

Other problem.

I think the difficulty starts about p 3.

Consider sampling without replacement values $\lambda_1, \dots, \lambda_N$ all finite.

A large sample is one in which each of the λ_i occurs a great many times, all equally frequently.

What is the large sample version of the real root of the equation

$$\sum \frac{\lambda_i - p}{\lambda_i^2 + \frac{(\lambda_i - p)^2}{\lambda_i}} = 0 ?$$

Now

$$\frac{\lambda_i - p}{\lambda_i^2 + \frac{(\lambda_i - p)^2}{\lambda_i}} = \frac{1}{\lambda_i} \cdot \frac{\lambda_i - p}{1 + \frac{\lambda_i - p}{\lambda_i}}$$

of which the numerator is given, while the denominator is

$$\frac{1}{\lambda_i^2} \cdot \frac{\lambda_i^2}{(n+1)(n+3)}$$

Hence, when the sample is infinite without limit

$$X = \sum \frac{\lambda_i - p}{\lambda_i^2 + \frac{(\lambda_i - p)^2}{\lambda_i}}$$

is distributed normally, and you will require

$$\frac{\lambda_i^2}{(n+1)(n+3)} \sum \frac{1}{\lambda_i^2}$$

$$\sim -\frac{dX}{dp} = \sum \frac{1}{\lambda_i^2} \cdot \frac{1 - \frac{\lambda_i - p}{\lambda_i}}{1 + \frac{\lambda_i - p}{\lambda_i}}$$

of which the numerator, intended for large sample is

$$\frac{\lambda_i^2}{n+3} \sum \frac{1}{\lambda_i^2}$$

How fast

$$n \cdot p = \frac{-X}{dX/dp}$$

$$V(n) =$$

$$\frac{n+3}{(n+1)}$$

$$\sum \frac{1}{\lambda_i^2}$$

