 |
| 3.2 | Dynamometer Testing | 92 |
| 3.2.1 | Test Arrangement | 92 |
| 3.2.2 | SMR Test Results | 92 |
| 3.2.3 | Summary of Testing | 99 |
| 3.3 | Wind Tunnel Testing | 100 |
| 3.3.1 | Test Arrangement | 100 |
| 3.3.2 | Turbine Coefficient of Performance | 102 |
| 3.3.3 | Open-Loop Control Mode | 104 |
| 3.3.4 | Comparison of Control Modes | 107 |
| 3.4 | Chapter Summary | 112 |

II Investigation of Grid-Connected Inverter based on Switched-Mode Rectifier Topology **115**

| | | |
|----------|---|------------|
| 4 | Simulation and Test of 150W GC Inverter | 117 |
| 4.1 | Introduction | 117 |
| 4.1.1 | Inverter Requirements | 118 |
| 4.1.2 | Desirable Features | 120 |
| 4.2 | Proposed Concept | 122 |
| 4.2.1 | Inverter Overview | 122 |
| 4.2.2 | Constant Current Source | 123 |
| 4.2.3 | Current Wave-Shaper | 124 |
| 4.2.4 | Unfolding Circuit | 126 |
| 4.2.5 | Low-Pass Filter | 127 |
| 4.3 | Test Set-up, Implementation and Simulation | 128 |
| 4.3.1 | Dynamometer Test Arrangement | 128 |
| 4.3.2 | Constant Current Source - PM Generator | 131 |
| 4.3.3 | Power Electronics and Control Implementation | 133 |
| 4.3.4 | Inverter Simulation | 135 |
| 4.4 | Experimental Testing | 138 |
| 4.4.1 | Proof of Concept - Resistive Loading | 138 |
| 4.4.2 | Constant Current Assumption | 141 |
| 4.4.3 | Grid-Connected Testing | 145 |
| 4.5 | Chapter Summary | 153 |
| 5 | Inverter Analysis and Control | 155 |
| 5.1 | Analysis of Non-Ideal Constant Current Source | 155 |
| 5.1.1 | Fluctuating Input Current | 156 |
| 5.1.2 | Rectifier Ripple | 160 |
| 5.1.3 | The Resulting Input Current | 162 |
| 5.2 | Total Harmonic Distortion | 164 |
| 5.2.1 | Fluctuating Input Power | 164 |
| 5.2.2 | Rectifier Ripple | 166 |
| 5.2.3 | The Resulting Input Current | 167 |
| 5.2.4 | PWM Switching Schemes | 171 |
| 5.2.5 | The Inverter Output Current | 175 |

| | | |
|----------|---|------------|
| 5.2.6 | Reducing Harmonic Distortion | 176 |
| 5.3 | Low-Pass Filter Analysis | 182 |
| 5.3.1 | Filter Response | 183 |
| 5.3.2 | Filter Damping | 184 |
| 5.3.3 | Damped Filter Response and Configuration Comparison | 184 |
| 5.3.4 | Design Considerations | 188 |
| 5.3.5 | Harmonic Attenuation and Distortion | 191 |
| 5.3.6 | Power Factor Requirements | 194 |
| 5.3.7 | Power Loss | 198 |
| 5.3.8 | Design Trade-Offs - Unipolar PWM Waveform | 201 |
| 5.3.9 | Effect of Non-Ideal Current Source | 208 |
| 5.3.10 | Alternative (Third-Order) Filter Configurations | 209 |
| 5.4 | Feed-Forward Control | 211 |
| 5.4.1 | Introduction | 211 |
| 5.4.2 | Aim of Proposed Feed-Forward Control | 211 |
| 5.4.3 | Controller 1 (FFC 1): Sample Machine Frequency | 213 |
| 5.4.4 | Controller 2 (FFC 2): Sample Inverter Input Current | 218 |
| 5.4.5 | Comparison of Feed-Forward and Open-Loop Control | 221 |
| 5.5 | Chapter Summary | 224 |
| 6 | Design and Simulation of 1kW GC Inverter System | 225 |
| 6.1 | Turbine Sizing and Machine Parameter Selection | 225 |
| 6.1.1 | System Assumptions | 225 |
| 6.1.2 | Turbine Power and Size Calculations | 226 |
| 6.1.3 | Generator Equivalent Circuit Parameter Selection | 228 |
| 6.2 | Low-Pass Filter Design | 234 |
| 6.2.1 | Design Criteria | 234 |
| 6.2.2 | Component Selection | 234 |
| 6.2.3 | Filter Simulation - Ideal Current Source | 237 |
| 6.2.4 | Filter Simulation - PM Generator Current Source | 238 |
| 6.3 | Demonstration of Feed-Forward Control | 242 |
| 6.3.1 | Control Implementation | 242 |
| 6.3.2 | Proof of Concept at Rated Wind Speed | 243 |
| 6.3.3 | Current Command Variation at Rated Wind Speed | 245 |
| 6.4 | Inverter Simulation for Wide Wind Speed Range | 252 |

