

Experimental and Numerical Investigation of a Parallel Jet MILD Combustion Burner System in a Laboratory-scale Furnace

by

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Appendix A MILD Modelling Summary

Table A.1: MILD combustion modelling summary

Author(s)	Year	Exp. data	Burner configuration	Fuel	Software package	Turbulence model	Combustion model	Kinetic mechanism	Radiation model	NO _x model	Comments
de Joannon et al. [45]	2000	–	–	CH ₄	Chemkin	–	PSR	Warnatz (40 species + 170 reactions)	–	–	Their numerical analysis with an O ₂ content of 5% in the reactant mixture showed that MILD combustion can be represented by a two-stage oxidation process, in which the first stage occurs in rich diluted conditions, that involves species such as CO and H ₂ .
Fleck et al. [61]	2000	[171, 61]	CGRI	320 kW CH ₄	TASCflow	standard $k - \epsilon$	ED	global two-step	optically dense gas	–	Predictions of temperature, velocities and major species depart from measured values. The results suggest that reactions close to the burner exit are controlled by turbulent mixing.
Ishii et al. [95]	2000	–	Regenerative slab reheat furnace with four burners	840 kW / burner NG	Fluent	standard $k - \epsilon$	ξ / β -PDF	15 species with equilibrium	–	Post-processing thermal, and reburn	Only NO _x emissions at the exhaust were used for validation. Turbulence and super-equilibrium O atoms had a strong influence on the predictions of NO. While prompt-NO levels were not reported, reburning was found to be negligible.
Coelho et al. [32]	2001	[154, 147]	FLOX [®] (REKUMAT)	5.4 kW CH ₄	Fluent 4.8 + PIPES	standard $k - \epsilon$	EPFM	ITM-RWTH (49 species + 547 reactions)	Fluent: DTM PIPES: unsteady DO	Post-processing unsteady EPFM	Discrepancies for mean and RMS velocities. Underprediction of mean residence times close to the burner exit. NO _x was one order of magnitude lower than experiments at exhaust.
Orsino et al. [146], Mancini et al. [123]	2001, 2002	[189, 194, 193]	NFK-HRS with a pre-combustor chamber	580 kW NG	IFRF solver, Fluent 5.4	standard $k - \epsilon$	EBU, EDC, ξ / β -PDF	global two-step, 11 species with equilibrium, 13 species with equilibrium	IFRF: DTM, Fluent: DO	Post-processing thermal, and reburn	Equilibrium models did not capture flame propagation in the fuel jet region. Nonetheless, major species profiles were well predicted and NO _x at the exhaust agreed with experiments. Thermal-NO formation accounted for 95% of emissions, while reburn was negligible.

Table A.1: MILD combustion modelling summary (continued)

Author(s)	Year	Exp. data	Burner configuration	Fuel	Software package	Turbulence model	Combustion model	Kinetic mechanism	Radiation model	NO _x model	Comments
Choi & Katsuki [27]	2002	–	counter-flow laminar flat flame	CH ₄	Chemkin	–	1D laminar flame calculations	GRI-2.11	–	NO _x chemistry included	The numerical study showed that NO destruction or reburn is possible in MILD conditions due to intense mixing of the reactants with flue gases.
Evrard et al. [57]	2002	[57]	FLOX [®] (REGEMAT)	200 kW NG	Fluent 5.4	standard $k - \epsilon$ with standard wall functions	ξ / β -PDF, ED	15 species with equilibrium and global one-step	DO	Post-processing thermal and prompt	Both combustion models overpredict wall temperatures and hence radiative heat fluxes. Turbulence affected NO _x predictions, which were only qualitative, and the prompt-NO route was negligible.
Tabacco et al. [180]	2002	[180]	FLOX [®] (REKUMAT)	40 kW CH ₄	Fluent, Chemkin III	Realizable $k - \epsilon$	ξ / β -PDF, ED, PSR	equilibrium assumption, global one-step, and GRI-3.0	DO	Post-processing thermal, prompt, N ₂ O-intermediate and reburn	The equilibrium assumption is not suitable for the large ignition delays. NO _x predictions are sensitive to turbulent fluctuations and departed at least one order of magnitude from the experiments. A PSR study with detailed kinetics revealed that although thermal-NO still contributes significantly to NO formation, N ₂ O-intermediate is the main pathway.
Dally et al. [37]	2004	[37]	FLOX [®] (REKUMAT)	7 kW CH ₄ , CH ₄ /N ₂ , CH ₄ /CO ₂	Fluent + RIF solver	modified standard $k - \epsilon$ ($C_{\epsilon 1} = 1.52$)	EPFM	detailed chemistry	–	NO _x chemistry included	A comparison between measured and predicted temperatures at the furnace centreline showed fair agreement for the pure methane case and fairly large discrepancies for the CO ₂ and N ₂ dilution cases. Contour plots revealed a shift of the stoichiometric mixture fraction to higher scalar dissipation regions when fuel was diluted with inert gases.

Table A.1: MILD combustion modelling summary (continued)

Author(s)	Year	Exp. data	Burner configuration	Fuel	Software package	Turbulence model	Combustion model	Kinetic mechanism	Radiation model	NO _x model	Comments
Hekkens [87, 88, 86]	2004	[64, 2]	NFK-HRS in the reverse-flow HEC furnace	950 kW NG	Fluent 6.1	standard $k - \epsilon$ with standard wall functions	ξ / β -PDF, modified ED ($A = 0.6$, $B = 10^{23}$), EDC	equilibrium assumption, laminar flamelet concept, global four-step	DO	–	Axial velocities were consistently over-predicted for the air jet and under-predicted for the fuel jet in the near burner region for all combustion models. In general, temperatures were over-predicted with fairly large discrepancies in the reaction zone, where the weak fuel jet entrains the strong air jet. The equilibrium assumption is not suitable to represent the initial fuel jet propagation.
Park et al. [150]	2004	–	counter-flow diffusion flame	H ₂ -Air diluted with steam	Chemkin	–	1D laminar flame calculations	GRI-3.0	optically-thin approximation	NO _x chemistry included	Steam was numerically added to the air stream in mole fractions from 0.3 - 0.85. The added H ₂ O caused a significant increase in OH radicals, but as expected, thermal-NO formation decreases.
de Joannon et al. [44]	2004	–	jet stirred flow reactor	CH ₄ /O ₂ /N ₂ mixture	Chemkin 3.6	–	transient PSR - AURORA	Warnatz (34 species + 164 reactions), Battin-Leclerc & Barbe (64 species + 439 reactions)	–	–	The dynamic behaviour of CH ₄ oxidation was characterised with both measurements and modelling at a temperature range from 1000 K to 1300 K for a variety of equivalence ratios in PSR conditions. The cyclic oscillations were classified according to inlet temperatures, C/O ratios and residence times. It was reported that the CH ₃ recombination path is the major mechanism controlling the temperature oscillations. The effect of heat losses was not included.

Table A.1: MILD combustion modelling summary (continued)

Author(s)	Year	Exp. data	Burner configuration	Fuel	Software package	Turbulence model	Combustion model	Kinetic mechanism	Radiation model	NO _x model	Comments
Christo & Dally [31], Christo et al. [29, 30]	2004, 2005, 2007	[39, 38]	Jet in Hot Coflow (JHC)	80% CH ₄ + 20% H ₂ by mass	Fluent 6.2	modified standard $k - \epsilon$ ($C_{\epsilon 1} = 1.6$)	EDC, TPDF + EMST	Smooke, GRI-3.0 without NO reactions, ARM-19	DO	–	In general, the EDC model with detailed kinetic mechanisms (e.g. GRI 3.0) yielded more accurate predictions than the TPDF model for conditions representative of MILD combustion, i.e. axial distance from the jet exit lower than ≈ 100 mm and O ₂ levels in the coflow lower than 6%. At downstream locations, where the surrounding air mixes with the jet and coflow causing localised extinction, the TPDF model provided the best agreement with the experiments regardless of the kinetic mechanism used. Although turbulent mixing was accurately predicted, neither models captured the location for flame stabilisation.
Yang & Blasiak [201]	2005	[200]	HTAC burner	200 kW LPG	STAR-CD	standard $k - \epsilon$	FRED	global five-step	DTM	Post-processing thermal, N ₂ O, N ₂ O ₂ and reburn	A comparison with NO _x emission measurements showed that NO predictions can be significantly improved when the N ₂ O-intermediate pathway is considered for excess air ratios (λ) less than 15%. NO _x emissions are overpredicted by a factor of two for $\lambda = 25\%$ due to the higher temperatures, which trigger the thermal-NO route. To decrease the discrepancies at high temperatures, the deactivation of the N ₂ O mechanism for temperatures above 1850 K was proposed.

Table A.1: MILD combustion modelling summary (continued)

Author(s)	Year	Exp. data	Burner configuration	Fuel	Software package	Turbulence model	Combustion model	Kinetic mechanism	Radiation model	NO _x model	Comments
Glagas et al. [68]	2005	[21]	Cabra burner	H ₂	joint scalar PDF solver	modified $k - \epsilon$ ($C_{\epsilon 2} = 1.8$)	TPDF + modified Curl	Li et al. [112]	–	–	A low temperature pre-ignition region was characterised by peak values of H ₂ O ₂ and HO ₂ , while high concentrations of O, H, and OH radicals were an indication of autoignition. The modelling results showed that the TPDF approach was able to predict the ignition phenomena for diluted conditions similar to MILD combustion.
Christo & Dally [28]	2005	[39, 38]	Jet in Hot Coflow (JHC)	80% CH ₄ + 20% H ₂ by mass	Fluent 6.2	standard $k - \epsilon$, RNG $k - \epsilon$, Realizable $k - \epsilon$, modified standard $k - \epsilon$ ($C_{\epsilon 1} = 1.6$)	laminar flamelet, ξ / β -PDF, FRED, EDC	Three-step global, Smooke, GRI-3.0 without NO reactions	DO	–	The modified $k - \epsilon$ provided the best agreement. Conserved scalar type models are inadequate for MILD conditions. For better accuracy detailed kinetic mechanisms must be used and differential diffusion effects should always be included.
Kim et al. [100]	2005	[39, 38]	Jet in Hot Coflow (JHC)	80% CH ₄ + 20% H ₂ by mass	VODE solver with a laminar flamelet library	modified standard $k - \epsilon$ ($C_{\epsilon 1} = 1.5$)	CMC	GRI-2.11	–	NO _x chemistry included	A single mixture fraction parameter was used to define a three-stream mixing problem. Model predicted major species and temperatures reasonably well. Good predictions of NO profiles.
Awsospe & Lockwood [10]	2005	[199, 189, 111]	FLOX [®] , NFK-HRS with a pre-combustor chamber, TECHNION afterburner	CH ₄ , 50% C ₃ H ₄ + 50% C ₄ H ₁₀ by volume	FAFNIR-3D	standard $k - \epsilon$	ξ / β -PDF, laminar flamelet	CH ₄ : Warnatz (28 species + 72 reactions), C ₃ H ₈ + C ₄ H ₁₀ : Marinov [124] (36 species + 200 reactions)	noneq. diffusion	Post-processing thermal, and prompt	Local extinction was important when high momentum jets are used to induce internal flue gas recirculation for strong dilution. Only qualitative agreement was found for CO profiles. The prompt-NO route was found to be negligible.

Table A.1: MILD combustion modelling summary (continued)

Author(s)	Year	Exp. data	Burner configuration	Fuel	Software package	Turbulence model	Combustion model	Kinetic mechanism	Radiation model	NO _x model	Comments
Yang & Blasiak [202]	2005	–	Single fuel jet in a oxygen deficient high temperature cross-flow	0.5 kW C ₃ H ₈	STAR-CD	RNG $k - \epsilon$	ED, modified ED ($A = 1$, $B = 0.5$) ($A = 2$, $B = 0.5$), ξ / β -PDF	global three-step, 11 species with equilibrium	DTM	Post-processing thermal, and prompt	The empirical constant A in the ED model was changed to slow combustion rates. The numerical analysis showed an increased reaction zone volume for 5% O ₂ levels in the cross-flow air. The low oxygen concentrations decreased NO formation, despite the fact that the fuel residence time in the reaction zone increased.
Nicolle & Dagaut [141]	2006	–	–	CH ₄	Chemkin 4.0	–	PSR, PaSR, PFR - Senkin	skeletal mechanism derived from [35] (95 species + 265 reactions), GRI-3.0, Konnov-0.5	–	NO _x chemistry included	The kinetic modelling analysis showed the sequential nature of the nitrogen chemistry at constant temperature in MILD conditions. During the ignition period, the NO-HCN conversion reactions are particularly active. The NO-reburning mechanism is mainly related to the fuel-ignition chemistry and depends on the equivalence ratio and mixing times. In the post-ignition period, the thermal-NO and N ₂ O-intermediate pathways increase in importance.
Sabia et al. [163]	2007	[44, 42]	jet stirred flow reactor	CH ₄ -H ₂ /O ₂ /N ₂ mixture	Chemkin 3.7	–	transient PSR - AURORA	(34 species + 164 reactions), (99 species + 734 reactions)	–	–	The effect of hydrogen addition on methane combustion was studied for MILD conditions. As expected, the addition of H ₂ in molar fractions from 0.25% to 0.9% caused an increase in reactivity and a reduction of instabilities related to thermokinetic temperature oscillations.
Galletti et al. [67]	2007	[67]	Enel radiant tube	13 kW CH ₄	CFX 5.7	modified standard $k - \epsilon$ ($C_{\epsilon 1} = 1.6$)	FRED	global one-step	DTM	Post-processing thermal and prompt	Only wall temperatures are available for validation. An axisymmetric model overestimated K_V in the burner by 15-20% when compared to a 3D model. Despite the difference, a regression equation for NO emissions as a function of K_V is proposed.

Table A.1: MILD combustion modelling summary (continued)

Author(s)	Year	Exp. data	Burner configuration	Fuel	Software package	Turbulence model	Combustion model	Kinetic mechanism	Radiation model	NO _x model	Comments
Dally & Peters [36]	2007	–	–	CH ₄ /O ₂ /N ₂ mixture	Chemkin 4.1	–	transient PSR - AURORA	GRI 3.0, Smooke	–	–	The PSR calculations for CH ₄ and C ₂ H ₄ at a low temperature range of 1000 K to 1300 K showed that temperature oscillations are independent of the inlet temperature. It was also found that oscillations are controlled by a radical scavenging mechanism followed by heat loss to the surroundings, rather than a recombination channel.
Kumar et al. [107]	2007	[105, 106]	High intensity low-emission burner	3 kW and 150 kW C ₃ H ₈	CFX 5.6	standard $k - \epsilon$	EDC	skeletal mechanism	–	–	A flame extinction criteria was initially proposed to predict the lift-off height of CH ₄ , C ₃ H ₈ and H ₂ flames and then used capture the flame propagation in a MILD burner. Essentially, if $Da < 1$ then the average reaction rate was set to zero in the EDC model. Temperatures were overpredicted by ≈ 200 K throughout the furnace for the 3 kW case. The overprediction of O ₂ concentrations at a downstream location, and particularly on the fuel jet region, implies that the reaction zone structure is not fully captured. No velocity data was available for validation.
Mancini et al. [122]	2007	[189, 194, 193]	NFK-HRS with a pre-combustor chamber	580 kW NG	IFRF solver, Fluent 5.4, Chemkin 3.7	standard $k - \epsilon$, RNG	EBU, ξ/β -PDF, PSR network	global two-step, 13 species with equilibrium, & GRI-3.0	IFRF: DTM, Fluent: DO	Post-processing thermal, prompt and reburn	The failure of RANS models to predict the weak fuel jet structure is due to discrepancies in predicting entrainment. There is little combustion within the fuel jet, which means the temperature increase and the presence of NO is a result of entrainment.

Table A.1: MILD combustion modelling summary (continued)

Author(s)	Year	Exp. data	Burner configuration	Fuel	Software package	Turbulence model	Combustion model	Kinetic mechanism	Radiation model	NO ₂ model	Comments
Lupant et al. [117]	2007	[57, 118, 117]	FLOX [®] (REGEMAT)	200 kW NG	Fluent 6.1	standard $k - \epsilon$ with standard wall functions	ED, FRED, modified ED ($A = 0.6$, $B = 10^{10}$), ξ / β -PDF	global one-step, global two-step, 15 species with equilibrium	DO	Post-processing thermal and prompt	Temperatures were largely overpredicted in the near burner region for all combustion models. Using the measured air inlet temperature as an input and modifying the empirical constants in the ED model resulted in a better agreement. However, the location of the reaction zone was not captured based on O ₂ profiles and OH visualisation. Exhaust NO ₂ was on the same order of magnitude than in the experiments.
Duwig et al. [54]	2008	[54]	Flameless gas turbine combustor	460 kW C ₃ H ₈	LES code + Cantera	LES	chemistry tabulated with PSR calculations	San Diego (46 species + 235 reactions)	–	–	The numerical results provided an insight into the unsteady aerodynamics of the flameless combustor. The analysis determined that the unburned gases entrained the same amount of combustion products before reaction, meaning a 0.5 global dilution rate.
Kim et al. [99]	2008	[189, 194, 193]	NFK-HRS with a pre-combustor chamber	580 kW NG	AIOLOS-3D	standard $k - \epsilon$	EDC	global three-step, global four-step	DO	Thermal, prompt, and reburn	A comparison of four different global reaction mechanisms for CH ₄ showed fairly large discrepancies in the near burner region for temperature and major species. To improve the predictions a modified Jones and Lindstedt mechanism [97] was proposed. Although a better agreement was seen for CO and H ₂ , the global mechanism still did not capture the weak fuel jet structure. No information on the relative contribution of each NO formation pathway was presented.

Appendix B Temperature Correction

B.1 Methodology

The correction to the temperature measurements for radiation was determined from a steady-state energy balance on the thermocouple bead surface. The actual gas temperature (T_g) was determined from the measured temperature (T_{tcb}) and net radiation flux between diffuse-gray surfaces in an enclosure according to

$$T_g = T_{tcb} + \frac{A_{tcb}\epsilon_{tcb} \sum_{w=1}^N \sigma G_{1w} (T_{tcb}^4 - T_w^4)}{h}, \quad (\text{B.1})$$

where A_{tcb} is the thermocouple bead surface area, ϵ_{tcb} is the thermocouple bead surface emissivity, N is the total number of surfaces (i.e. walls) in the enclosure, σ is the Stefan-Boltzmann constant, G_{1w} is the fraction of radiation emitted by the thermocouple bead that is incident on a particular wall surface w in the furnace enclosure and is absorbed [168], T_w is the surface temperature of wall w in the enclosure, and h is the convection coefficient. Catalytic and oxidation effects were neglected, as well as conductive heat transfer along the ceramic sheath.