| | | |
|----------|---|------------|
| 6.4.1 | Turbine Characteristics | 252 |
| 6.4.2 | Power Control Modes | 254 |
| 6.4.3 | Optimised Component Selection | 255 |
| 6.4.4 | Inverter Simulations | 256 |
| 6.4.5 | Efficiency Analysis | 259 |
| 6.5 | Chapter Summary | 262 |
| 7 | Conclusions and Future Work | 263 |
| 7.1 | Summary and Conclusions | 263 |
| 7.2 | Original Contributions | 265 |
| 7.3 | Recommendations for Future Work | 267 |
| | Appendices | 269 |
| A | PWM Control Strategies and Low-Pass Filter Design Trade-Offs | 269 |
| A.1 | PWM Switching Schemes | 269 |
| A.1.1 | Bipolar and Unipolar Pulse-Width Modulation | 269 |
| A.1.2 | Selective Harmonic Elimination | 269 |
| A.1.3 | Current Hysteresis | 270 |
| A.1.4 | Space Vector Modulation | 271 |
| A.2 | Low-Pass Filter Design | 272 |
| A.2.1 | Power Loss vs. THD Trade-Off - Unipolar PWM Case | 272 |
| B | Relevant Publications | 273 |
| B.1 | Wind Turbine Control using SMR Paper | 274 |
| B.2 | Novel Low-Cost Grid-Connected Inverter Paper | 284 |
| C | Microcontroller Code | 291 |
| C.1 | Switched-Mode Rectifier | 291 |
| C.2 | Grid-Connected Inverter | 294 |
| | References | 299 |

Abstract

This research investigates a low-cost generator and power electronics unit for small-scale (<10kW) wind turbines, for both standalone and grid-connected applications. The proposed system uses a high-inductance permanent magnet generator together with a switched-mode rectifier (SMR) to produce a variable magnitude output current. The high inductance characteristic allows the generator to operate as a current source, which has the following advantages over conventional low-inductance generator (voltage source) systems: it offers simple control, and avoids the need for bulky / costly energy storage elements, such as capacitors and inductors.

The SMR duty-cycle is controlled in an open-loop manner such that 1) maximum power is obtained for wind speeds below rated, and 2) the output power and turbine speed is limited to safe values above rated wind speed. This topology also has the ability to extract power at low wind speeds, which is well suited to small-scale wind turbines, as there is often limited flexibility in their location and these commonly see low average wind speeds.

The thesis is divided into two parts; the first part examines the use of the SMR as a DC-DC converter, for use in standalone applications. The duty-cycle is essentially kept constant, and is only varied for maximum power tracking and turbine speed / power limiting purposes. The SMR operates in to a fixed voltage source load, and has the ability to allow current and hence power to be drawn from the generator even at low wind and hence turbine speeds, making it ideal for battery charging applications. Initial dynamometer testing and limited wind-tunnel testing of a commercially available wind turbine show that turbine power can be maximised and its speed can be limited by adjusting the SMR duty-cycle in an open-loop manner.

The second part of the thesis examines the use of the SMR as a DC-AC converter for grid-connected applications. The duty-cycle is now modulated sinusoidally at the mains frequency such that the SMR produces an output current that resembles a full-wave rectified sinewave that is synchronised to the mains voltage. An additional H-

bridge inverter circuit and low-pass filter is used to unfold, filter and feed the sinusoidal output current in to the utility grid. Simulation and initial resistive load and preliminary grid-connected tests were used to prove the inverter concept, however, the permanent magnet generator current source is identified as non-ideal and causes unwanted harmonic distortion.

The generator harmonics are analysed, and the system performance is compared with the Australian Standard THD requirement. It is concluded that the harmonics are caused by 1) the low-cost single-phase output design, 2) the use of an uncontrolled rectifier, and 3) the finite back-EMF voltage. The extent of these harmonics can be predicted based on the inverter operating conditions. A feed-forward current compensation control algorithm is investigated, and shown to be effective at removing the harmonics caused by the non-ideal current source. In addition, the unipolar PWM switching scheme, and its harmonic components are analysed. The low-pass filter design is discussed, with an emphasis on power factor and THD grid requirements. A normalised filter design approach is used that shows how design aspects, such as cutoff frequency and quality factor, affect the filter performance. The filter design is shown to be a trade-off between the output current THD, power loss, and quality factor.

The final chapter summarises the thesis with the design and simulation of a 1kW single-phase grid-connected inverter. The inverter is designed based on the low-pass filter and feed-forward compensation analysis, and is shown to deliver an output current to the utility grid that adheres to the Australian Standards.

Statement of Originality

This work contains no material which has been accepted for the award of any other degree or diploma in any university or other tertiary institution to David M. Whaley and, to the best of my knowledge and belief, contains no material previously published or written by another person, except where due reference has been made in the text.