The convective heat transfer coefficient, h , was calculated for a sphere from the expression [91];

$$Nu = \frac{hD_{tcb}}{k} = 2 + (0.4Re^{1/2} + 0.06Re^{2/3}) Pr^{0.4} \left(\frac{\mu}{\mu_s} \right)^{1/4} \quad (\text{B.2})$$

$$\left[\begin{array}{l} 0.71 < Pr < 380 \\ 3.5 < Re < 7.6 \times 10^{-4} \\ 1.0 < \left(\frac{\mu}{\mu_s} \right) < 3.2 \end{array} \right]$$

where D_{tcb} is the thermocouple bead diameter, Nu is the Nusselt number, Re is the Reynolds number, Pr is the Prandtl number, k is the thermal conductivity, and μ is the dynamic viscosity. Air was used to approximate furnace gas properties for determining the parameters of equation B.2. The air jet bulk velocity (U) was used to calculate the Reynolds number. All properties were evaluated at T_{tcb} , except μ_s , which was evaluated at the film temperature defined as

$$T_f = \frac{T_{tcb} + T_{air}}{2}. \quad (\text{B.3})$$

The thermocouple bead diameter (D_{tcb}) was determined from an image obtained with an Olympus BX60MF microscope using a $5\times$ magnification objective. The image was processed with an open source image manipulation program. Figure B.1 shows the original image and processed image used to determine D_{tcb} . First, the process involved converting the image to a grayscale and applying an edge detection and enhancement algorithm to sharpen the image and reveal the circumference of the bead. Then, a calibration disc with a 1 mm scale was used to find a pixel-to-length ratio for images taken at a $5\times$ magnification and generate a marker. Finally, the average circumference of the bead (red circle) was compared to the marker size, resulting in $D_{tcb} \approx 1.2$ mm.

The G_{1w} correction factor was obtained for each probe position by matrix inversion from a system of equations (equation 6.37 of Ref. [168]) written in compact notation as

$$[G_{kw}] = m^{-1}f; \quad m = \delta_{kw} + (\epsilon_w - 1)F_{kw}; \quad f = \epsilon_w F_{kw}; \quad (\text{B.4})$$

where $1 \leq k \leq 7$, ϵ_w is the emissivity for surface w , F_{kw} is the configuration or view factor between surface k and w of the enclosure, δ_{kw} is the Kronecker delta, defined as

$$\delta_{kw} = \begin{cases} 1, & k = w \\ 0, & k \neq w \end{cases} \quad (\text{B.5})$$

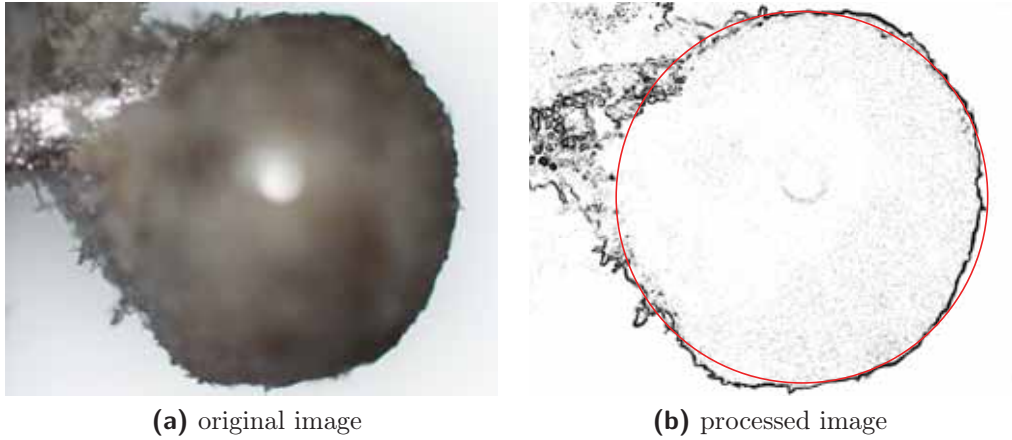


Figure B.1: Images used to determine the thermocouple bead diameter. The red circle represents the average circumference of the bead.

The bead emissivity used in the calculations was $\epsilon_1 = 0.22$, which is based on acceptable values of small diameter platinum-rhodium wires [83, 175], and the furnace wall emissivity was $\epsilon_2 = \epsilon_3 = \epsilon_4 = \epsilon_5 = \epsilon_6 = \epsilon_7 = 0.93$, which is the value provided by the manufacturer of the insulation material. This procedure always resulted in corrected temperatures lower than the adiabatic flame temperature.

B.2 Error Propagation

Some degree of uncertainty is associated with the methodology described in the previous section, since the parameters used in the calculations (equation B.1) are not precisely known. The errors introduced by each parameter will affect the resulting final gas temperature. A common approach to determine the total uncertainty (ΔT_g) is through an error propagation analysis. In this analysis, an estimated deviation is attributed to each parameter (Table B.1) and the propagation of errors is calculated from the following expression:

$$\Delta f = \sqrt{\sum_{i=1}^n \left(\frac{\partial f}{\partial a_i} \cdot \Delta a_i \right)^2} \quad (\text{B.6})$$

$$\Delta T_g = \sqrt{\left(\frac{\partial T_g}{\partial T_w} \cdot \Delta T_w \right)^2 + \left(\frac{\partial T_g}{\partial \epsilon_{tcb}} \cdot \Delta \epsilon_{tcb} \right)^2 + \left(\frac{\partial T_g}{\partial D_{tcb}} \cdot \Delta D_{tcb} \right)^2 + \left(\frac{\partial T_g}{\partial U} \cdot \Delta U \right)^2}.$$

Table B.1: Estimated uncertainty of the parameters used to calculate the temperature correction

Parameter (a_i)	Unit	Δ
T_w	°C	±10%
ϵ_{tcb}	–	±15%
D_{tcb}	mm	±5%
U	m/s	±5%

The results of the error estimation procedure are shown in Table B.2, where δ represents the correction between raw and actual gas temperatures in absolute and relative terms.

Table B.2: Error estimates for in-furnace temperature data for the baseline operating conditions

TC position			$T_{air} = 25^\circ\text{C}$			$T_{air} = 450^\circ\text{C}$		
x	y	z	δ	δ	ΔT_g	δ	δ	ΔT_g
(mm)	(mm)	(mm)	(°C)	(%)	(%)	(°C)	(%)	(%)
-100	0	42.5	-40.2	-3.3	1.3	-8.6	-0.7	1.2
-100	55	42.5	-39.2	-3.2	1.3	-13.4	-1.1	1.2
-100	110	42.5	-37.7	-3.1	1.3	-8.7	-0.7	1.2
-100	140	42.5	-30.4	-2.6	1.3	-1.2	-0.1	1.3
-100	0	142.5	-43.6	-3.6	1.2	-16.6	-1.3	1.1
-100	55	142.5	-40.8	-3.4	1.2	-16.2	-1.3	1.1
-100	110	142.5	-41.7	-3.4	1.2	-8.4	-0.7	1.2

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Table B.2: Error estimates for in-furnace temperature data for the baseline operating conditions (continued)

TC position			$T_{air} = 25^{\circ}\text{C}$			$T_{air} = 450^{\circ}\text{C}$		
x	y	z	δ	δ	ΔT_g	δ	δ	ΔT_g
(mm)	(mm)	(mm)	($^{\circ}\text{C}$)	(%)	(%)	($^{\circ}\text{C}$)	(%)	(%)
-100	140	142.5	-25.4	-2.2	1.3	-8.8	-0.7	1.2
-100	0	242.5	-31.8	-2.7	1.3	4.4	0.4	1.4
-100	55	242.5	-37.2	-3.1	1.3	-6.7	-0.5	1.2
-100	110	242.5	-43.0	-3.5	1.2	-12.0	-1.0	1.2
-100	140	242.5	-23.1	-2.0	1.4	5.3	0.5	1.4
-100	0	342.5	-16.2	-1.4	1.4	3.3	0.3	1.3
-100	55	342.5	-31.8	-2.7	1.3	-7.3	-0.6	1.2
-100	110	342.5	-41.5	-3.4	1.2	-15.0	-1.2	1.1
-100	140	342.5	-17.5	-1.5	1.4	6.3	0.5	1.3
-100	0	442.5	-28.3	-2.4	1.3	-6.8	-0.6	1.2
-100	55	442.5	-33.6	-2.8	1.3	-9.0	-0.7	1.2
-100	110	442.5	-35.6	-3.0	1.3	-10.6	-0.9	1.1
-100	140	442.5	-15.5	-1.4	1.4	2.3	0.2	1.3
-100	0	542.5	-26.2	-2.2	1.3	-8.5	-0.7	1.2
-100	55	542.5	-27.7	-2.4	1.3	-10.2	-0.8	1.1
-100	110	542.5	-25.9	-2.2	1.3	-11.8	-0.9	1.1
-100	140	542.5	-18.8	-1.6	1.4	-5.5	-0.4	1.2
0	0	42.5	80.1	11.7	3.0	73.8	9.1	2.6
0	55	42.5	-33.4	-2.8	1.3	-11.5	-0.9	1.2
0	110	42.5	-1.4	-0.1	1.5	33.7	3.2	1.8
0	140	42.5	-17.2	-1.5	1.4	7.7	0.7	1.4
0	0	142.5	8.8	0.8	1.6	30.3	2.8	1.7
0	55	142.5	-22.7	-2.0	1.4	-20.7	-1.6	1.1
0	110	142.5	-39.7	-3.3	1.3	-11.8	-0.9	1.2
0	140	142.5	-26.4	-2.3	1.3	-2.8	-0.2	1.3
0	0	242.5	-22.9	-2.0	1.4	4.2	0.4	1.4
0	55	242.5	-21.3	-1.8	1.4	-15.7	-1.2	1.1

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Table B.2: Error estimates for in-furnace temperature data for the baseline operating conditions (continued)

TC position			$T_{air} = 25^{\circ}\text{C}$			$T_{air} = 450^{\circ}\text{C}$		
x	y	z	δ	δ	ΔT_g	δ	δ	ΔT_g
(mm)	(mm)	(mm)	($^{\circ}\text{C}$)	(%)	(%)	($^{\circ}\text{C}$)	(%)	(%)
0	110	242.5	-45.1	-3.7	1.2	-19.5	-1.5	1.1
0	140	242.5	-44.5	-3.6	1.2	-1.3	-0.1	1.3
0	0	342.5	-24.3	-2.1	1.3	-3.5	-0.3	1.2
0	55	342.5	-24.0	-2.1	1.4	-13.0	-1.0	1.1
0	110	342.5	-50.8	-4.1	1.2	-26.6	-2.0	1.0
0	140	342.5	-28.8	-2.4	1.3	-6.8	-0.6	1.2
0	0	442.5	-24.3	-2.1	1.3	-6.0	-0.5	1.2
0	55	442.5	-27.2	-2.3	1.3	-10.1	-0.8	1.1
0	110	442.5	-35.8	-3.0	1.3	-15.7	-1.2	1.1
0	140	442.5	-17.6	-1.5	1.4	-2.5	-0.2	1.2
0	0	542.5	-15.3	-1.3	1.3	-3.7	-0.3	1.2
0	55	542.5	-16.6	-1.5	1.3	-7.3	-0.6	1.2
0	110	542.5	-17.6	-1.5	1.3	-10.2	-0.8	1.1
0	140	542.5	-9.3	-0.8	1.4	-0.6	0	1.3
100	0	42.5	-41.6	-3.4	1.2	-15.4	-1.2	1.1
100	55	42.5	-38.2	-3.2	1.3	-13.5	-1.1	1.2
100	110	42.5	-39.4	-3.3	1.3	-14.6	-1.2	1.2
100	140	42.5	-27.4	-2.3	1.3	-2.7	-0.2	1.3
100	0	142.5	-51.8	-4.1	1.2	-15.9	-1.3	1.1
100	55	142.5	-49.1	-4.0	1.2	-22.5	-1.7	1.1
100	110	142.5	-51.3	-4.1	1.2	-21.8	-1.7	1.1
100	140	142.5	-29.8	-2.5	1.3	-6.5	-0.5	1.2
100	0	242.5	-44.0	-3.6	1.2	-22.8	-1.8	1.1
100	55	242.5	-50.6	-4.1	1.2	-24.2	-1.9	1.1
100	110	242.5	-49.9	-4.0	1.2	-20.3	-1.6	1.1
100	140	242.5	-29.4	-2.5	1.3	-4.7	-0.4	1.3
100	0	342.5	-30.4	-2.6	1.3	-13.2	-1.0	1.1

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Table B.2: Error estimates for in-furnace temperature data for the baseline operating conditions (continued)

TC position			$T_{air} = 25^{\circ}\text{C}$			$T_{air} = 450^{\circ}\text{C}$		
x	y	z	δ	δ	ΔT_g	δ	δ	ΔT_g
(mm)	(mm)	(mm)	($^{\circ}\text{C}$)	(%)	(%)	($^{\circ}\text{C}$)	(%)	(%)
100	55	342.5	-31.6	-2.7	1.3	-17.5	-1.4	1.1
100	110	342.5	-36.0	-3.0	1.3	-13.8	-1.1	1.1
100	140	342.5	-20.6	-1.8	1.4	-13.0	-1.0	1.1
100	0	442.5	-23.0	-2.0	1.4	-7.6	-0.6	1.2
100	55	442.5	-22.3	-1.9	1.4	-11.0	-0.9	1.1
100	110	442.5	-23.6	-2.0	1.4	-9.6	-0.8	1.1
100	140	442.5	-15.7	-1.4	1.4	1.7	0.1	1.3
100	0	542.5	-21.3	-1.8	1.3	-4.8	-0.4	1.2
100	55	542.5	-16.8	-1.5	1.3	-7.7	-0.6	1.2
100	110	542.5	-16.7	-1.5	1.3	-8.4	-0.7	1.2
100	140	542.5	-13.6	-1.2	1.4	-1.4	-0.1	1.2

Appendix C Control Logic

This is a simplified flowdiagram that illustrates the main steps involved in the logic integrated in the BMS that controls the MILD combustion burner system.

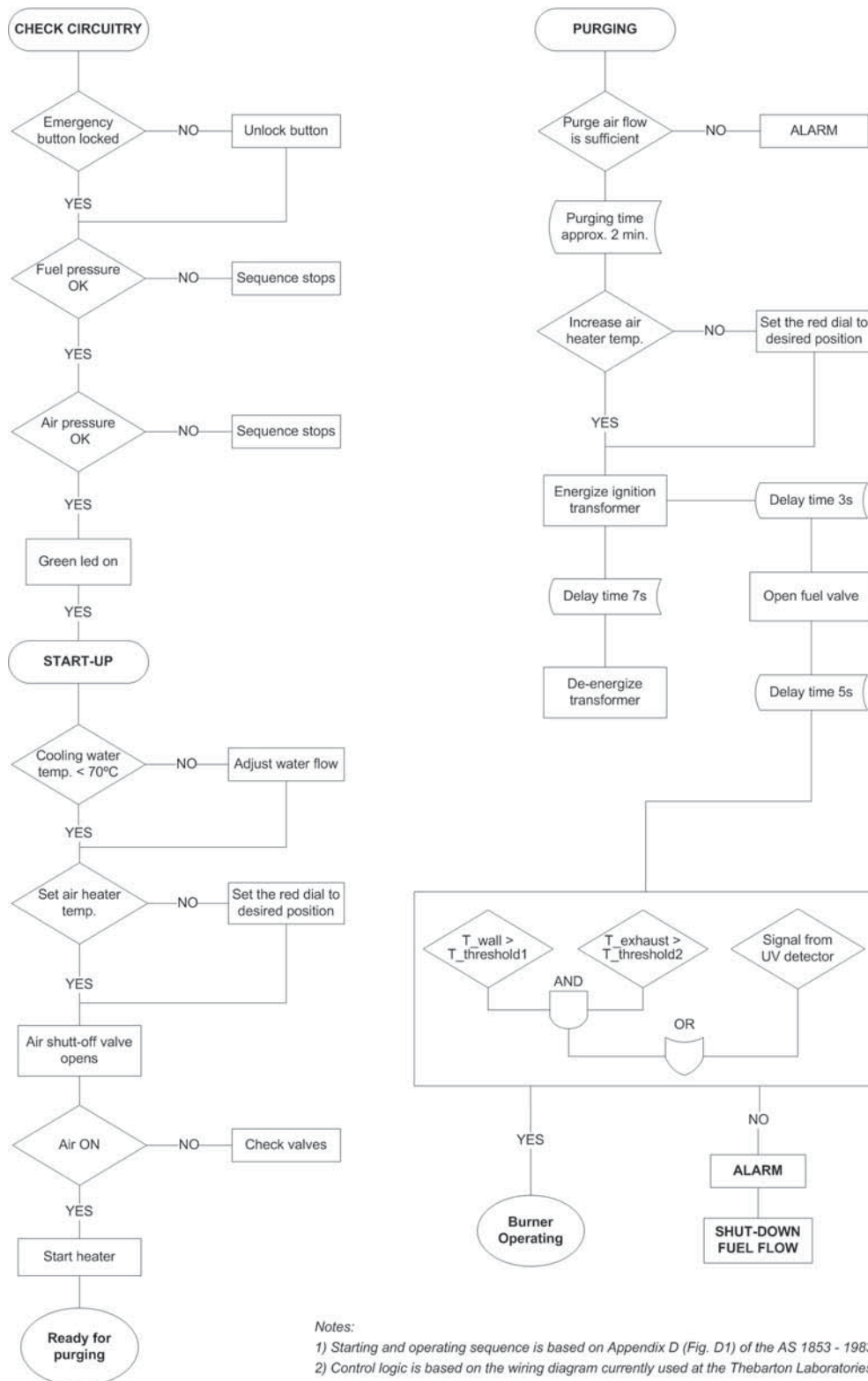


Figure C.1: Flowdiagram of the control logic integrated in the burner management system (BMS).

Appendix D Particle Size Distribution

This histogram shows the particle size distribution of the fused white alumina powder used to seed the central air jet for the LDA measurements. The particle size analysis was carried out by Pulver Technology Ltd., which is the company that supplied the seeding material.

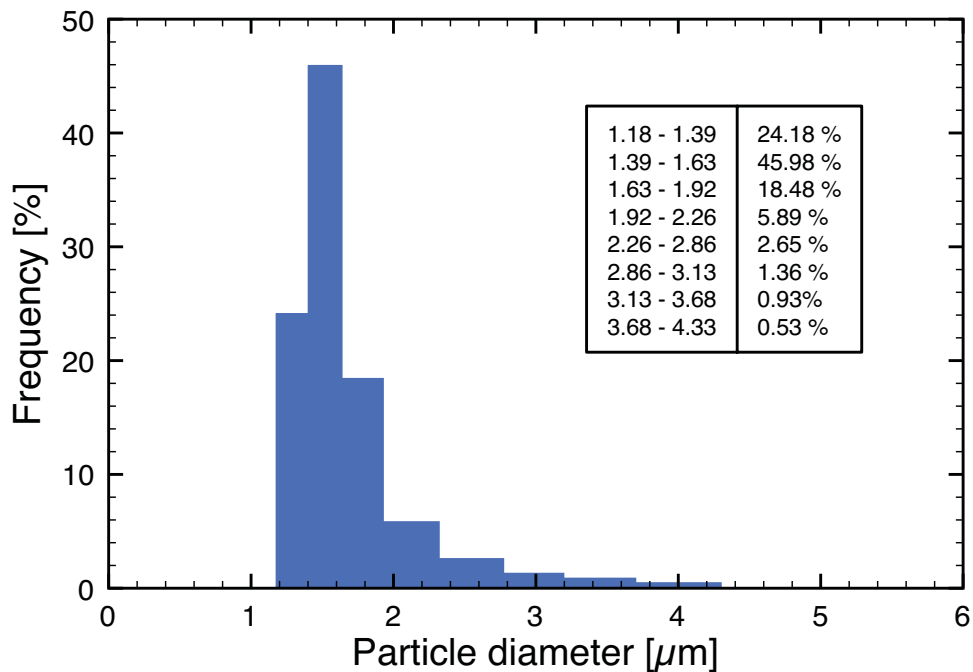


Figure D.1: Al₂O₃ particle size distribution. (*Source:* Pulver Technology Ltd.)

Appendix E Velocity for Nonreacting Isothermal Conditions

The results presented in Figures 7.1 through 7.4 are repeated here for convenience to show the comparison for the realizable $k - \epsilon$ turbulence model alone.

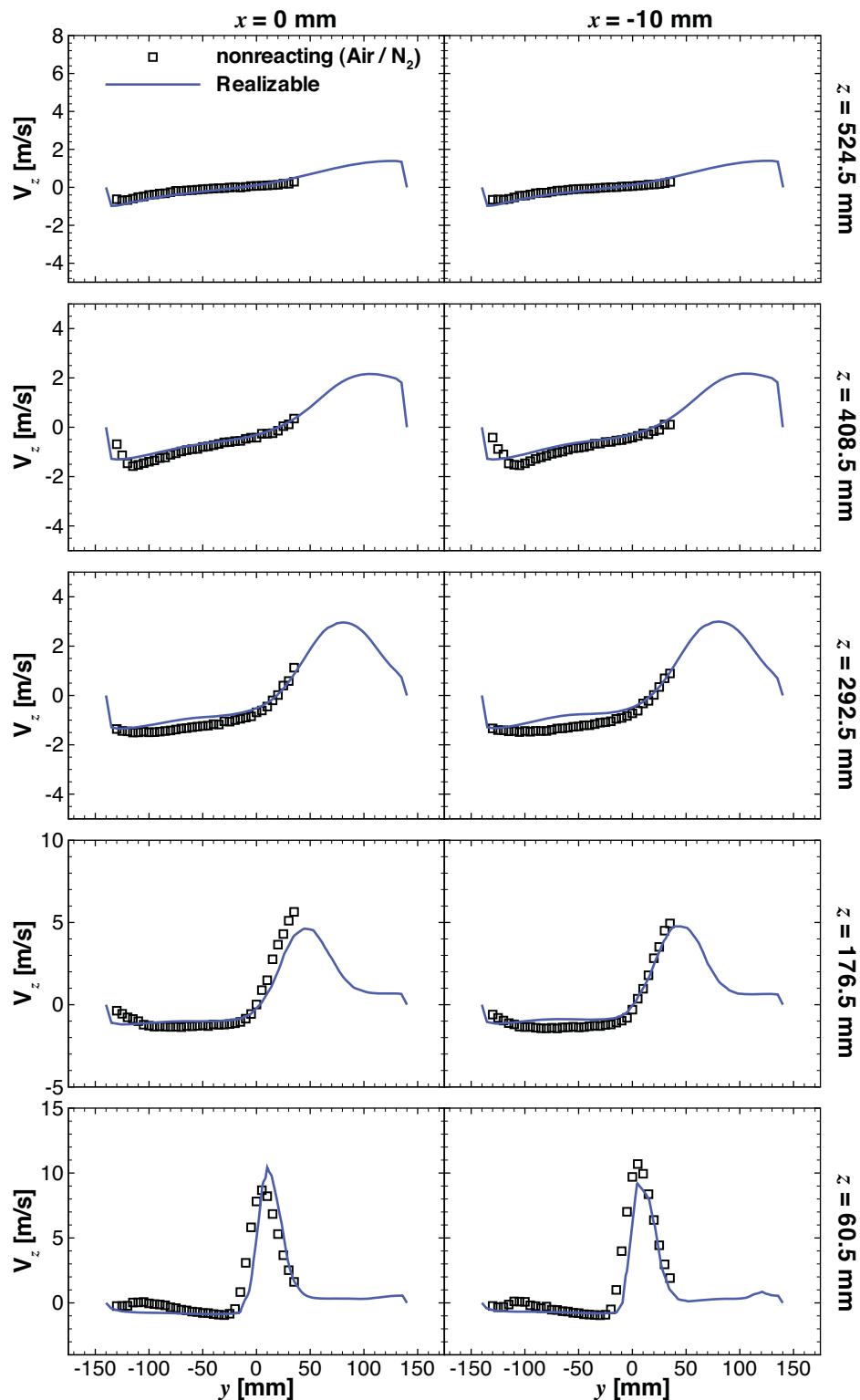


Figure E.1: Comparison of measured (open symbols) and predicted (blue lines) mean axial velocity (V_z) profiles across the y -axis for nonreacting conditions at $x = 0$ (left) and $x = -10$ (right) for the realizable $k - \epsilon$ turbulence model at various axial locations.

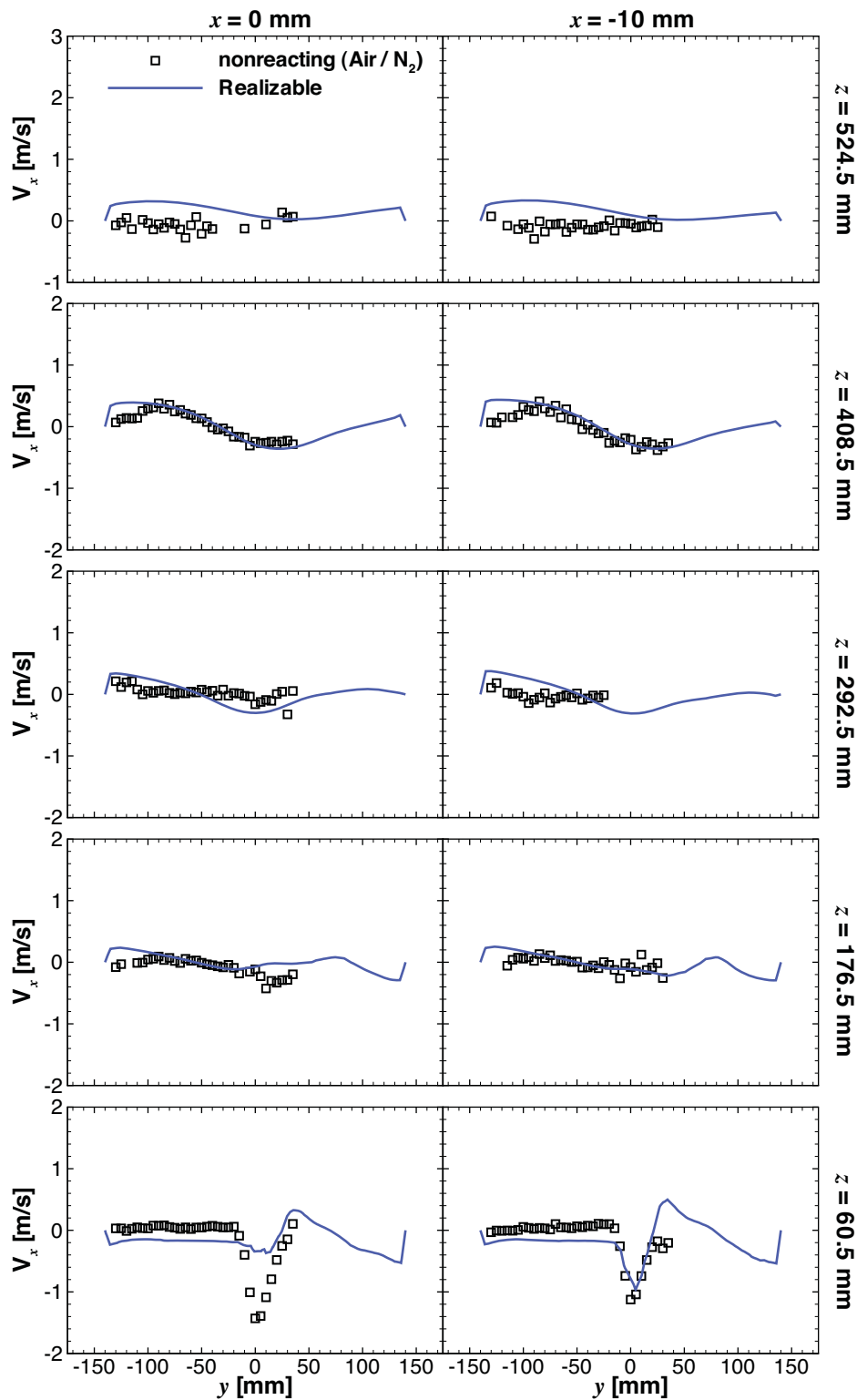


Figure E.2: Comparison of measured (open symbols) and predicted (blue lines) mean radial velocity (V_x) profiles across the y -axis for nonreacting conditions at $x = 0$ (left) and $x = -10$ (right) for the realizable $k - \epsilon$ turbulence model at various axial locations.

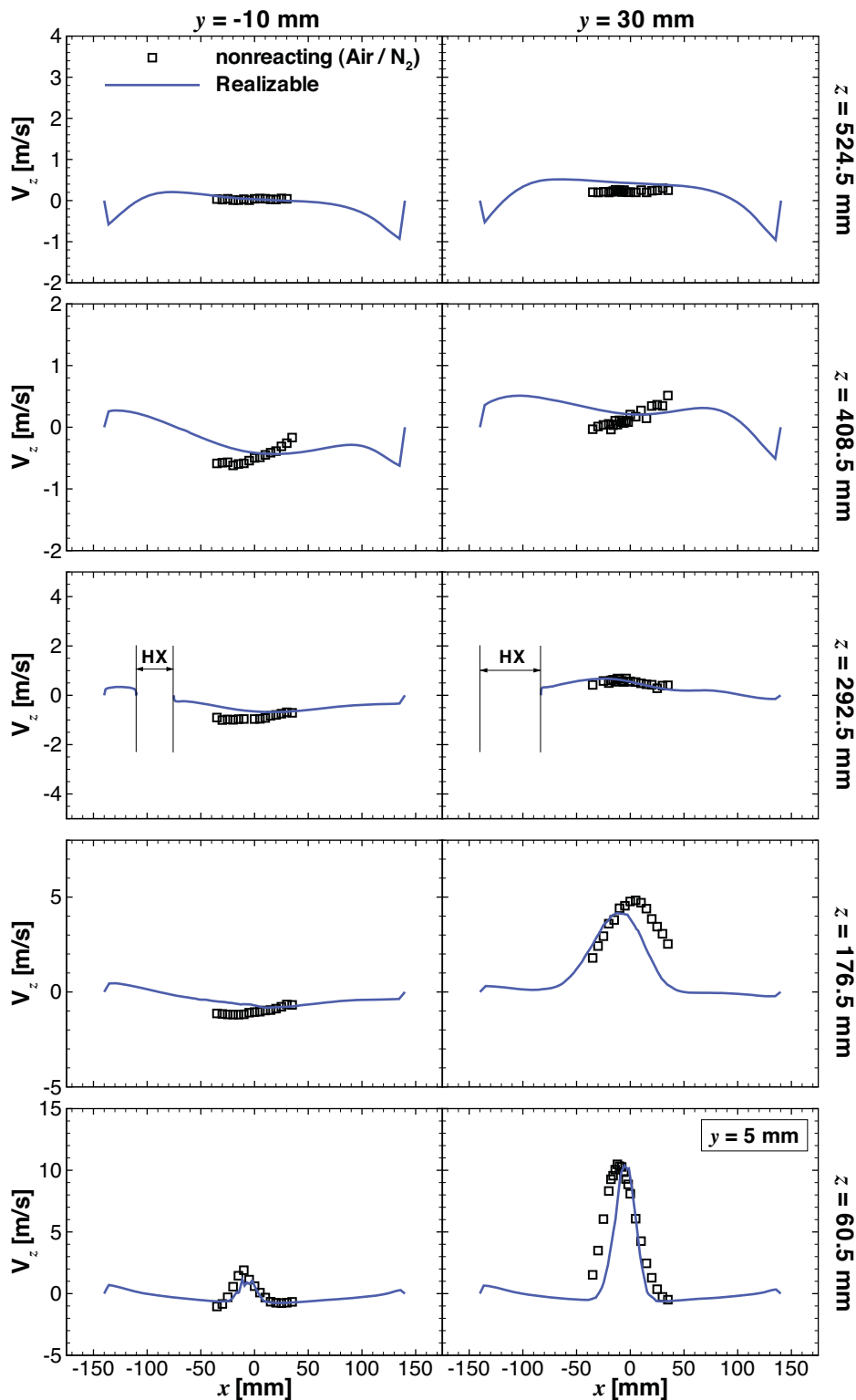


Figure E.3: Comparison of measured (open symbols) and predicted (blue lines) mean axial velocity (V_z) profiles across the x -axis for nonreacting conditions at $y = -10$ (left) and $y = 30$ (right) with the exception of $y = 5$ (lower right) for the realizable $k - \epsilon$ turbulence model at various axial locations.

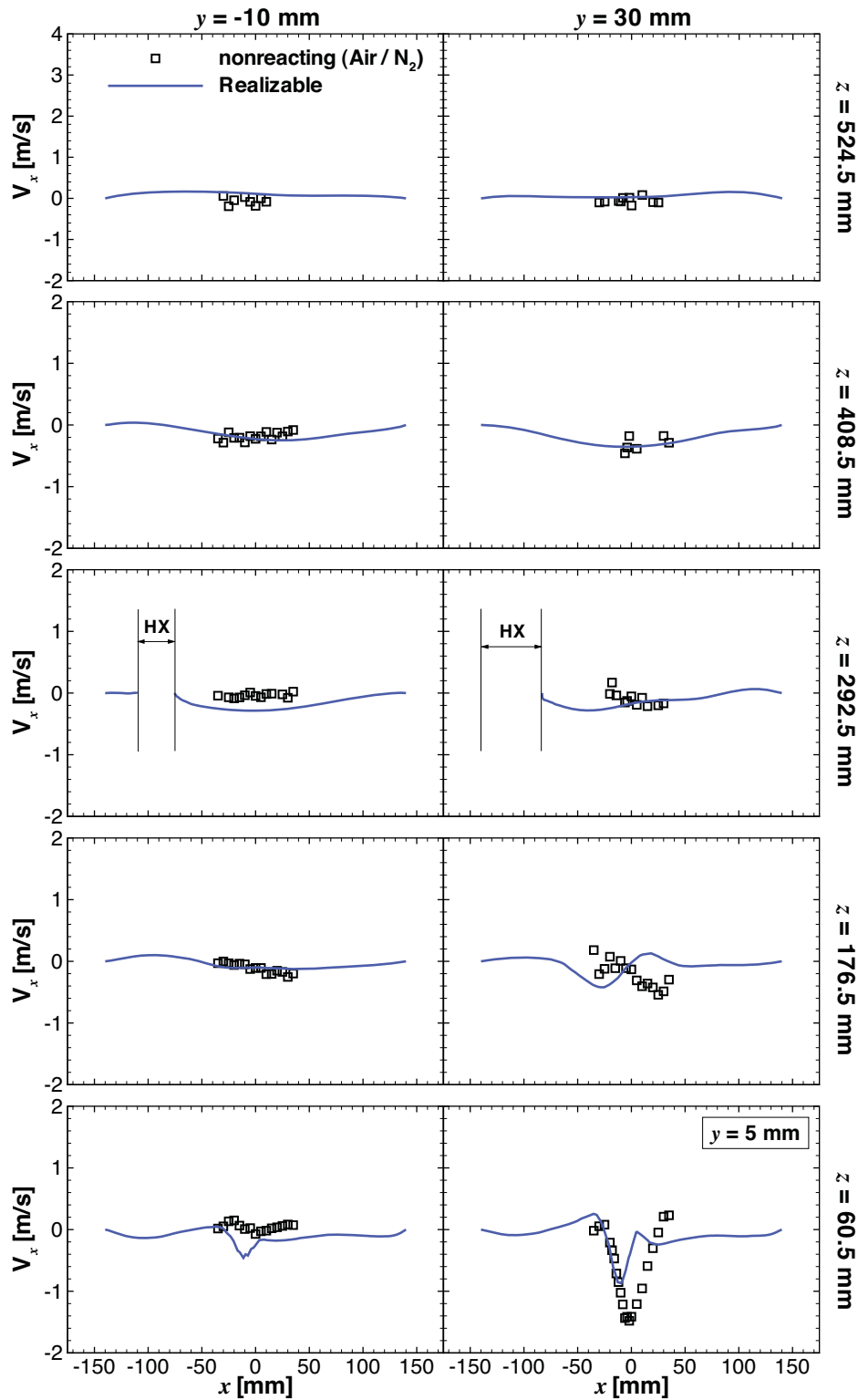


Figure E.4: Comparison of measured (open symbols) and predicted (blue lines) mean radial velocity (V_x) profiles across the x -axis for nonreacting conditions at $y = -10$ (left) and $y = 30$ (right) with the exception of $y = 5$ (lower right) for the realizable $k - \epsilon$ turbulence model at various axial locations.

Appendix F Compositional Structure Contours

It must be noted that the mole fraction contours of all species presented in this Appendix are displayed on a wet basis.