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Signed

Date

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List of Publications

- [1] G. Ertasgin, **D.M. Whaley**, N. Ertugrul and W.L. Soong, “Implementation and Performance Evaluation of a Low-Cost Current-Source Grid-Connected Inverter for PV Application”, in *Proceedings of the IEEE International Conference on Sustainable Energy Technologies*, Nov. 2008, Singapore.
- [2] G. Ertasgin, **D.M. Whaley**, N. Ertugrul and W.L. Soong, “Analysis and Design of Energy Storage for Current-Source 1-ph Grid-Connected PV Inverters”, in *Proceedings of the IEEE Applied Power Electronics Conference and Exposition*, Feb., 2008, pp. 1229 – 1234.
- [3] G. Ertasgin, **D.M. Whaley**, N. Ertugrul, and W.L. Soong, “A Current-Source Grid-Connected Converter Topology for Photovoltaic Systems”, in *Proceedings of Australasian Universities Power Engineering Conference*, 2006.
- [4] **D.M. Whaley**, G. Ertasgin, W.L. Soong, N. Ertugrul, J. Darbyshire, H. Dehbonei, and C.V. Nayar, “Investigation of a Low-Cost Grid-Connected Inverter for Small-Scale Wind Turbines Based on a Constant-Current Source PM Generator”, in *Proceedings of the IEEE Industry Electronics*, Nov., 2006, pp. 4297 – 4302.
- [5] C.Z. Liaw, **D.M. Whaley**, W.L. Soong, and N. Ertugrul, “Implementation of Inverterless Control of Interior Permanent Magnet Alternators”, in *IEEE Transactions on Industry Applications*, vol. 42, no. 2, Mar. - Apr., 2006, pp. 536 – 544.
- [6] **D.M. Whaley**, W.L. Soong, and N. Ertugrul, “Investigation of Switched-Mode Rectifier for Control of Small-Scale Wind Turbines”, in *Proceedings of the IEEE Industry Applications Conference*, vol. 4, Oct., 2005, pp. 2849 – 2856.
- [7] C.Z. Liaw, **D.M. Whaley**, W.L. Soong, and N. Ertugrul, “Implementation of Inverterless Control of Interior Permanent Magnet Alternators”, in *Proceedings of the IEEE Industry Applications Conference*, Oct., 2004.

- [8] **D.M. Whaley**, W.L. Soong, and N. Ertugrul, “Extracting More Power from the Lundell Car Alternator”, in *Proceedings of Australasian Universities Power Engineering Conference*, 2004.

Portions of the work presented in this thesis have been previously published. The material in Chapters 2 and 3 correspond to work in publications [6], whilst Chapter 4 corresponds to the work presented in publication [4]. Reprints of these publications are found in appendix B, for convenience.

Conventions

This thesis employs the IEEE reference style for citations, and is written using Australian English, as defined by the Macquarie English Dictionary 2005.

All voltages and currents shown in figures and equations are expressed as RMS (root-mean squared) quantities, unless otherwise stated.

The *hat* symbol is used in Chapters 5 and 6 to indicate peak value, i.e. $\hat{\alpha}$ and $\hat{\alpha}_0$ indicate the peak values of α and α_0 , respectively. Similarly, the *check* symbol is used in Chapter 6 to represent the nadir (minimum) value, e.g. $\check{\beta}$ represents the minimum value of β .

Measured data is represented by hollow points, e.g. circles, squares, diamonds etc. and is often accompanied by solid lines that correspond to the equivalent analytical or computer based simulations. Multiple cases of measured (and simulated) data commonly appear on a single figure, and are differentiated by colour and shape. In contrast, coloured / shaded points represent calculated data. These are also shown with solid lines, however, these are for aesthetic purposes, i.e. they simply join the calculated data.

The above convention is used for the majority of this thesis, i.e. Chapters 2 to 5, however, the convention is modified for Chapter 6, as the data presented in this chapter is either simulated or analytically calculated. The simulated data, of Chapter 6 is hence shown as shaded points, whilst the analytical calculations are shown by the solid lines.

Nomenclature

| | | |
|-----------------|--|-------|
| α | normalised rectifier voltage | pu |
| α_0 | ratio of grid to open-circuit rectifier voltage | |
| α_{cu} | temperature coefficient of copper | /°C |
| β | normalised rectifier current | pu |
| $\check{\beta}$ | normalised minimum inverter input current | pu |
| β_{app} | normalised approximated rectifier current | pu |
| β_{exp} | normalised experimental rectifier current | pu |
| β_{id} | normalised ideal rectifier current | pu |
| Δ | difference | |
| δ | skin depth | m |
| η_{gen} | generator efficiency | % |
| η_{inv} | inverter efficiency | % |
| λ | tip-speed ratio | |
| μ | permability | H/m |
| ω | machine angular speed | rad/s |
| ω | turbine angular speed | rad/s |
| ω_{cn} | normalised cutoff frequency (relative to f_1) | pu |
| ω_e | electrical angular frequency | rad/s |

| | | |
|------------------|---|-----------------------------|
| ω_g | grid angular frequency | rad/s |
| ω_m | mechanical angular frequency | rad/s |
| ϕ | filter delay | deg |
| ϕ | power factor angle | deg |
| Ψ_m | RMS flux linkage | Wb or Vs |
| ρ | air density | kg/m ³ |
| σ | conductivity | (Ω m) ⁻¹ |
| $\hat{\alpha}_0$ | peak value of α_0 | |
| ξ | saliency ratio | |
| C | capacitance | F |
| c_p | turbine coefficient of performance | |
| d | duty-cycle | % |
| d_a | adjusted duty-cycle | % |
| d_i | stored duty-cycle | % |
| dB | decibels | |
| E | induced back-EMF voltage | V |
| f | frequency | Hz |
| f_1 | fundamental frequency | Hz |
| f_{cn} | normalised cutoff frequency (relative to f_{sw}) | pu |
| f_c | cutoff frequency | Hz |
| f_m | machine frequency | Hz |
| f_{res} | resonant frequency | Hz |
| f_{sw} | switching frequency | Hz |