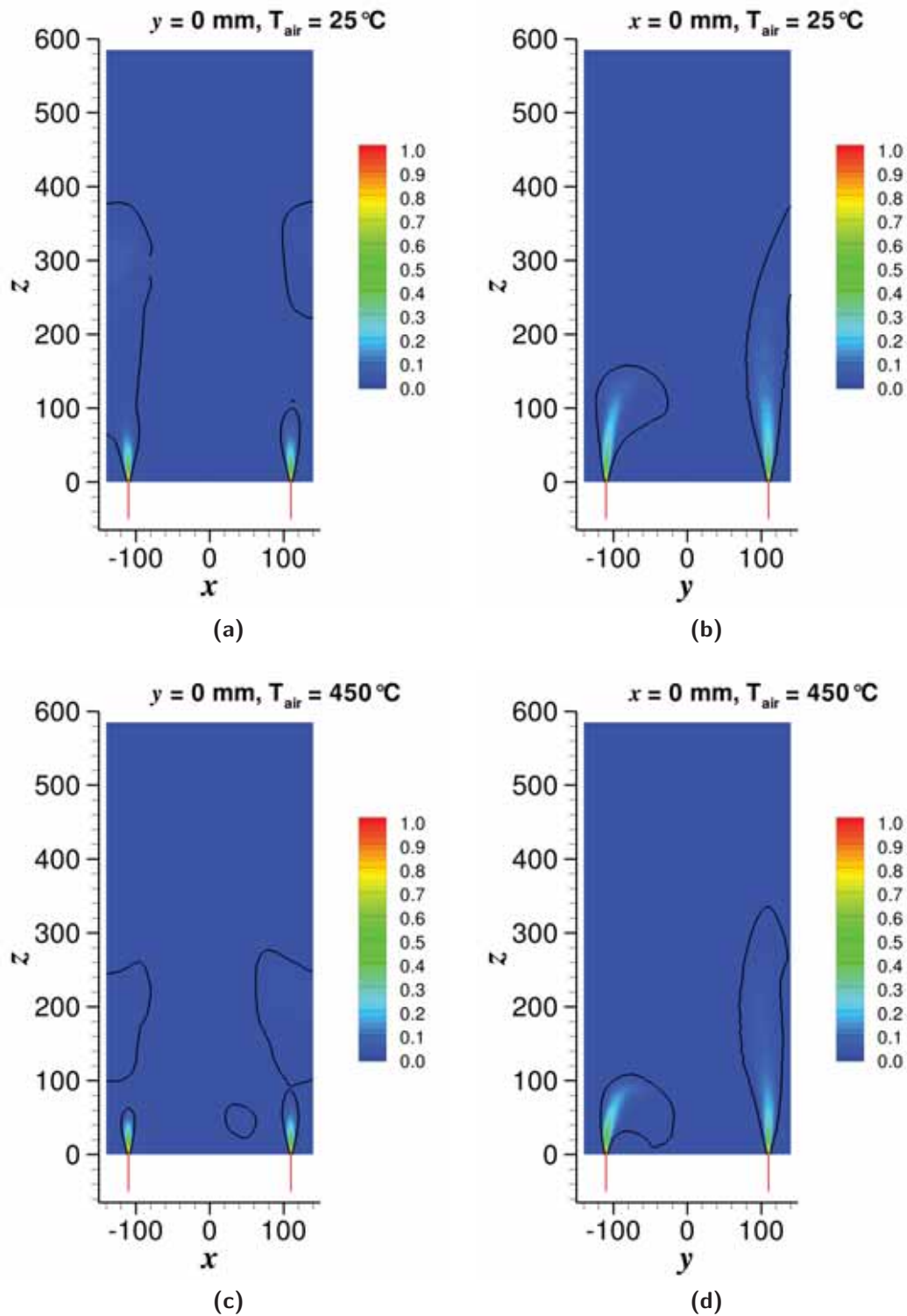


Figure F.1: Predicted CH₄ mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at the $x - z$ and $y - z$ centreline planes.

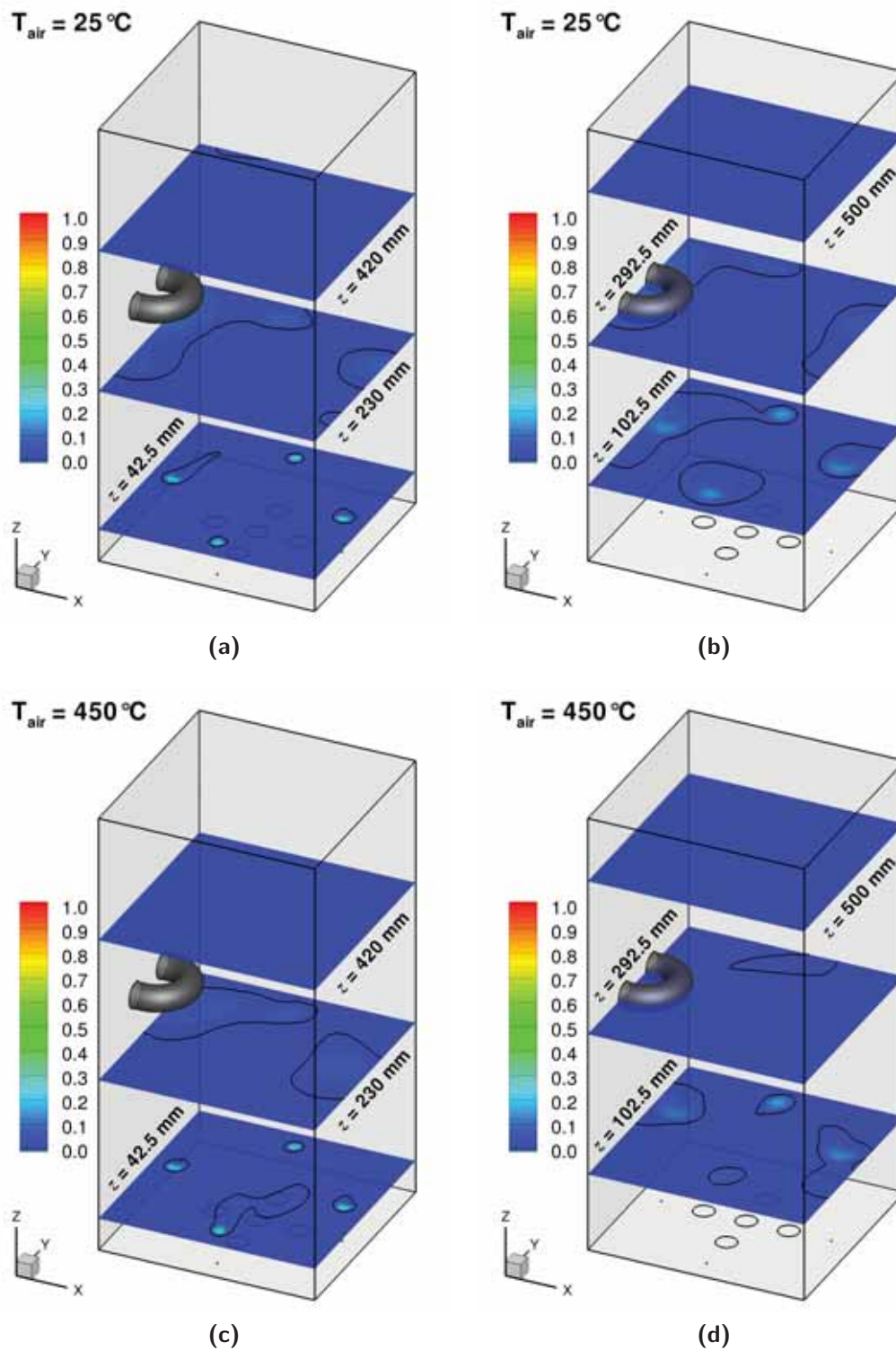


Figure F.2: Predicted CH_4 mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at different $x - y$ planes.

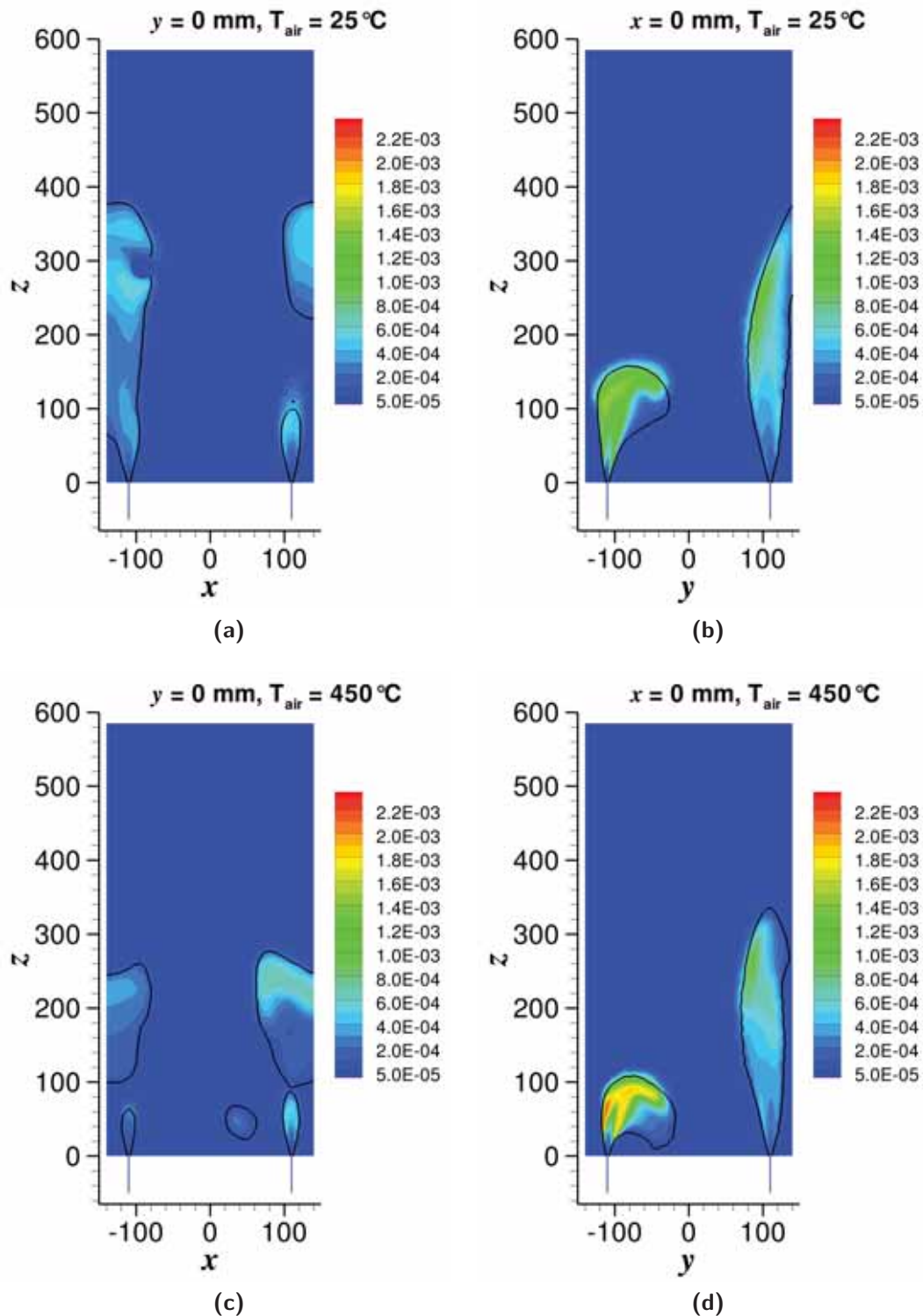


Figure F.3: Predicted CH₃ mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at the $x-z$ and $y-z$ centreline planes.

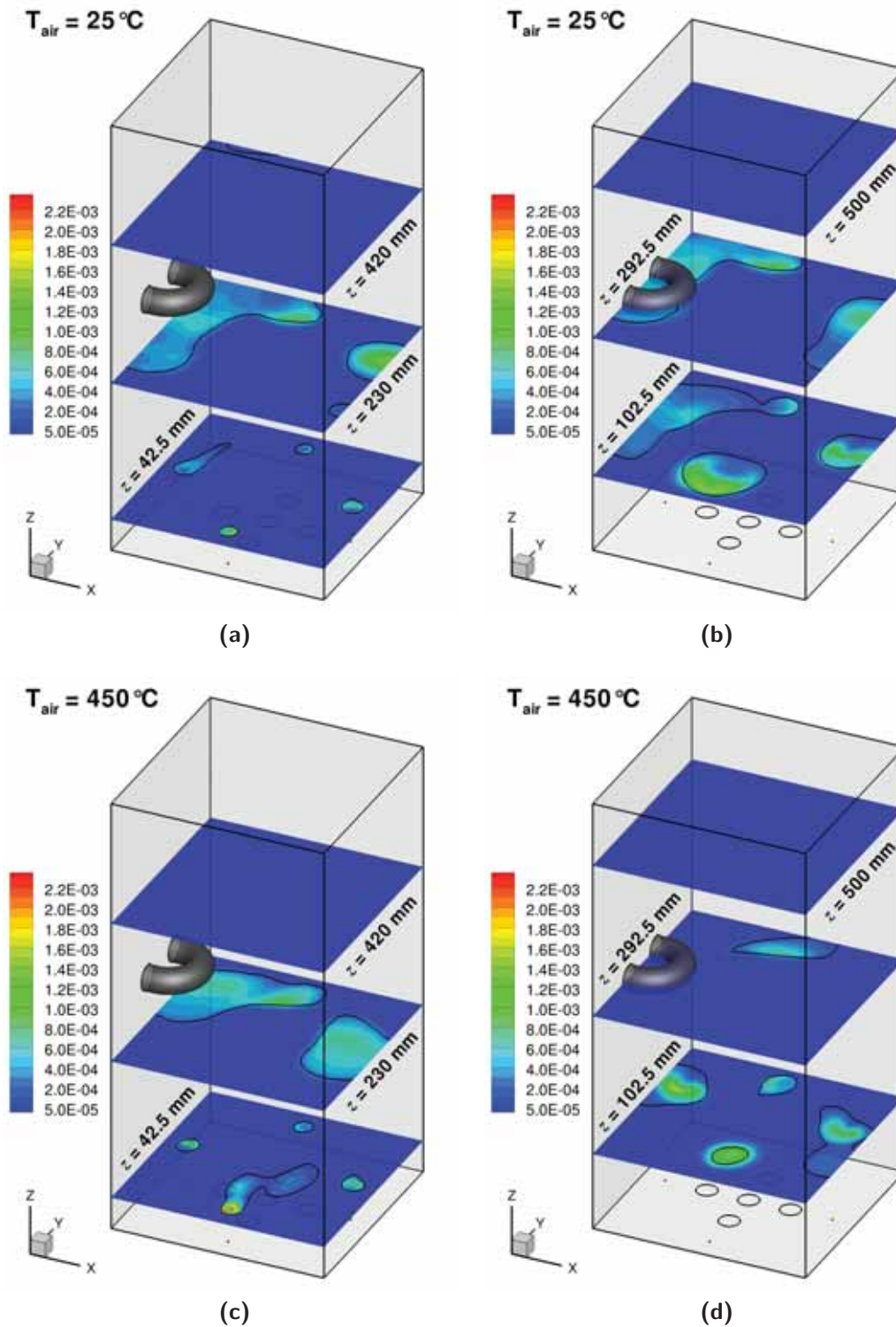


Figure F.4: Predicted CH_3 mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at different $x - y$ planes.

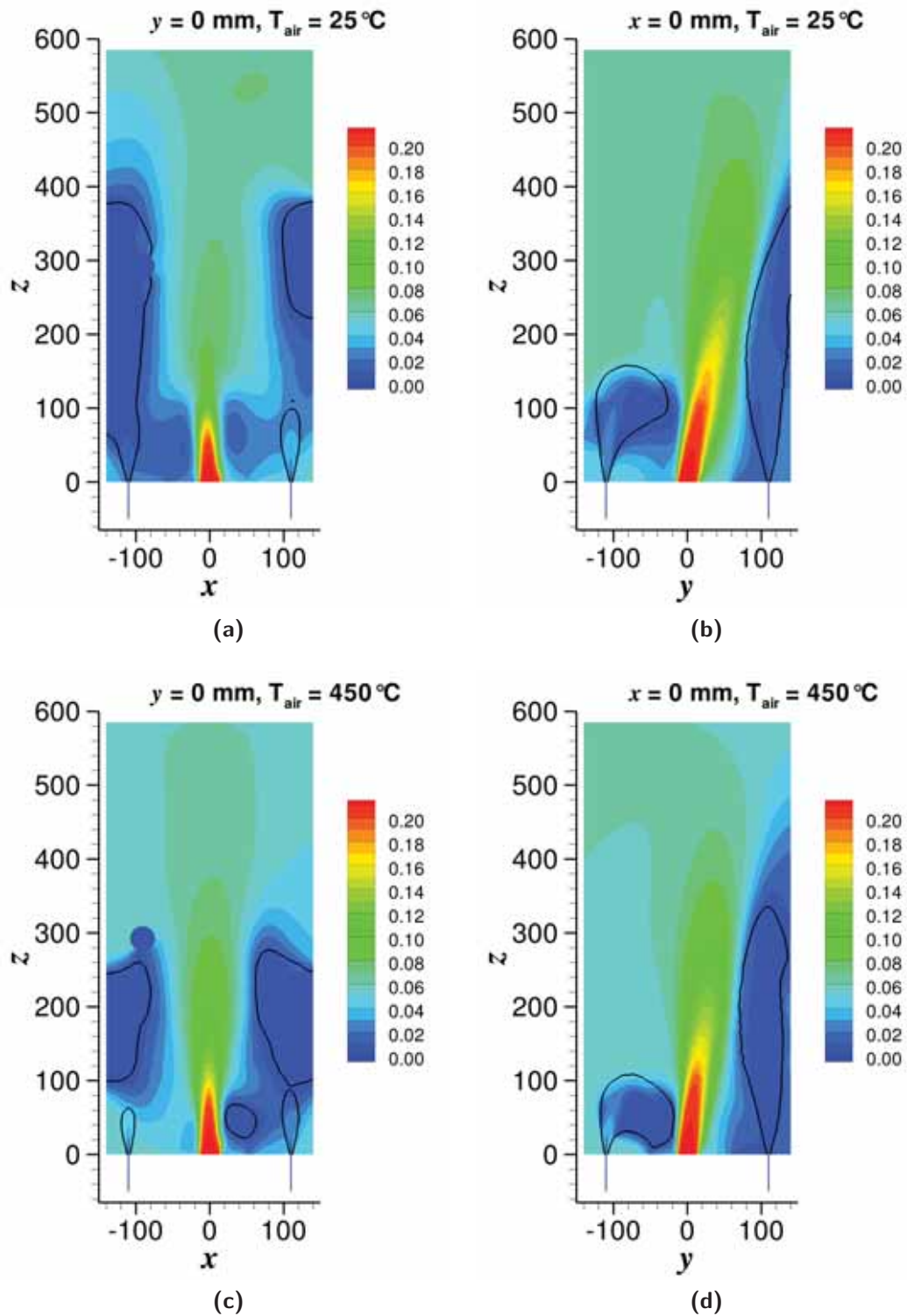


Figure F.5: Predicted O_2 mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{\text{air}} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{\text{air}} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at the $x - z$ and $y - z$ centreline planes.

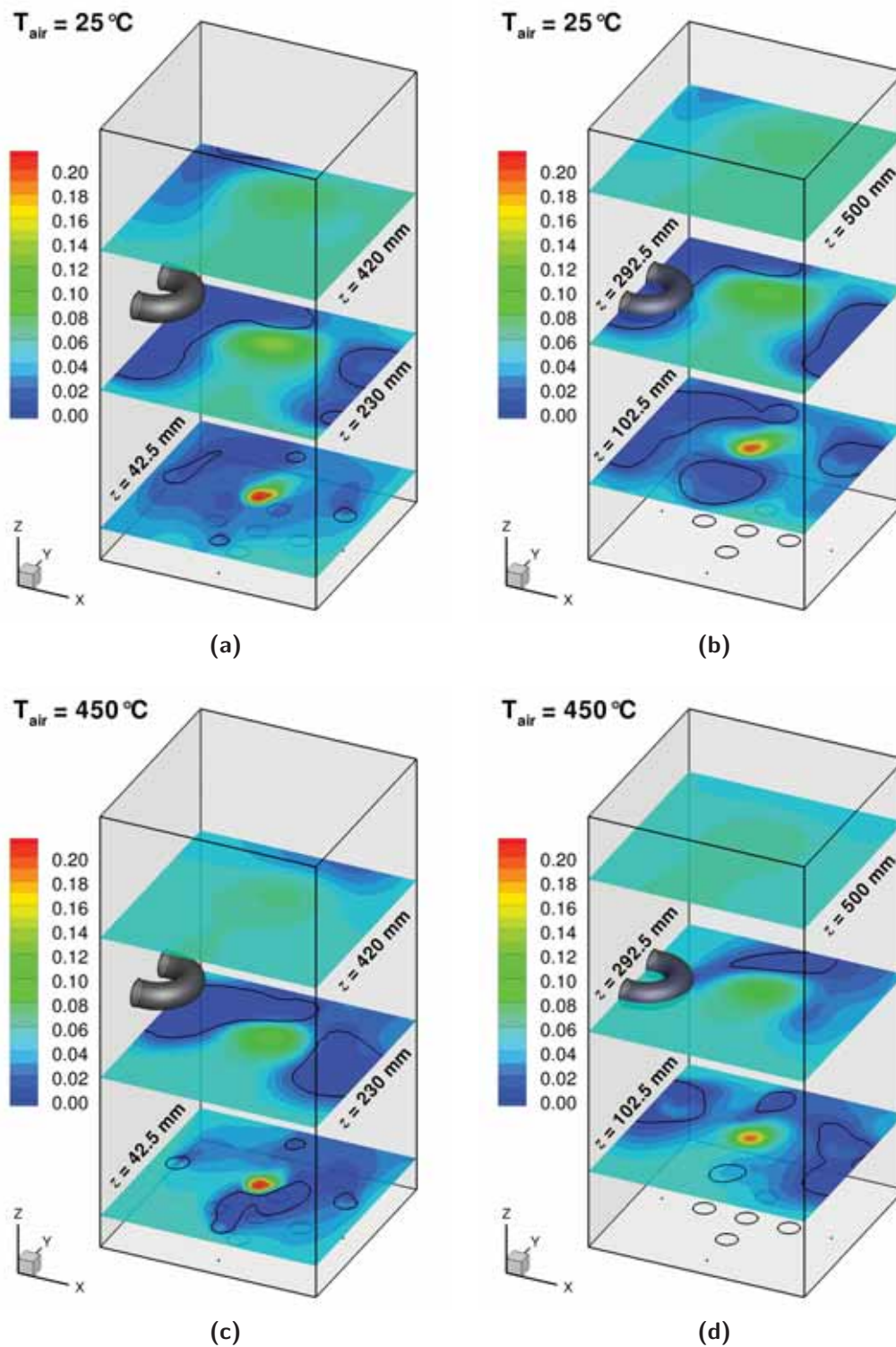


Figure F.6: Predicted O₂ mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at different $x - y$ planes.

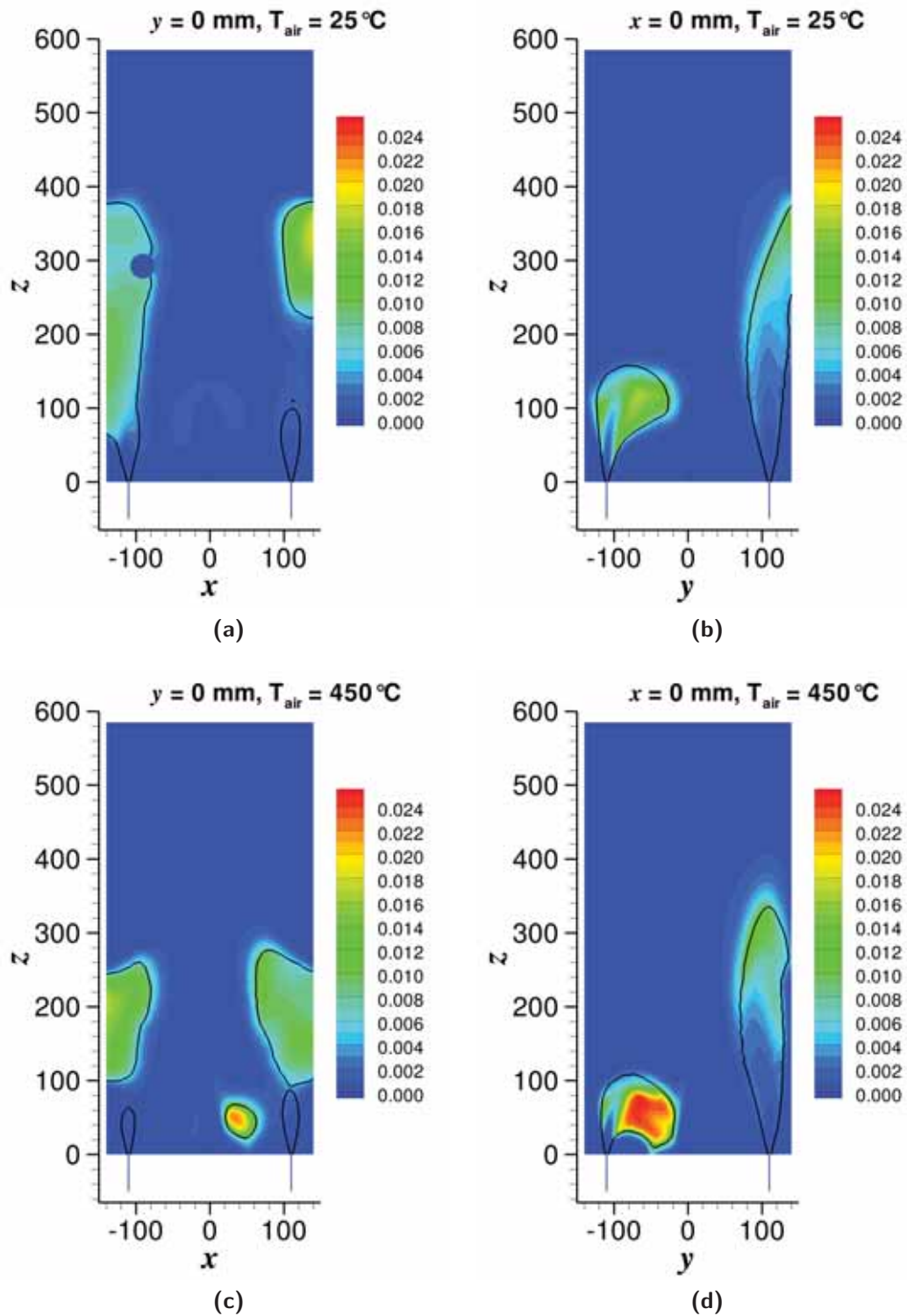


Figure F.7: Predicted CO mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{\text{air}} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{\text{air}} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at the $x-z$ and $y-z$ centreline planes.

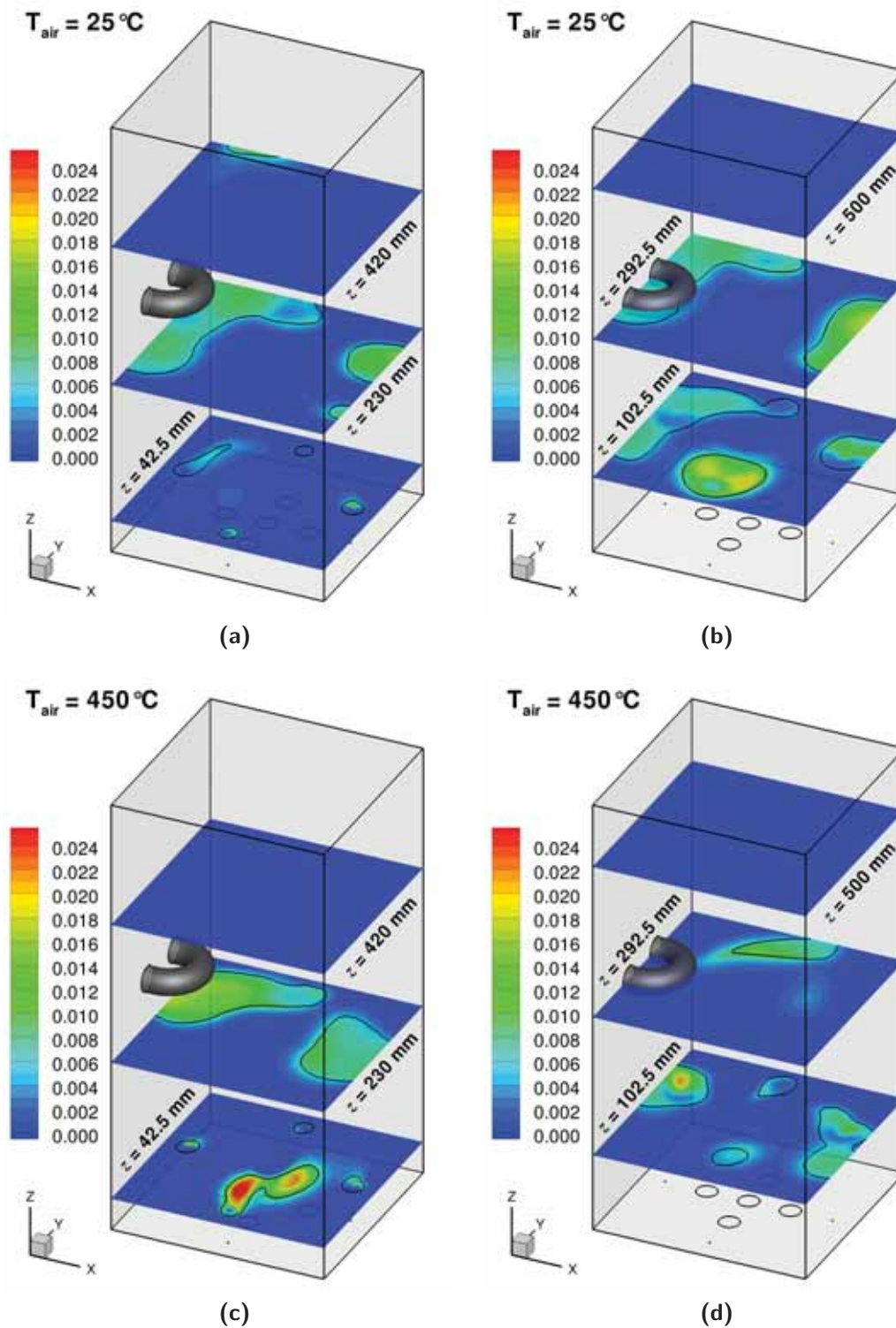


Figure F.8: Predicted CO mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at different $x - y$ planes.

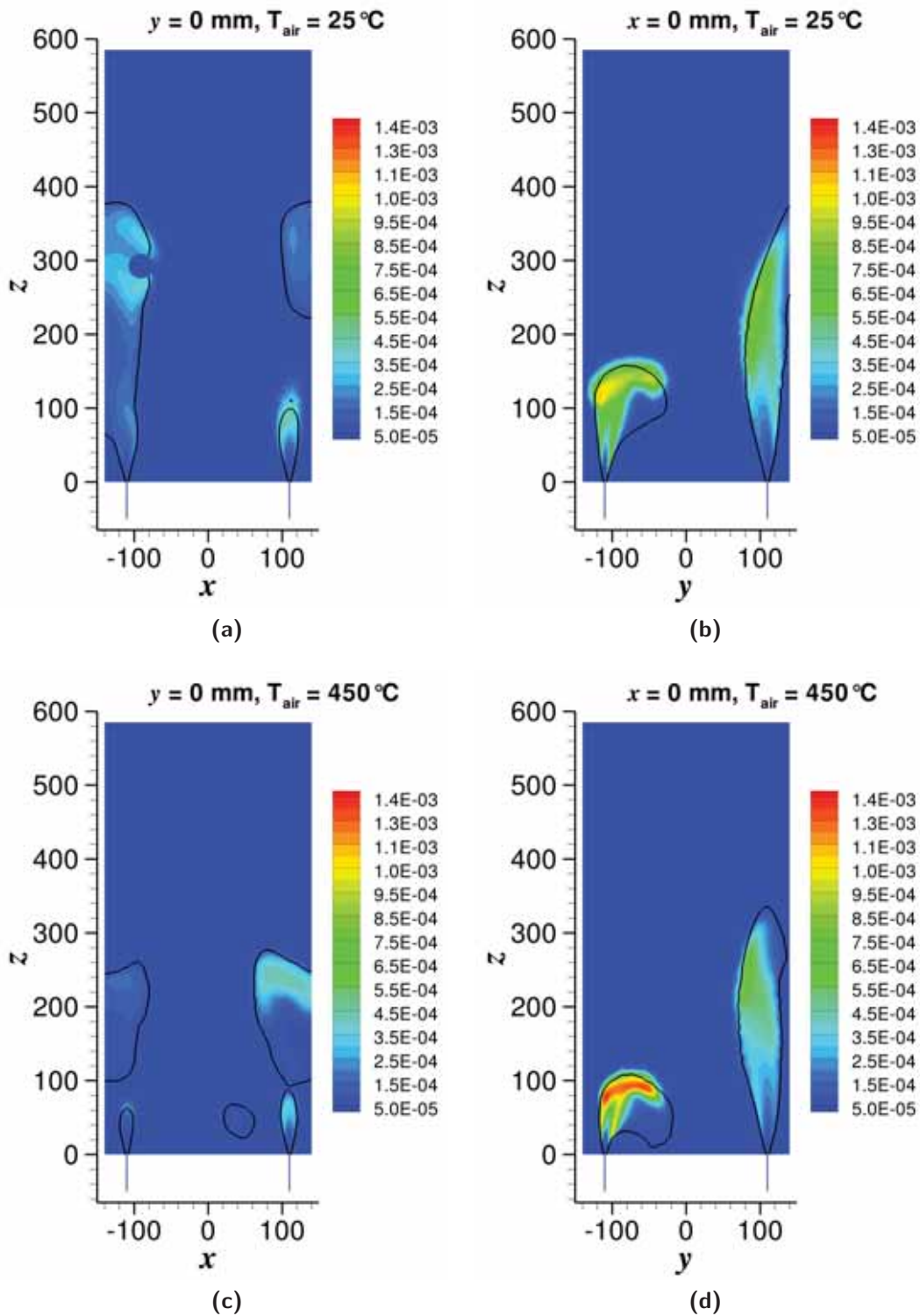


Figure F.9: Predicted CH₂O mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{\text{air}} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{\text{air}} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at the $x-z$ and $y-z$ centreline planes.

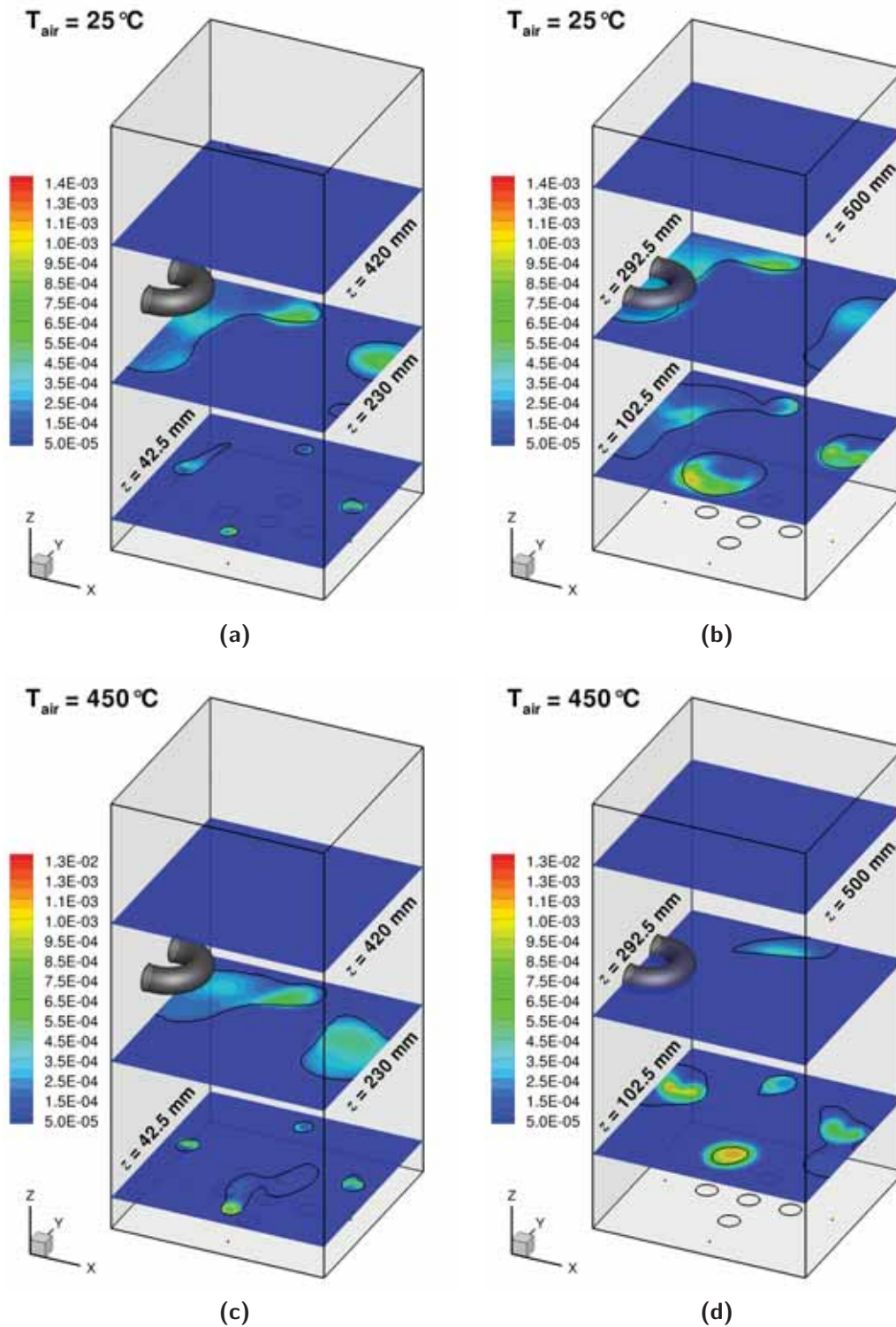


Figure F.10: Predicted CH_2O mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{\text{air}} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{\text{air}} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at different $x - y$ planes.