| | | |
|--------------------|--|----|
| $H(s)$ | filter transfer function | |
| h_1 | fundamental harmonic magnitude | % |
| h_f | harmonic frequency | Hz |
| h_m | harmonic magnitude at m multiples of f_1 | % |
| h_{tot} | total harmonic components | % |
| I | current | A |
| I^* | compensation current command | A |
| $i_{c\ exp}(t)$ | compensated current using the experimental I-V locus | pu |
| $i_{c\ id}(t)$ | compensated current using the ideal I-V locus | pu |
| I_{ch} | characteristic current | A |
| $i_c(t)$ | time-varying compensated current | A |
| I_{DC} | DC current | A |
| I_d | damping resistor current | A |
| I_f | damping resistor current (from inverter) | A |
| I_g | grid drawn current (from grid) | A |
| I_{inv} | inverter output current | A |
| I_{in} | input current | A |
| I_L | line current | A |
| $i_{out\ (id)}(t)$ | normalised time-varying ideal output current | pu |
| I_{out} | output current | A |
| I_{ph} | phase current | A |
| $i_{R\ (id)}(t)$ | normalised time-varying ideal rectifier voltage | pu |
| $I_{R\ min}$ | minimum rectifier output current | A |

| | | |
|-----------------|---|-------|
| I_R | rectifier output current | A |
| $i_R(t)$ | normalised time-varying rectifier current | pu |
| $i_{ws(id)}(t)$ | normalised time-varying ideal wave-shaper current | pu |
| I_{ws} | wave-shaper current | A |
| j | $\sqrt{-1}$ | |
| k | back-EMF constant | V/rpm |
| k_{ph} | phase back-EMF constant | V/rpm |
| L | inductance | H |
| L_1 | transformer primary inductance | H |
| L_2 | transformer secondary inductance | H |
| L_{eq} | equivalent inductance | H |
| L_{ph} | phase inductance | H |
| L_s | stator inductance | H |
| m | number of machine phases | |
| m | positive integer | |
| m_a | modulation index | % |
| n | machine / generator speed | rpm |
| n | positive odd integer | |
| n | transformer turns ratio | |
| n_k | machine speed | k rpm |
| P | power | W |
| P | real power | W |
| p | number of machine pole-pairs | |

| | | |
|---------------|---|-----------------|
| P_{CU} | copper loss | W |
| P_d | damping resistor power loss | W |
| P_{IFW} | machine iron, friction and windage loss | W |
| $P_{inv\ in}$ | total inverter input power | W |
| P_{inv} | inverter output power | W |
| P_{in} | input power | W |
| P_{loss} | SMR / generator power loss | W |
| P_L | machine power loss | W |
| P_{SMR} | SMR output power | W |
| P_{sw} | switching power loss | W |
| P_T | wind turbine power | W |
| P_W | wind power | W |
| $pk - pk$ | peak to peak | |
| Q | quality factor | |
| Q | reactive power | VA _r |
| Q_C | capacitive reactive power | VA _r |
| Q_L | inductive reactive power | VA _r |
| R | resistance | Ω |
| r | blade radius | m |
| R_1 | transformer primary resistance | Ω |
| R_2 | transformer secondary resistance | Ω |
| R_{cold} | cold resistance | Ω |
| R_d | damping resistance | Ω |

| | | |
|-------------|--|----------|
| R_{eq} | equivalent resistance | Ω |
| R_{hot} | hot resistance | Ω |
| R_L | load resistance | Ω |
| R_{ph} | phase resistance | Ω |
| R_s | stator resistance | Ω |
| $rect(t)$ | normalised time-varying rectifier ripple | pu |
| S | apparent power | VA |
| S | number of stator slots | |
| s | $j\omega$ | |
| T | torque | Nm |
| t | time | s |
| t_{off} | device <i>turn-off</i> time | s |
| t_{on} | device <i>turn-on</i> time | s |
| t_q | thyristor turn-off time | s |
| V | voltage | V |
| v | wind speed | m/s |
| V_C | capacitor voltage | V |
| V_{DC} | DC link voltage | V |
| V_{DC} | DC voltage | V |
| v_{eq} | turbine equivalent wind speed | m/s |
| $V_{g\ pk}$ | peak grid voltage | V |
| V_g | grid voltage | V |
| $v_g(t)$ | normalised time-varying grid voltage | pu |

| | | |
|-----------------|---|----------|
| v_i | internal wind tunnel wind speed | m/s |
| V_L | line voltage | V |
| $V_{ph\ pk}$ | generator phase peak voltage | V |
| $V_{R\ pk\ OC}$ | peak rectifier voltage | V |
| v_r | rated wind speed | m/s |
| $v_R(t)$ | normalised time-varying rectifier voltage | pu |
| $v_{ws}(t)$ | normalised time-varying current wave-shaper voltage | pu |
| X | reactance | Ω |
| X_{ph} | phase reactance | Ω |
| X_s | stator reactance | Ω |
| Z_{0n} | normalised characteristic impedance | pu |
| Z_0 | characteristic impedance | Ω |
| Z_s | stator impedance | Ω |