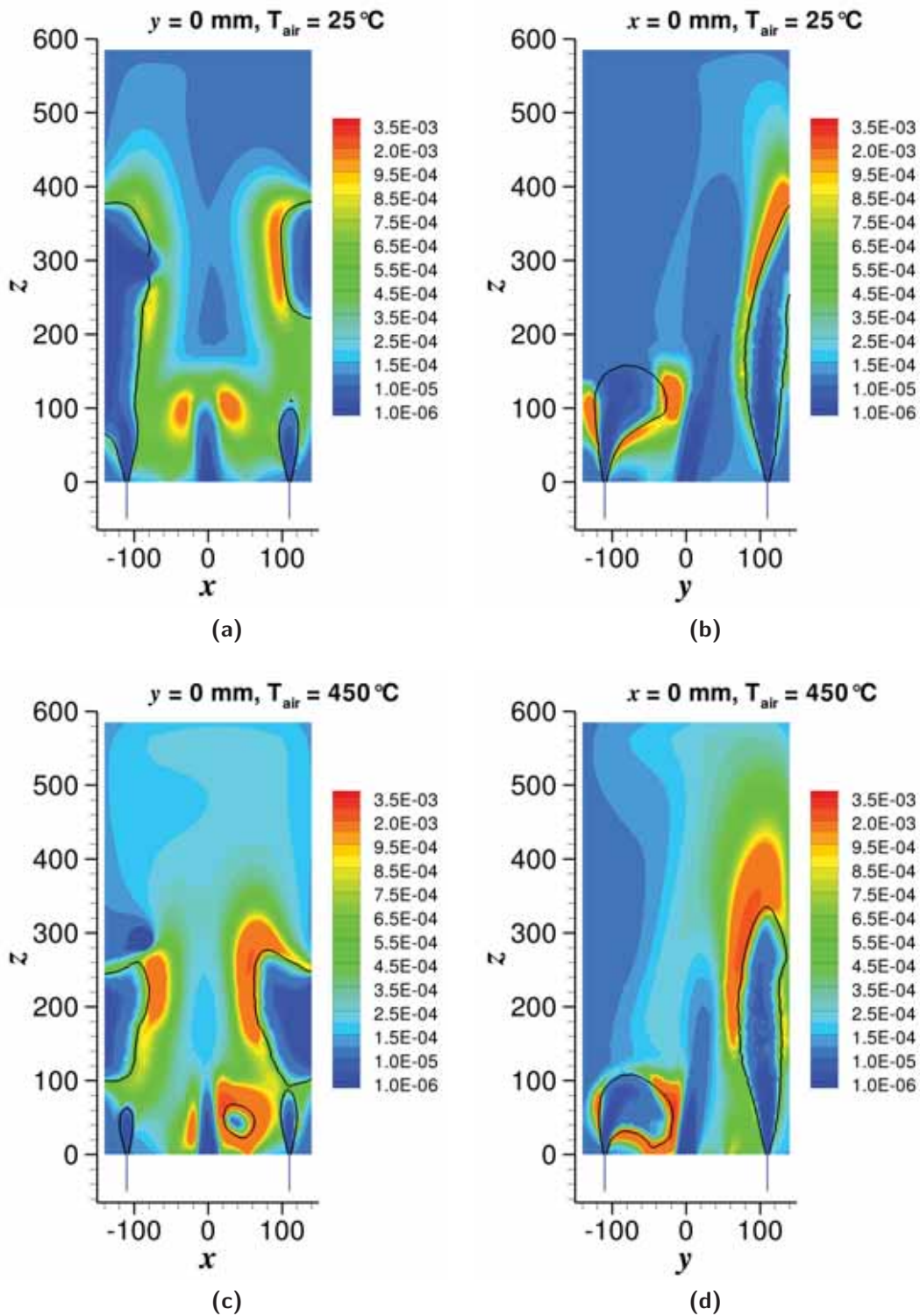


Figure F.11: Predicted OH mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at the $x - z$ and $y - z$ centreline planes.

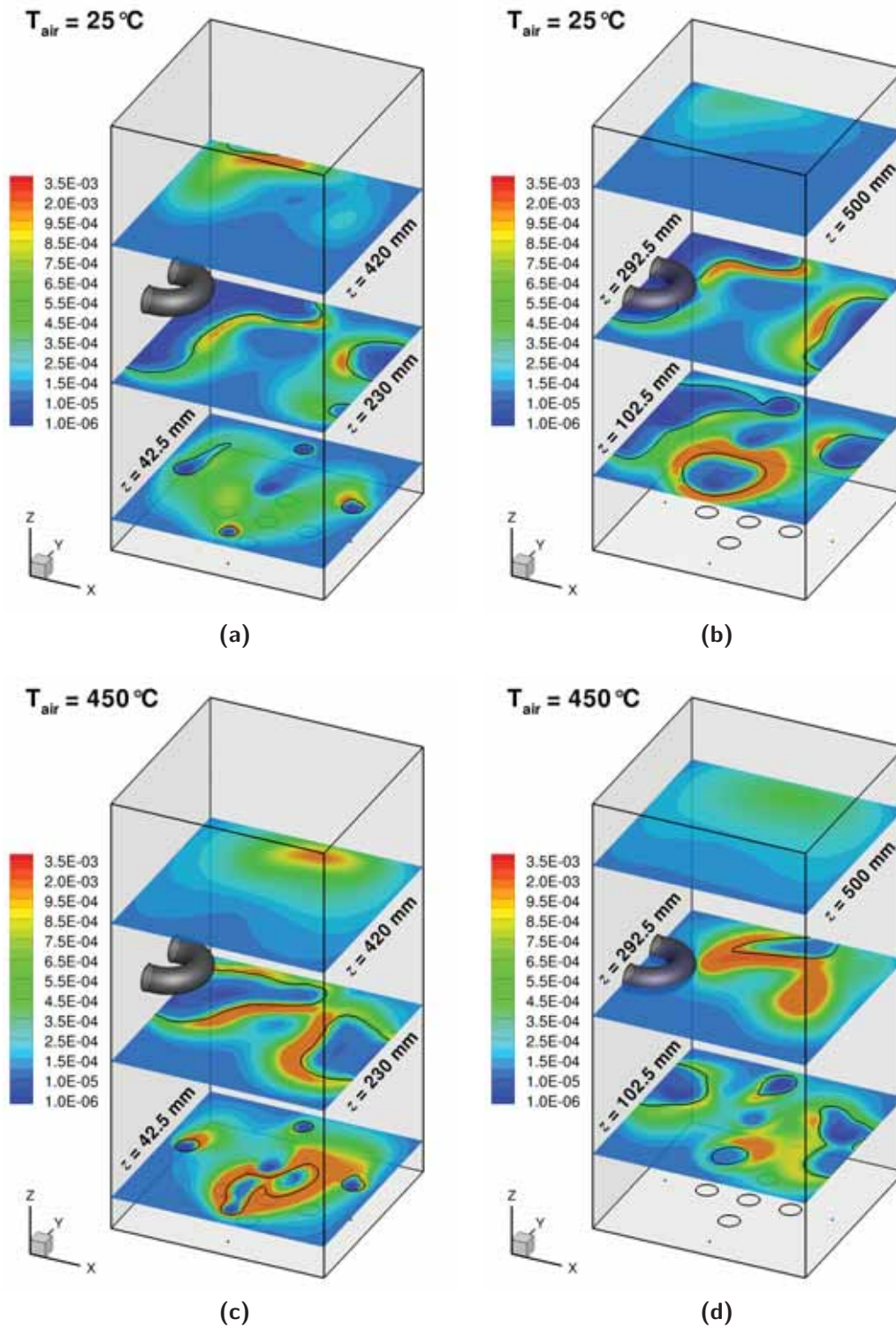


Figure F.12: Predicted OH mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at different $x - y$ planes.

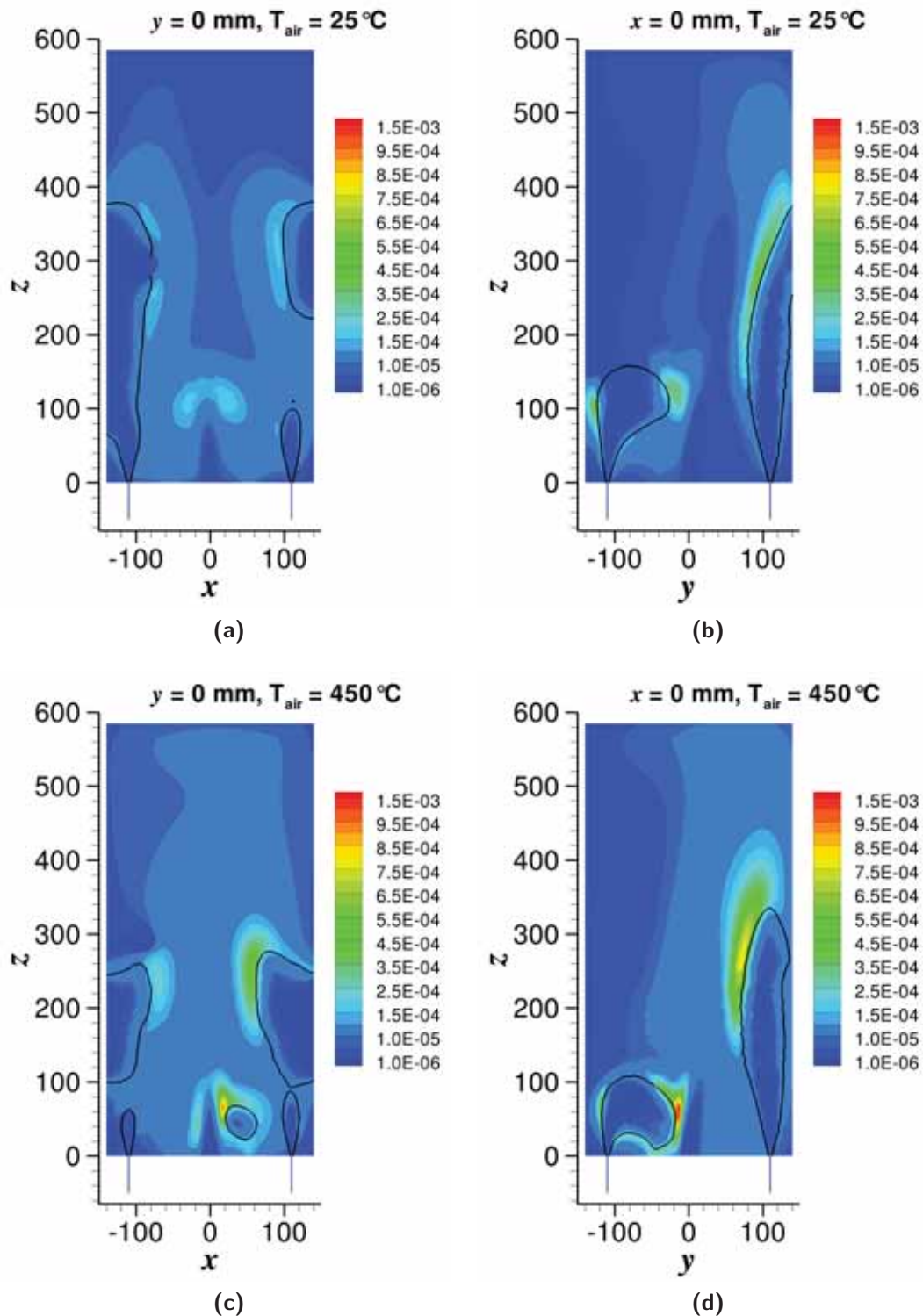


Figure F.13: Predicted O mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at the $x-z$ and $y-z$ centreline planes.

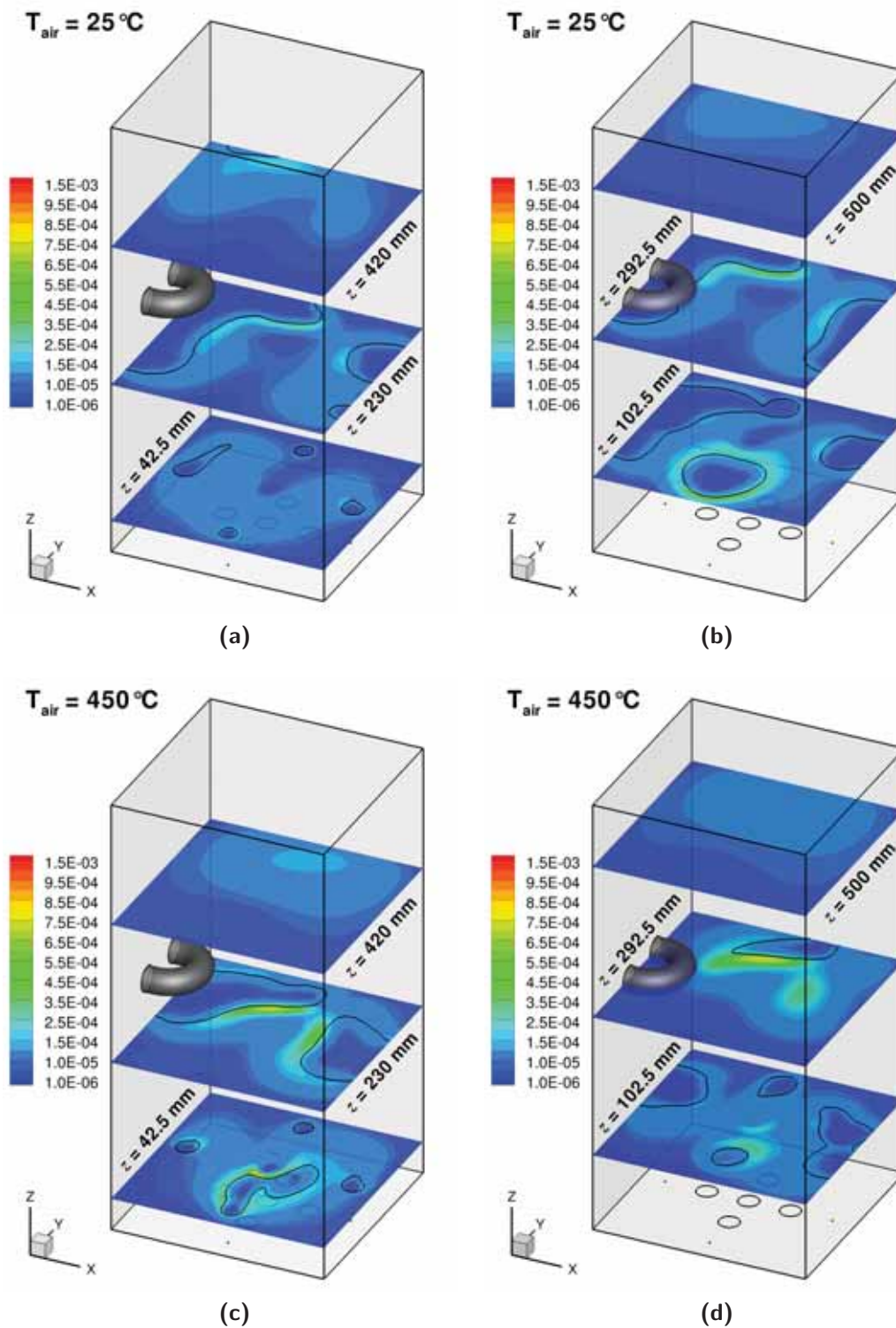


Figure F.14: Predicted O mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at different $x - y$ planes.

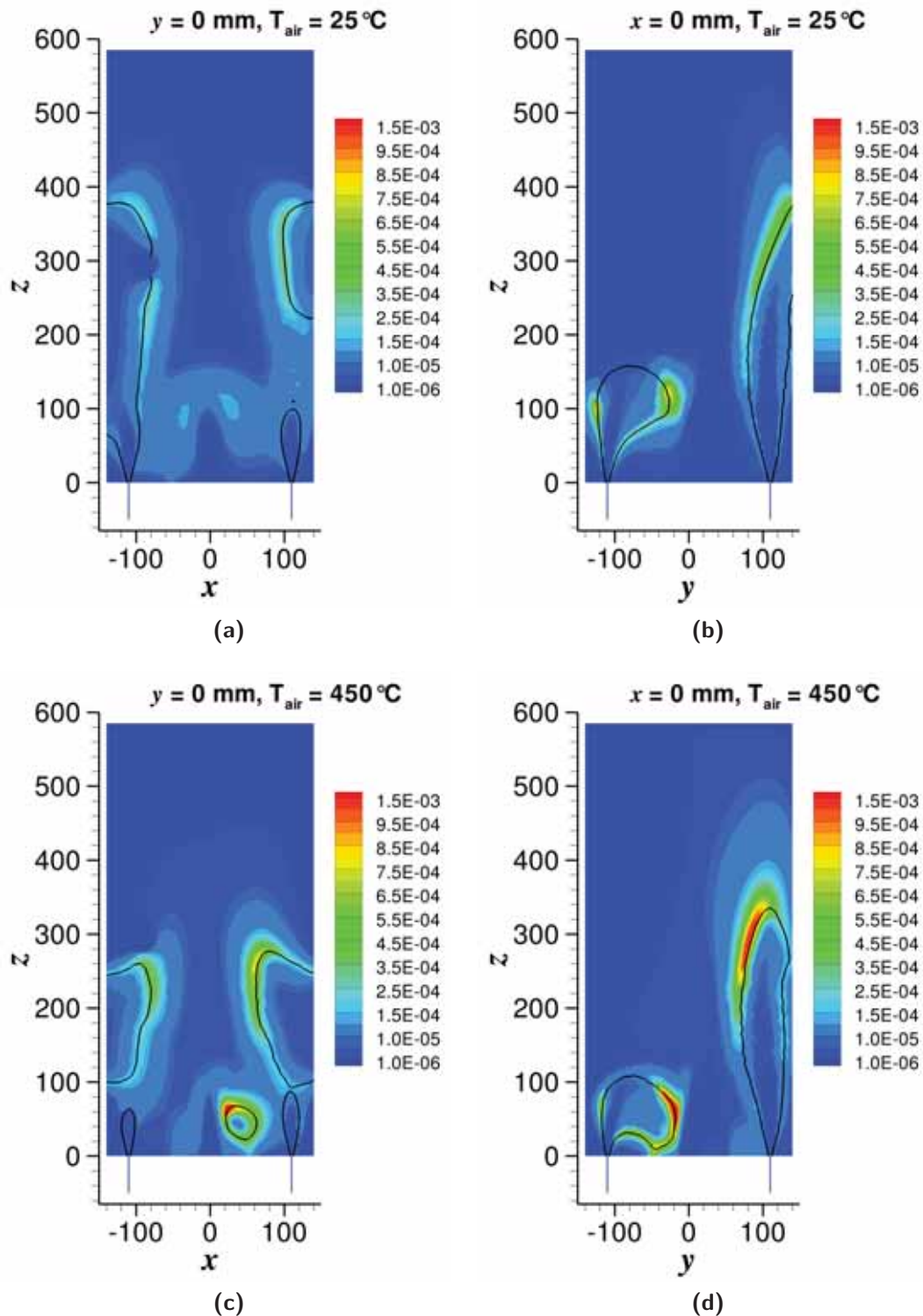


Figure F.15: Predicted H mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at the $x-z$ and $y-z$ centreline planes.