Acronyms

| | |
|-----|-------------------------|
| AC | alternating current |
| AS | Australian Standard |
| CCS | constant current source |
| CM | control modes |
| CSI | current-source inverter |
| CWS | current wave-shaper |
| DC | direct current |
| DCC | duty-cycle command |

| | |
|------|--------------------------------------|
| DFT | discrete Fourier transform |
| ESR | equivalent series resistance |
| F&P | Fisher & Paykel [®] |
| FC | filter configuration |
| FFT | fast Fourier transform |
| GC | grid connected |
| GCI | grid-connected inverter |
| HF | high-frequency |
| IFW | iron, friction and windage |
| IPM | interior permanent magnet |
| IR | International Rectifier [®] |
| ISA | integrated starter alternator |
| LA | <i>Lundell</i> alternator |
| LF | line-frequency |
| MPPT | maximum power point tracker |
| NEG | net energy gain |
| NICS | non-ideal current source |
| OC | open circuit |
| PM | permanent magnet |
| pu | per-unit |
| PV | photovoltaic |
| PWM | pulse-width modulation |
| RMS | root-mean-squared |

| | | |
|-----|---------------------------|---|
| rpm | revolutions per minute | |
| RR | rectifier ripple | |
| SC | short circuit | |
| SC | squirrel cage | |
| SG | synchronous generator | |
| SMR | switched-mode rectifier | |
| SPM | surface permanent magnet | |
| THD | total harmonic distortion | % |
| TL | transformerless | |
| TSR | tip-speed ratio | |
| UCG | uncontrolled generation | |
| VSI | voltage-source inverter | |
| WF | wound field | |
| WR | wound rotor | |

Abbreviations

| | |
|-----|--------------------------------|
| CL | capacitive-inductive |
| I-V | current vs. voltage |
| LC | inductive-capacitive |
| LCL | inductive-capacitive-inductive |
| P-V | power vs. voltage |
| RLC | resistive-inductive-capacitive |
| SPP | slots per phase per pole |

SW switch

THY thyristor

List of Figures

| | | |
|------|--|----|
| 1.1 | Breakdown of worldwide electricity production for 2005 | 3 |
| 1.2 | Typical 3-bladed wind turbine coefficient of performance | 7 |
| 1.3 | Coefficient of performance of various wind turbine rotors | 8 |
| 1.4 | Turbine power simulation | 9 |
| 1.5 | Turbine power, c_p , speed and torque simulation | 10 |
| 1.6 | Furling concept demonstration | 13 |
| 1.7 | Comparison of early and modern small-scale turbine topologies used for battery charging | 14 |
| 1.8 | Current vs. voltage locus of low and high-inductance PM generators | 17 |
| 1.9 | Comparison of DC power converter equivalent circuits | 19 |
| 1.10 | Rectifier circuit simplified equivalent modelling | 21 |
| 1.11 | Rectifier phasor diagram for various generator speeds | 22 |
| 1.12 | Generator voltage, current and power plot | 23 |
| 1.13 | SMR phasor diagrams for various generator speeds | 24 |
| 1.14 | SMR current and power plot | 25 |
| 1.15 | Simplified machine phase model under inverter operation | 26 |
| 1.16 | Inverter phasor diagram for various generator speeds | 26 |
| 1.17 | SMR current and power plot | 27 |
| 1.18 | Comparison of power converter output powers | 28 |
| 1.19 | Cost comparison of standalone and grid-connected inverters | 29 |
| 1.20 | Line-commutated current-source inverter topology | 30 |
| 1.21 | Current-source inverter with active compensation and passive filters | 31 |
| 1.22 | Comparison of voltage-source and current-source inverters | 32 |
| 1.23 | Comparison of bipolar and unipolar PWM output voltages / currents . . . | 33 |
| 1.24 | Three-phase voltage-source inverter | 37 |
| 1.25 | Voltage-source inverter topology with reverse-blocking diode | 38 |
| 1.26 | Voltage-source inverter with boost converter | 38 |

| | | |
|------|--|----|
| 1.27 | Back-to-back PWM voltage-source inverter | 39 |
| 1.28 | Hybrid voltage and current source inverter | 39 |
| 1.29 | Three-phase current-source inverter circuit | 40 |
| 1.30 | Line-commutated H-bridge inverter | 41 |
| 1.31 | Actively-commutated PWM current-source inverter | 41 |
| 1.32 | Soft-switching single-phase current-source inverter | 42 |
| 1.33 | Proposed low-cost grid-connected inverter | 43 |
| 1.34 | Thesis structure | 46 |
| | | |
| 2.1 | Fisher & Paykel surface PM machine | 52 |
| 2.2 | Comparison of interior and surface PM machines | 53 |
| 2.3 | Simplified PM machine model | 54 |
| 2.4 | I-V loci of surface PM, DC and interior PM machines | 55 |
| 2.5 | Operating regions of high and low-inductance PM machines | 56 |
| 2.6 | Realistic phase and equivalent delta connected model, and simplified machine representation | 57 |
| 2.7 | Effect of varying stator resistance on PM machine voltage loci | 58 |
| 2.8 | PM and DC machine test arrangement | 59 |
| 2.9 | PM machine load arrangement | 60 |
| 2.10 | F&P surface PM machine open-circuit characteristic | 61 |
| 2.11 | Generator open-circuit voltage waveform at 1000 rpm | 61 |
| 2.12 | F&P surface PM machine short-circuit characteristic | 62 |
| 2.13 | F&P surface PM machine inductance vs. phase current and generator speed | 63 |
| 2.14 | F&P machine stator temperature increase | 64 |
| 2.15 | Machine open and short-circuit losses | 65 |
| 2.16 | PM generator phase model | 67 |
| 2.17 | Normalised PM machine line (AC) voltage loci | 69 |
| 2.18 | PSIM [®] delta-connected PM machine model with AC and DC resistive loads | 70 |
| 2.19 | Normalised PM machine DC voltage loci | 71 |
| 2.20 | Peak normalised DC power vs. generator speed prediction, comparing the analytical and PSIM [®] models | 72 |
| 2.21 | AC and DC I-V and P-V loci, comparing ideal analytical and PSIM [®] model | 73 |
| 2.22 | PM machine load arrangement | 74 |
| 2.23 | PM machine AC voltage loci | 75 |
| 2.24 | Measured generator efficiency vs. output power | 77 |

| | | |
|------|---|-----|
| 2.25 | PM machine DC voltage loci | 78 |
| 2.26 | Maximum DC output power vs. generator speed | 79 |
| 2.27 | DC to RMS line voltage ratio | 80 |
| 2.28 | Measured generator and rectifier efficiency vs. DC output power | 81 |
| | | |
| 3.1 | SMR equivalent circuit | 86 |
| 3.2 | Ideal rectifier and SMR voltage and current vs. duty-cycle | 87 |
| 3.3 | PSIM [®] model for the switched-mode rectifier | 87 |
| 3.4 | Voltage, current and power of generator for various load voltages | 89 |
| 3.5 | SMR operating regions | 90 |
| 3.6 | SMR internal components and control circuitry | 91 |
| 3.7 | SMR test arrangement | 92 |
| 3.8 | Rectifier output voltage vs. duty-cycle for various generator speeds | 93 |
| 3.9 | Rectifier output current vs. duty-cycle for various machine speeds | 94 |
| 3.10 | SMR output current vs. duty-cycle for various generator speeds | 95 |
| 3.11 | SMR output power vs. duty-cycle for various machine test speeds | 96 |
| 3.12 | Measured torque vs. duty-cycle for various generator speeds | 96 |
| 3.13 | Duty-cycle corresponding to maximum SMR power and generator torque | 97 |
| 3.14 | Measured SMR efficiency vs. SMR output power for various machine speeds | 98 |
| 3.15 | Total efficiency vs. SMR output power characteristic for various generator speeds | 99 |
| 3.16 | Wind tunnel test arrangement | 100 |
| 3.17 | Equivalent wind speed calculation at blade sweep area | 101 |
| 3.18 | Estimated coefficient of performance vs. tip-speed ratio curve | 102 |
| 3.19 | Estimated equivalent vs. wind tunnel wind speed curve | 103 |
| 3.20 | Estimated turbine power vs. speed | 104 |
| 3.21 | Estimated turbine torque vs. speed | 105 |
| 3.22 | SMR output power vs. duty-cycle | 106 |
| 3.23 | Turbine speed vs. duty-cycle | 107 |
| 3.24 | Measured duty-cycle vs. wind speed comparison for both control modes | 108 |
| 3.25 | Turbine and SMR operating characteristics for both control modes | 109 |
| 3.26 | Estimated SMR and generator efficiency vs. SMR output power | 110 |
| | | |
| 4.1 | Simple block diagram of a grid-connected wind turbine, and inverter output current | 118 |
| 4.2 | Lagging and leading power factors | 119 |

| | | |
|------|---|-----|
| 4.3 | Overview of proposed grid-connected inverter | 122 |
| 4.4 | Circuit diagram and input and output current for the constant current source | 123 |
| 4.5 | Current wave-shaper circuit | 124 |
| 4.6 | Comparison of SMR circuit used for the DC-DC converter, and the modified SMR circuit used for the inverter | 125 |
| 4.7 | Comparison of constant and time-varying SMR duty-cycle | 125 |
| 4.8 | Unfolding circuit, and input and output currents | 126 |
| 4.9 | Inverter low-pass filter circuit, and input and output currents | 127 |
| 4.10 | Preliminary resistive / capacitive load test arrangements | 128 |
| 4.11 | Grid-connected inverter test arrangement | 129 |
| 4.12 | Grid-connected inverter test arrangement equivalent circuit | 130 |
| 4.13 | Measured transformer equivalent inductance and resistance | 130 |
| 4.14 | Photograph of an outer-rotor PM generator | 131 |
| 4.15 | I-V locus of PM generator | 132 |
| 4.16 | Photograph of power electronic components of the grid-connected inverter . | 133 |
| 4.17 | Microcontroller hardware, and software flow chart | 134 |
| 4.18 | PSIM® grid-connected inverter model | 135 |
| 4.19 | Preliminary PSIM® simulation proving the grid-connected inverter concept | 137 |
| 4.20 | Simulated effect of modulation index variation on inverter operation | 137 |
| 4.21 | Proof of inverter concept using an ideal current source | 139 |
| 4.22 | Proof of inverter concept using PM generator as current source | 140 |
| 4.23 | Effect of load resistance and generator speed on I-V locus | 142 |
| 4.24 | Inverter input and output currents for resistive load case 1 | 142 |
| 4.25 | Inverter input and output currents for resistive load case 2 | 143 |
| 4.26 | Inverter input and output currents for resistive load case 3 | 144 |
| 4.27 | Inverter output current and voltage of intermediate grid-connected case . . | 145 |
| 4.28 | Inverter output current and voltage for the pure grid-connected case | 146 |
| 4.29 | Grid-connected inverter output current for various grid voltages | 147 |
| 4.30 | Filter capacitance vs. grid voltage | 148 |
| 4.31 | Resonant frequency and quality factor vs. grid voltage | 149 |
| 4.32 | Inverter output current THD vs. grid voltage | 149 |
| 4.33 | Grid-connected inverter output current for various modulation indices . . . | 150 |
| 4.34 | Grid-connected inverter output current and voltage for various modulation indices | 151 |
| 4.35 | Inverter output current THD vs. modulation index | 152 |