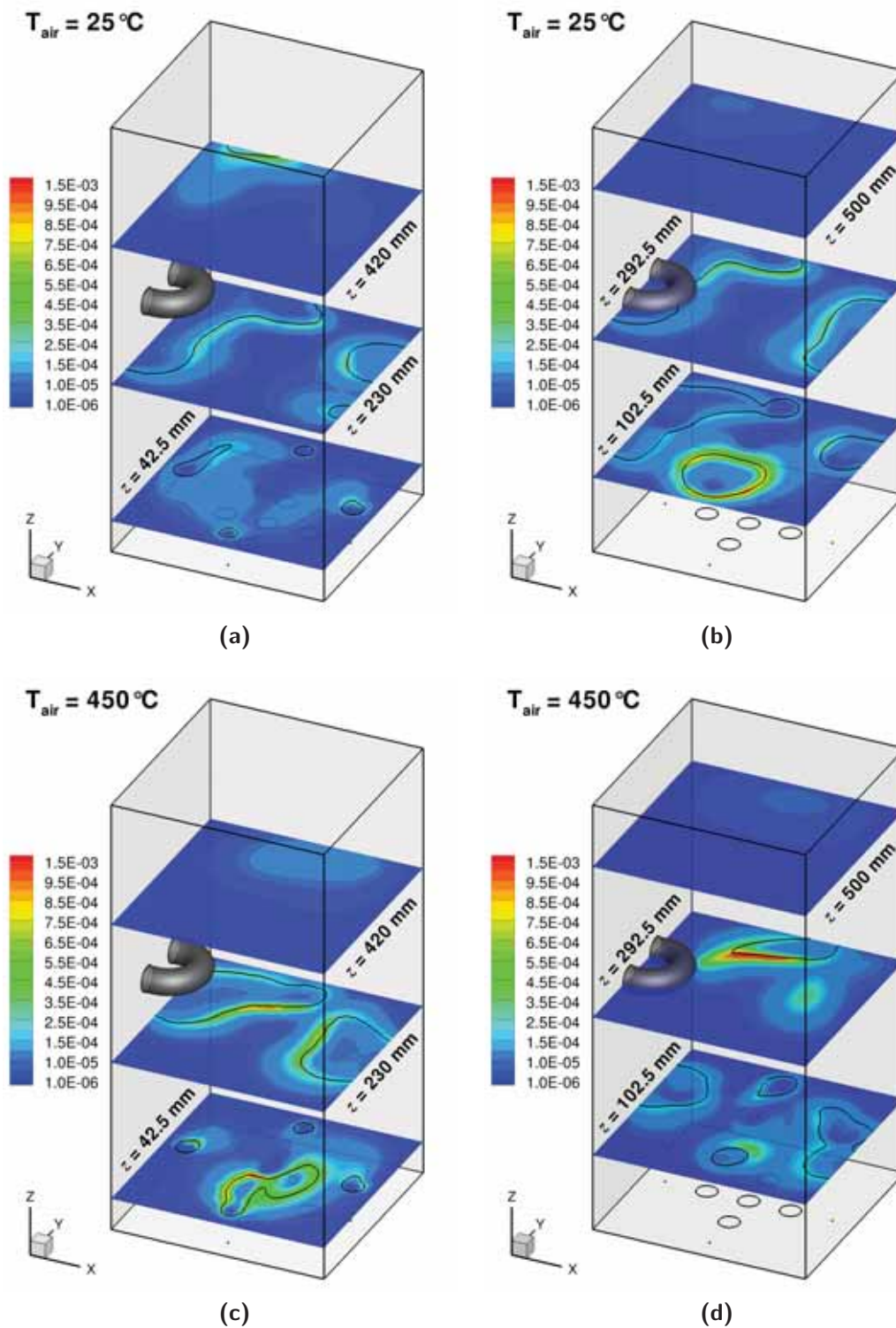


Figure F.16: Predicted H mole fraction contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at different $x - y$ planes.

Appendix G NO_x Contours

It must be noted that the mole fraction contours of all species presented in this Appendix are displayed on a wet basis.

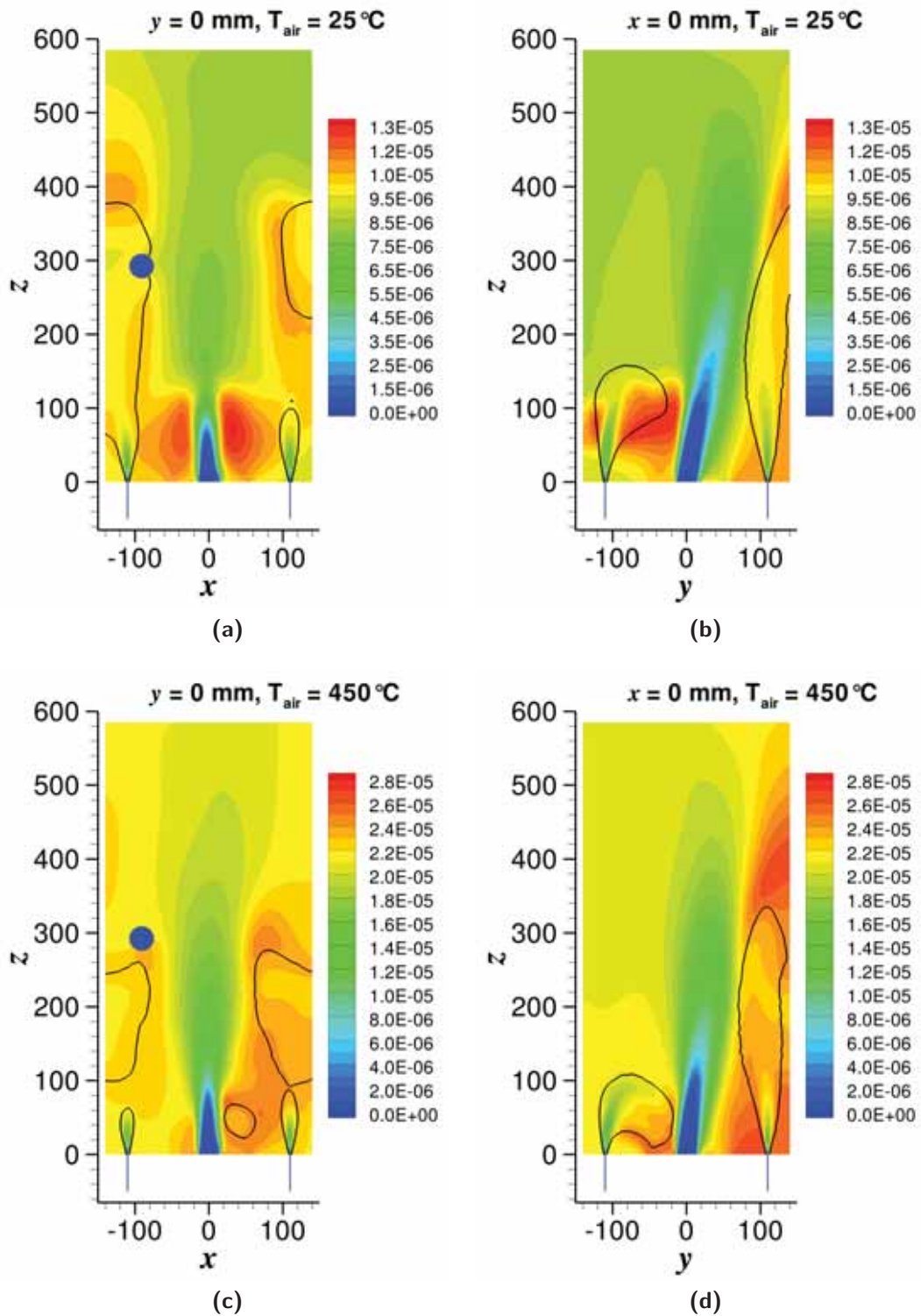


Figure G.1: Predicted NO mole fraction contours on a wet basis with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at the $x-z$ and $y-z$ centreline planes.

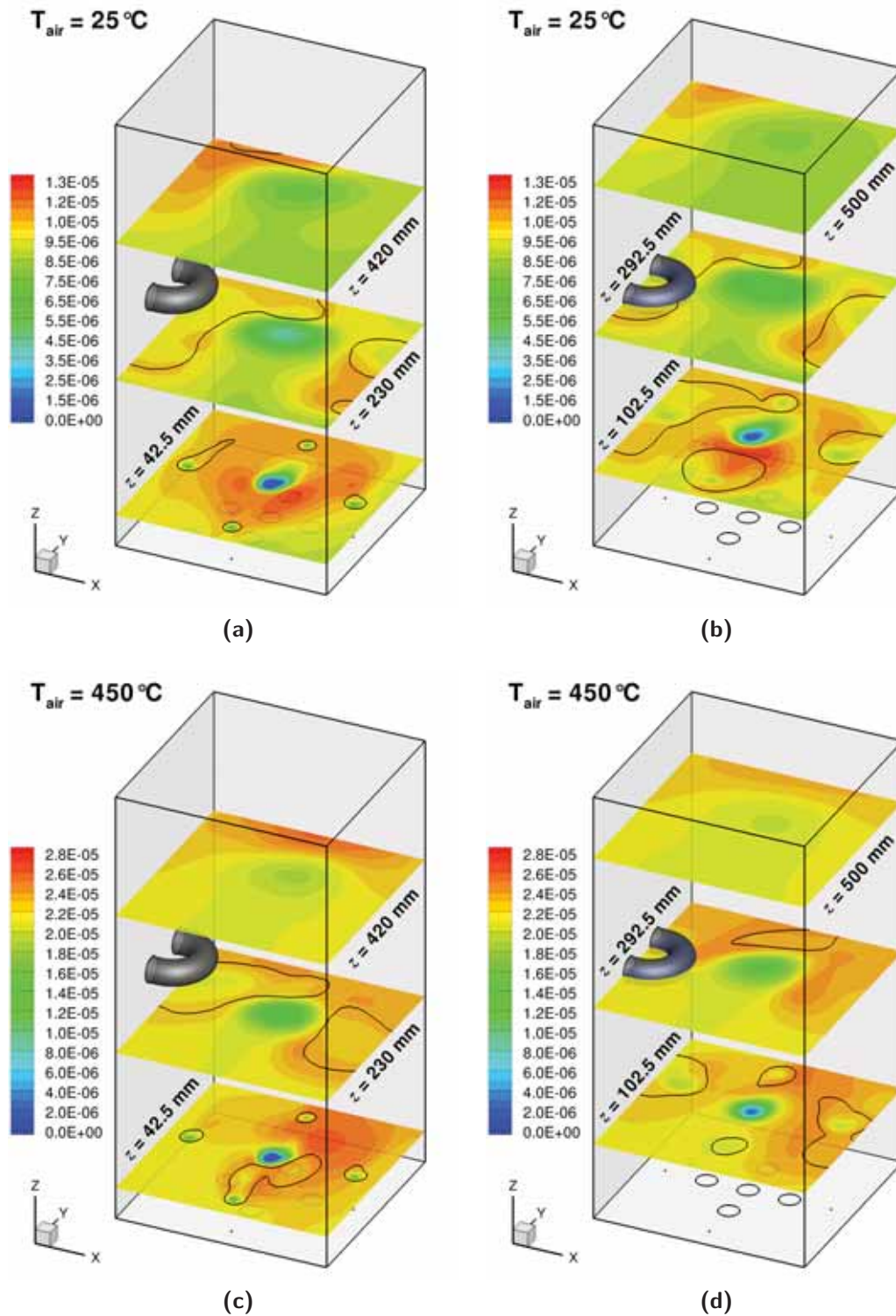


Figure G.2: Predicted NO mole fraction contours on a wet basis with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case, (a) and (b) without air preheat, $T_{air} = 25^\circ\text{C}$, and (c) and (d) with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at different $x - y$ planes.

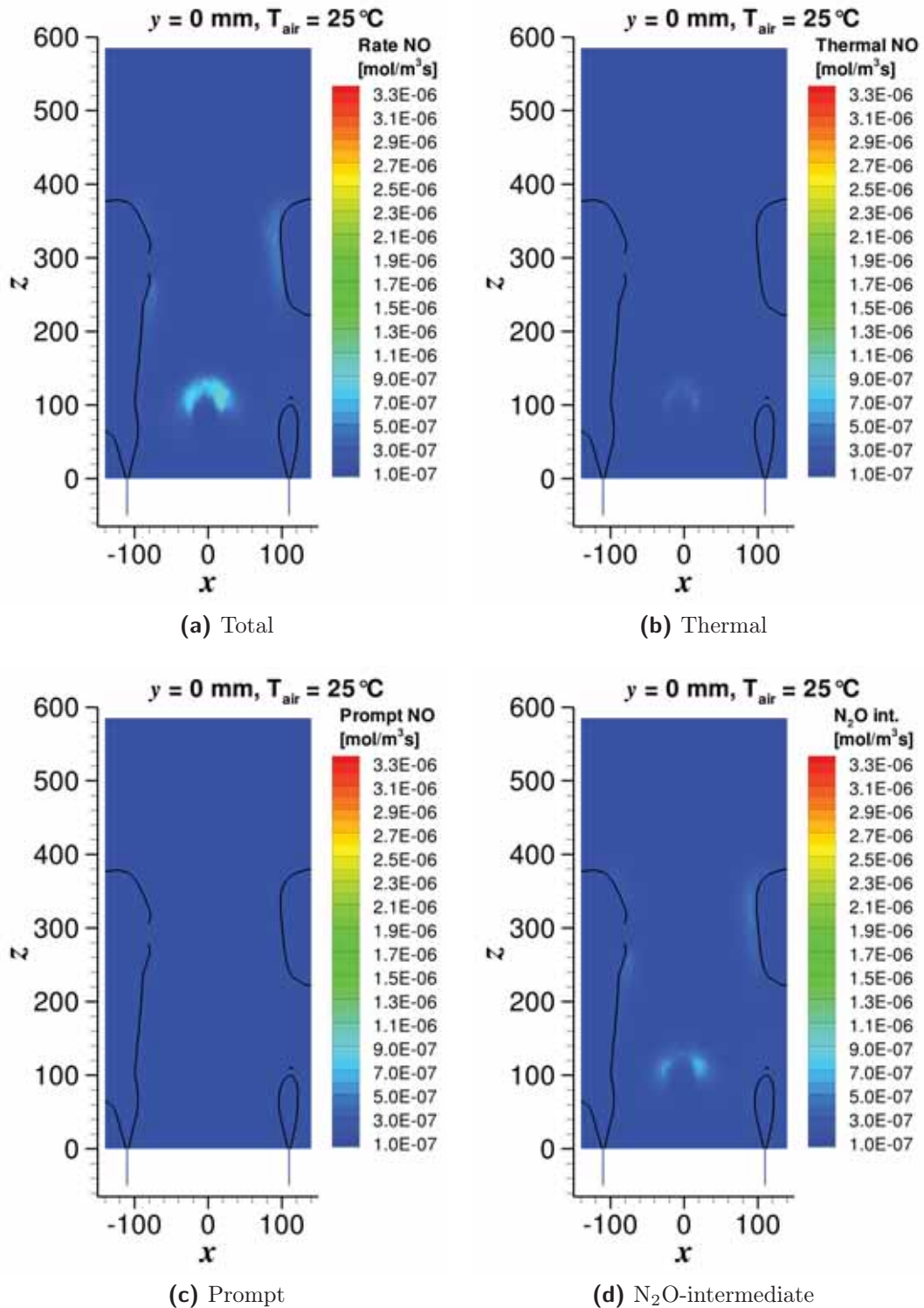


Figure G.3: Predicted NO reaction rate contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case without air preheat, $T_{\text{air}} = 25^\circ\text{C}$, for the EDC model with the Smooke mechanism at the $x-z$ centreline plane. The thermal, prompt and N_2O -intermediate NO_x models were considered (Full NO case shown in Table 7.2).

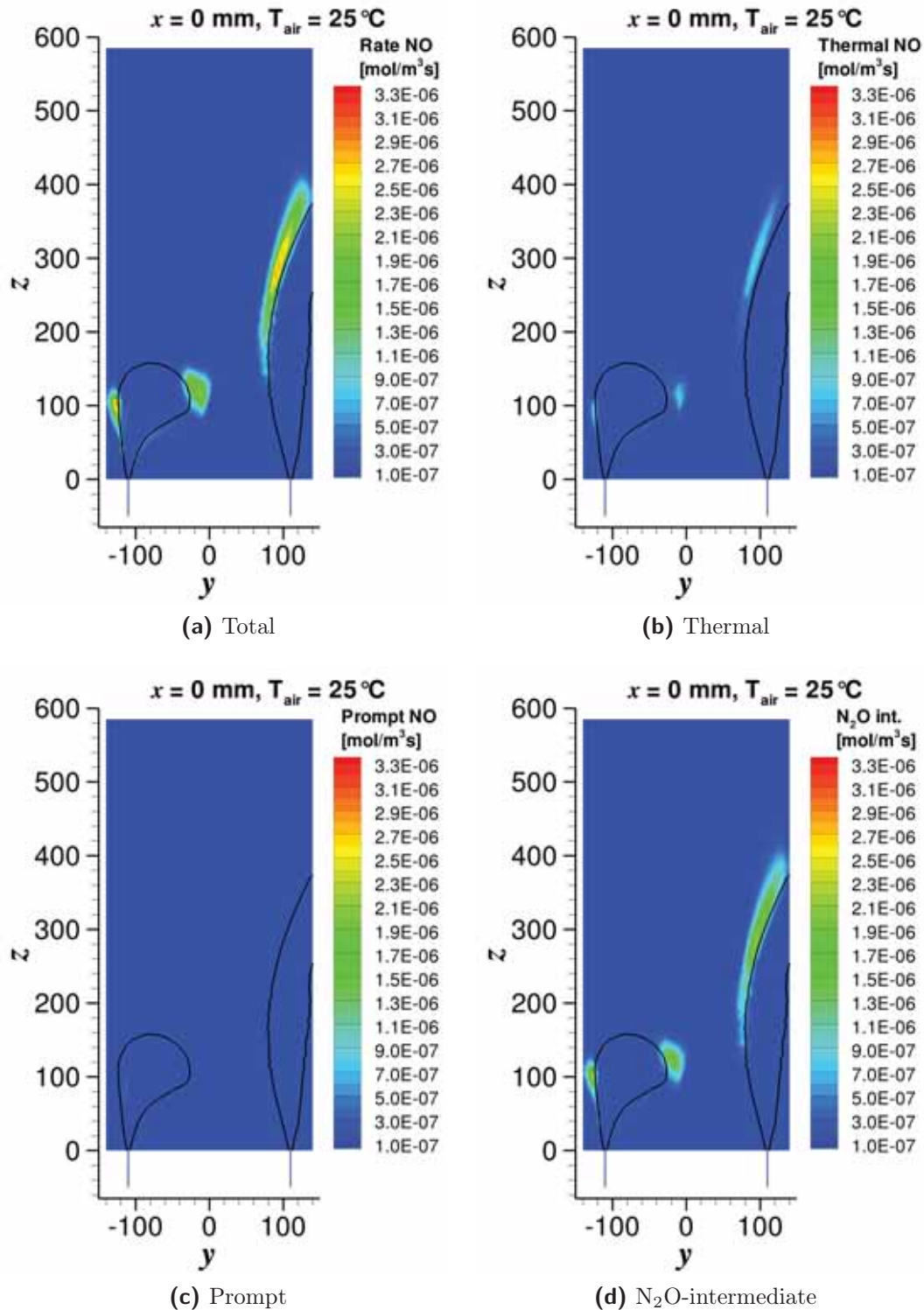


Figure G.4: Predicted NO reaction rate contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case without air preheat, $T_{air} = 25^\circ C$, for the EDC model with the Smooke mechanism at the $y - z$ centreline plane. The thermal, prompt and N_2O -intermediate NO_x models were considered (Full NO case shown in Table 7.2).

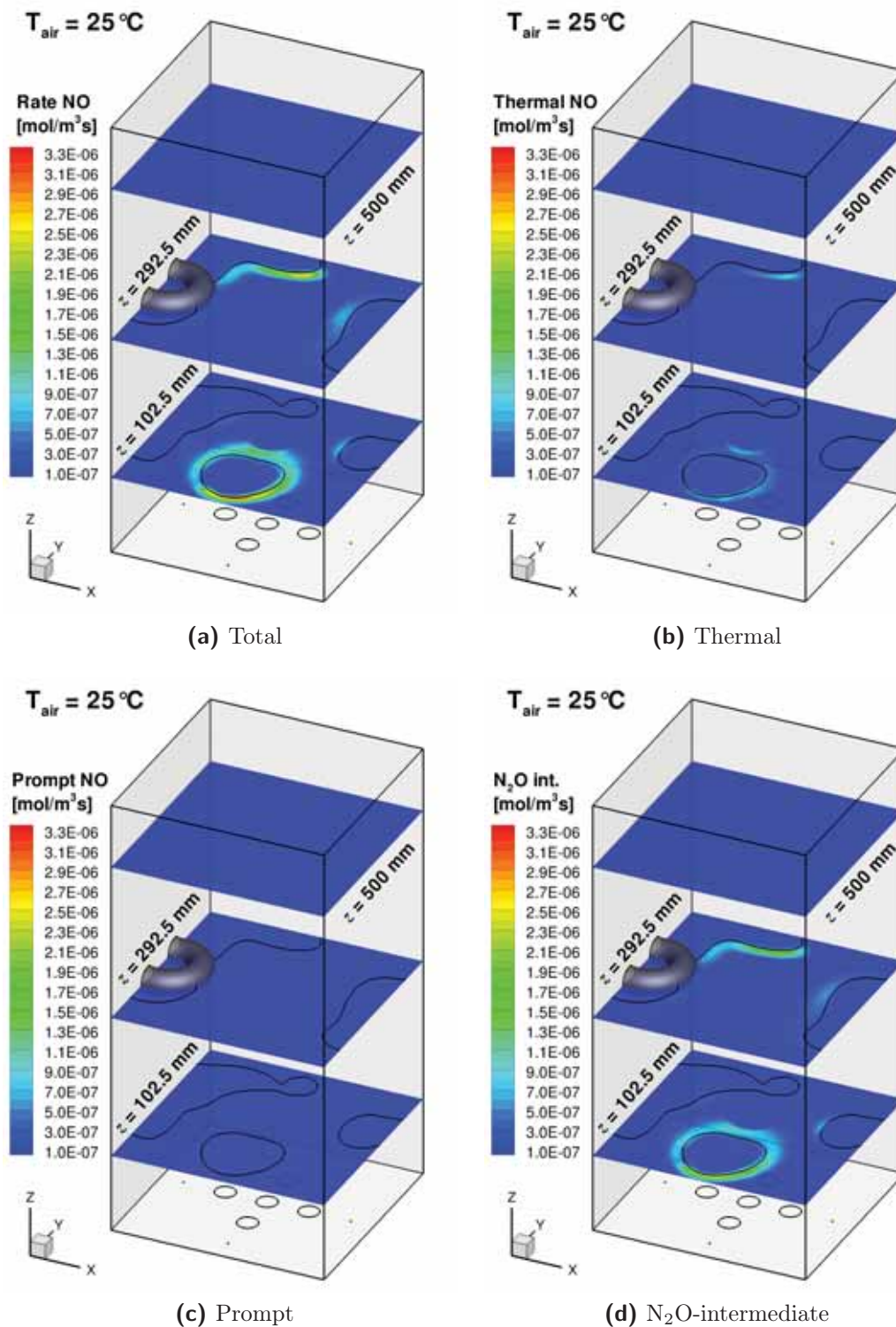


Figure G.5: Predicted NO reaction rate contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case without air preheat, $T_{\text{air}} = 25^\circ\text{C}$, for the EDC model with the Smooke mechanism at different $x - y$ planes. The thermal, prompt and N_2O -intermediate NO_x models were considered (Full NO case shown in Table 7.2).

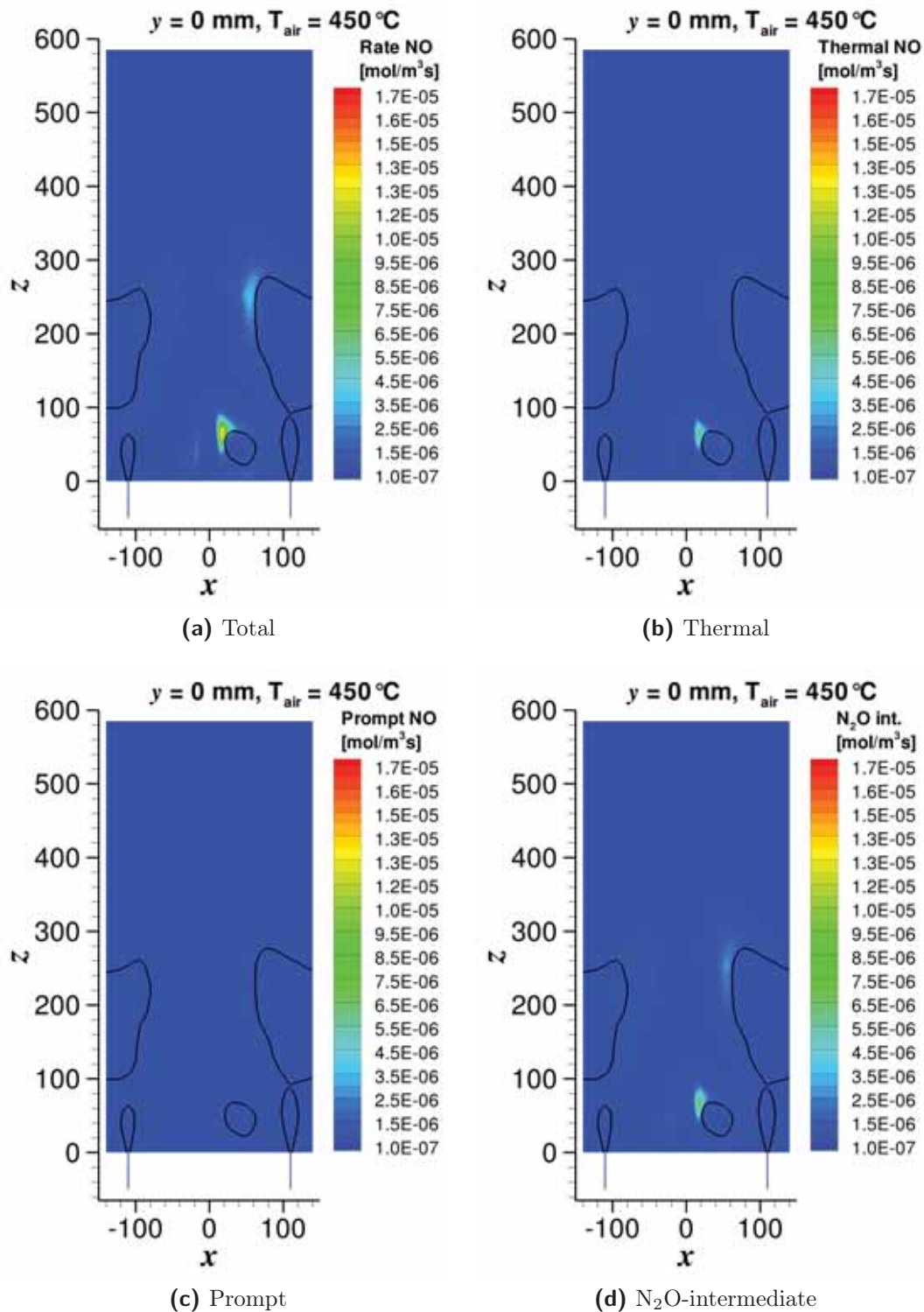


Figure G.6: Predicted NO reaction rate contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case with air preheat, $T_{\text{air}} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at the $x - z$ centreline plane. The thermal, prompt and N_2O -intermediate NO_x models were considered (Full NO case shown in Table 7.2).

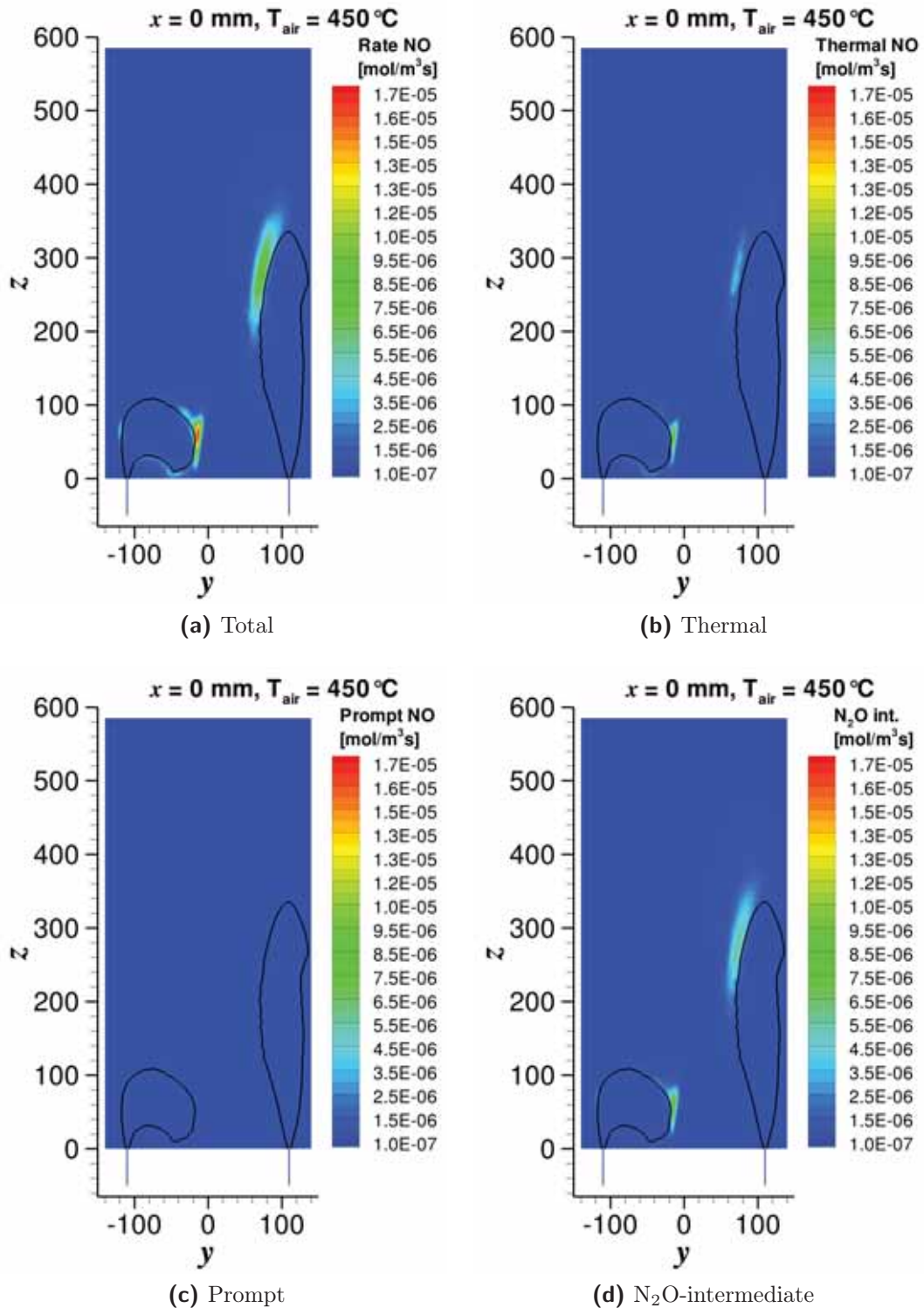


Figure G.7: Predicted NO_x reaction rate contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case with air preheat, $T_{\text{air}} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at the $y-z$ centreline plane. The thermal, prompt and N_2O -intermediate NO_x models were considered (Full NO_x case shown in Table 7.2).

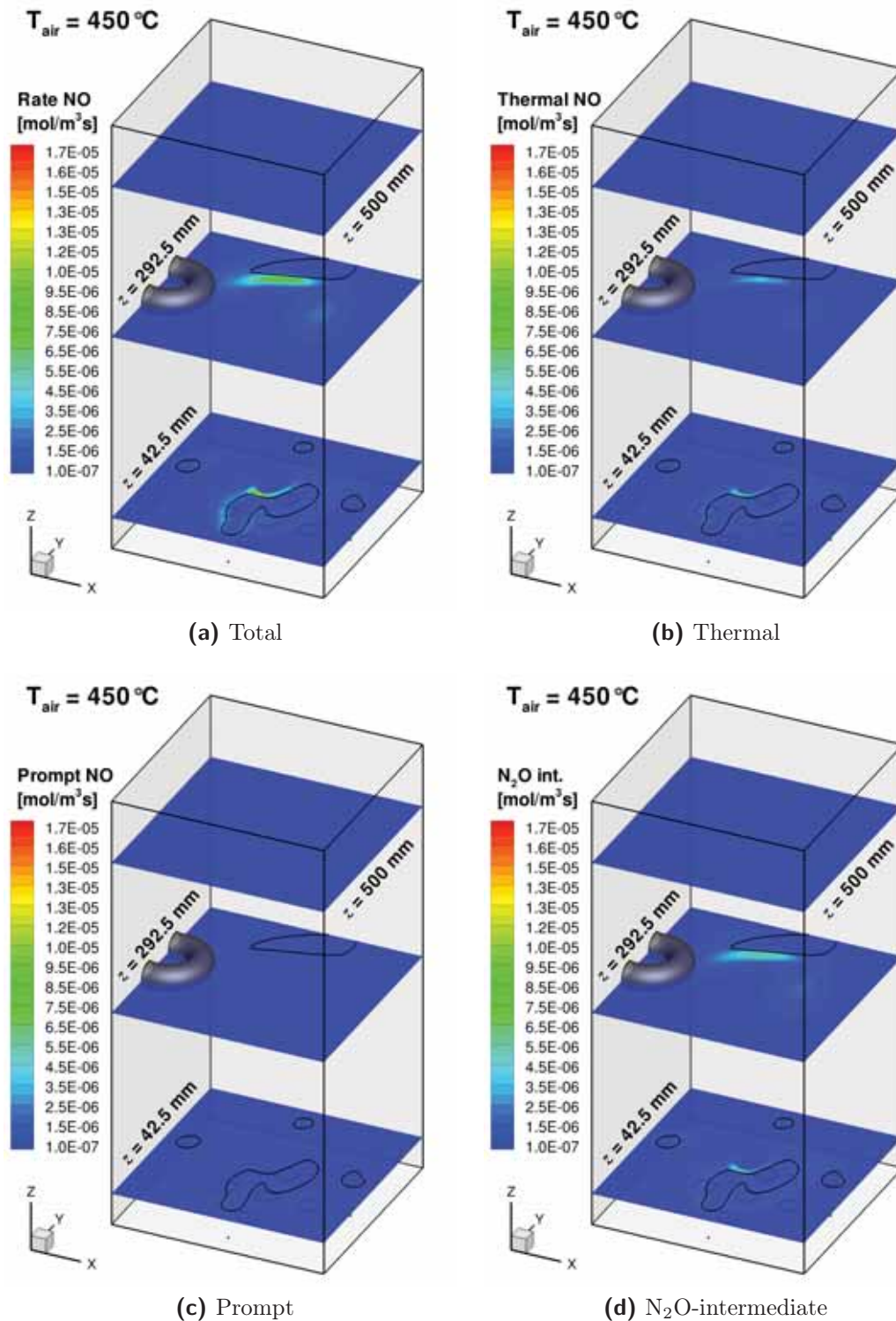


Figure G.8: Predicted NO reaction rate contours with stoichiometric surface ($\xi_{st} = 0.0552$) overlaid for the baseline case with air preheat, $T_{air} = 450^\circ\text{C}$, for the EDC model with the Smooke mechanism at different $x - y$ planes. The thermal, prompt and N_2O -intermediate NO_x models were considered (Full NO case shown in Table 7.2).

Appendix H Publications

Publications arising from this thesis

G. G. Szegő, B. B. Dally, G. J. Nathan, F. C. Christo, Design optimisation of a MILD combustion furnace based on CFD modelling, in: Proceedings of the Australian Symposium on Combustion and the Eighth Australian Flame Days, No. P047, Monash University, Melbourne, 2003.

G. G. Szegő, B. B. Dally, G. J. Nathan, F. C. Christo, Performance characteristics of a 20kW MILD combustion furnace, in: The Sixth Asia-Pacific Conference on Combustion, The Combustion Institute, Nagoya, Japan, 2007, pp. 231–234.

G. G. Szegő, B. B. Dally, G. J. Nathan, Stability limits of a parallel jet MILD combustion burner system, in: Proceedings of the Australian Combustion Symposium, University of Sydney, 2007, pp. 62–65.

G. G. Szegő, B. B. Dally, G. J. Nathan, Experimental investigation of a parallel jet MILD combustion burner system, in: The Seventh High Temperature Air Combustion and Gasification International Symposium, Phuket, Thailand, 2008.

G. G. Szegő, B. B. Dally, G. J. Nathan, Scaling of NO_x emissions from a laboratory-scale MILD combustion furnace, *Combustion and Flame* 154 (1–2) (2008) 281–295.

G. G. Szegő, B. B. Dally, G. J. Nathan, Operational characteristics of a parallel jet MILD combustion burner system, *Combustion and Flame* 156 (2) (2009) 429–438.

G. G. Szegő, B. B. Dally, F. Christo, Investigation of the mixing patterns inside a MILD combustion furnace based on CFD modelling, in: Proceedings of the Australian Combustion Symposium, University of Queensland, 2009.