| | | |
|------|--|-----|
| 5.1 | Normalised ideal and non-ideal inverter input and output currents | 156 |
| 5.2 | Output voltage of various inverter stages | 158 |
| 5.3 | Normalised ideal and experimental generator I-V loci | 158 |
| 5.4 | Derivation of normalised ideal inverter input current | 159 |
| 5.5 | Normalised inverter input and output currents for various values of $\hat{\alpha}$, using the ideal and experimental I-V loci | 161 |
| 5.6 | Effect of rectifier on normalised inverter input and output current | 161 |
| 5.7 | Effect of rectifier and fluctuating output power on the normalised ideal inverter input and output currents | 162 |
| 5.8 | Normalised inverter input and output currents for two cases of $\hat{\alpha}$ equal to 0.2pu | 163 |
| 5.9 | Effect of the fluctuating input power on the inverter output current and the harmonics for the ideal rectifier I-V locus | 165 |
| 5.10 | Effect of the fluctuating input power on the inverter output current and the harmonics for the experimental rectifier I-V locus | 165 |
| 5.11 | THD vs. $\hat{\alpha}$ comparison using the ideal and experiential locus | 166 |
| 5.12 | Output current distortion and FFT analysis, caused by the rectifier ripple . | 167 |
| 5.13 | Output current distortion and FFT analysis, caused by the rectifier ripple and fluctuating input power | 167 |
| 5.14 | Output current THD vs. modulation index for various values of $\hat{\alpha}$, using the ideal and experimental I-V loci | 168 |
| 5.15 | THD vs. $\hat{\alpha}$ comparison using the ideal and experiential locus | 169 |
| 5.16 | Turbine speed and the resulting $\hat{\alpha}_0$ vs. wind speed | 170 |
| 5.17 | Modulation index and the resulting $\hat{\alpha}$ vs. wind speed | 170 |
| 5.18 | Open-loop output current THD vs. wind pseed | 171 |
| 5.19 | Bipolar and Unipolar PWM waveforms | 172 |
| 5.20 | Harmonic spectra of the bipolar and unipolar PWM waveforms | 172 |
| 5.21 | Distortion, fundamental magnitude and THD vs. modulation index for unipolar PWM waveform | 173 |
| 5.22 | Effect of the rectifier and fluctuating input power on the inverter input and output currents | 175 |
| 5.23 | Harmonic spectrum of the inverter output current waveform | 175 |
| 5.24 | THD vs. modulation index for various values of $\hat{\alpha}_0$ | 176 |
| 5.25 | CL type low-pass filter | 177 |
| 5.26 | Normalised low-pass filter frequency response | 178 |

| | | |
|------|---|-----|
| 5.27 | Notch filter circuit | 179 |
| 5.28 | Notch filter frequency response | 179 |
| 5.29 | Typical voltage and current source inverter low-pass filter configurations | 182 |
| 5.30 | CL filter damping, using resistance | 184 |
| 5.31 | Comparison of damped CL low-pass filter gain and phase margins, for two damping resistances | 185 |
| 5.32 | LC filter gain and phase margin at the resonant frequency, for various resistances | 186 |
| 5.33 | Filter delay at the fundamental frequency vs. quality factor for various cutoff frequencies | 187 |
| 5.34 | Cutoff frequency and characteristic impedance plots vs. normalised inductance and capacitance | 190 |
| 5.35 | Harmonic spectrum of unipolar PWM waveform and filter gains of each damped low-pass filter | 191 |
| 5.36 | Unipolar PWM harmonic spectrum, showing the effect of varying the cutoff frequency on the filter gain | 192 |
| 5.37 | Unipolar PWM harmonic spectrum, showing the effect of varying the filter quality factor on the filter gain | 193 |
| 5.38 | THD vs. filter cutoff frequency and quality factor | 194 |
| 5.39 | Real, reactive and apparent power triangle corresponding to the grid power factor limits | 195 |
| 5.40 | Real and reactive power flow diagram of the inverter filter | 195 |
| 5.41 | Low-pass filter capacitance and inductance design region | 198 |
| 5.42 | Damping resistor current determined by theory of superposition | 199 |
| 5.43 | Filter power loss vs. output current THD, for various cutoff frequencies | 202 |
| 5.44 | Design Regions of each filter configuration, considering THD and power loss | 203 |
| 5.45 | THD and power loss contours within the design region of each filter type | 204 |
| 5.46 | THD vs. cutoff frequency and quality factor, showing the effects of fluctuating output power and rectifier ripple | 209 |
| 5.47 | Third-order damped low-pass filters | 210 |
| 5.48 | Inverter input and compensated output current, showing concept of feed-forward current compensation | 212 |
| 5.49 | Comparison of modulation index, and input and output currents for the uncompensated and feed-forward compensation schemes | 214 |
| 5.50 | Approximated experimental I-V locus | 215 |

| | | |
|------|---|-----|
| 5.51 | Comparison of modulation index, and input and output currents for the uncompensated and feed-forward compensation schemes | 216 |
| 5.52 | Compensated output current THD vs. rectifier ripple phase angle error . . | 218 |
| 5.53 | Summary of proposed feed-forward controller | 219 |
| 5.54 | Comparison of modulation index, and input and output currents for the uncompensated and feed-forward compensation schemes | 220 |
| 5.55 | Inverter output current THD and fundamental magnitude vs. $\hat{\alpha}_0$ using the open-loop and both feed-forward control algorithms | 221 |
| 5.56 | Comparison of inverter output current and power vs. wind speed, using both open-loop and feed-forward control algorithms | 223 |
| 6.1 | Turbine c_p curve used to calculate turbine operating speed | 228 |
| 6.2 | Inverter input and peak compensated output current | 230 |
| 6.3 | Designed machine I-V locus | 233 |
| 6.4 | Quality factor, THD, power loss and cutoff frequency tradeoff curves, used to design the 1kW grid-connected inverter | 236 |
| 6.5 | Simulated inverter output currents and voltage using an ideal current source and open-loop control | 237 |
| 6.6 | THD prediction using the PM generator current source | 239 |
| 6.7 | Simulated inverter currents using the PM generator current source and open-loop control | 239 |
| 6.8 | Relevant part of PSIM [®] circuit showing feed-forward control implementation | 242 |
| 6.9 | Feed-forward control proof of concept | 243 |
| 6.10 | Comparison of feed-forward (compensated) and open-loop inverter output currents, for 4 kHz switching case | 244 |
| 6.11 | Comparison of compensated and open-loop inverter output currents, for 10 kHz switching case | 245 |
| 6.12 | Apparent power vs. current command, for power less than rated | 246 |
| 6.13 | Inverter power factor vs. apparent power, for power less than rated | 247 |
| 6.14 | Inverter output current THD vs. apparent power, for power less than rated | 247 |
| 6.15 | Inverter input and output currents, for desired power greater than rated . . | 248 |
| 6.16 | Inverter control signals and output current, for power greater than rated . | 249 |
| 6.17 | Apparent power vs. current command for wide power range | 250 |
| 6.18 | Inverter power factor vs. entire apparent power range | 251 |
| 6.19 | Output current THD vs. entire range of apparent power | 251 |

| | | |
|------|---|-----|
| 6.20 | Wind, turbine, generator and inverter output power vs. wind speed characteristic | 252 |
| 6.21 | Turbine and generator operating characteristics vs. wind speed | 253 |
| 6.22 | Generator $\hat{\alpha}$ and $\check{\beta}$ vs. wind speed | 254 |
| 6.23 | Current command vs. wind speed for both control modes | 255 |
| 6.24 | Inverter simulation using control mode 1, for various wind speeds | 257 |
| 6.25 | Inverter simulation using control mode 2, for wind speeds beyond rated | 258 |
| 6.26 | Comparison of inverter apparent power and compensated current THD vs. wind speed characteristic, using both control modes | 259 |
| 6.27 | Inverter power loss break-down. | 260 |
| 6.28 | Inverter efficiency breakdown vs. output power | 261 |
| A.1 | Principle of sinusoidal pulse-width modulation | 270 |
| A.2 | Harmonic elimination PWM control signal | 270 |
| A.3 | Principle of current hysteresis control scheme | 271 |
| A.4 | Filter output current THD vs. power loss vs. cut-off frequency | 272 |

List of Tables

| | | |
|-----|---|-----|
| 1.1 | Net energy gain comparison of various renewable and non-renewable energy sources | 4 |
| 1.2 | Comparison of small and large scale wind turbine properties | 5 |
| 1.3 | Generator and power converter summary, used for automotive and wind power generation | 18 |
| 1.4 | Comparison of small-scale wind turbine generator DC power converters . . | 20 |
| 1.5 | Comparison of transformer and transformerless inverter properties | 36 |
| 1.6 | Comparison of inverter properties for various transformer topologies | 36 |
| 2.1 | Physical, measured and calculated PM generator properties | 66 |
| 3.1 | SMR component properties | 91 |
| 4.1 | Current harmonic limits of Australian Standard 4777.2 | 119 |
| 4.2 | Measured PM generator properties | 132 |
| 4.3 | Semiconductor properties | 136 |
| 4.4 | Simulated and measured resistive load inverter performance | 141 |
| 4.5 | Simulated and measured inverter performance for cases 1–3 | 144 |
| 5.1 | Unipolar PWM waveform harmonic analysis, for various modulation indices | 174 |
| 5.2 | Low-pass filter property comparison, for four damping resistor locations . . | 187 |
| 5.3 | Low-pass filter variable vs. parameter | 188 |
| 5.4 | Summary of apparent, real and reactive power, under grid power factor requirement extreme cases | 194 |
| 5.5 | Comparison of damping resistor current, for various filter configurations . . | 200 |
| 5.6 | Effect of varying C_n on filter design region | 206 |
| 5.7 | Effect of varying f_{sw} on filter design region | 207 |
| 6.1 | Summary of calculated turbine properties for the proposed 1kW GCI | 228 |

| | | |
|------|---|-----|
| 6.2 | Designed generator properties | 232 |
| 6.3 | Filter base quantities | 235 |
| 6.4 | Filter component values for the proposed 1kW system | 236 |
| 6.5 | Simulated inverter performance using an ideal current source | 237 |
| 6.6 | Simulated inverter performance using an the PM generator current source . | 240 |
| 6.7 | Current compensated inverter performance using the PM generator and rectifier current source | 243 |
| 6.8 | Comparison of open-loop and compensated inverter performance | 245 |
| 6.9 | Optimised inverter semiconductor properties | 256 |
| 6.10 | MOSFET vs. IGBT turn on and off times, and maximum* calculated losses | 256 |