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Jan 9. (1939)

Dear Fisher,

About the question of $n s^2 = \sum (x_i - \bar{x})^2$ or $(n-1) s^2 = \sum (x_i - \bar{x})^2$

In response to mails from my class last term I have decided that a probability book for me is due, & have started it. I don't want to make unnecessary departures from the usual practice, & in particular I am adopting the practice of using italics for estimates & Greek letters for quantities to be found - it was a matter of random selection after getting fed up with σ & μ that made me adopt the opposite practice. However I'm bothered about n or $n-1$. The argument for $n-1$ is, I think, that it brings the mode of the χ^2 distribution to $\chi^2 = 0$. With n there is a bias, though the formulae are similar except for one to have to look pretty carefully to see the difference. The χ^2 distribution goes over into my theory in an estimation problem: given one set of deviations, what is the probability of a given scatter in a new series of observations a means where there is reason to expect σ to be the same?

On the other hand in the method of least squares what comes in is $\left\{ 1 + \frac{n(x_i - \bar{x})^2}{\sum c^2} \right\}^{-(n-n+1)}$, and in significance tests

for one new parameter the same thing with index $-(n-m+2)$, where in the former m is the total number of parameters found, in the latter the number of old ones; S or C is a residual so it is really $2C/n$ that comes in, the m appearing only in the index, & taking $2C/(n-m)$ will complicate the algebra badly. Also it's the sort of algebra that I usually get wrong.

So it rather looks as if I shall have to stick to n . I should then have to say add $\frac{1}{2}$ by $\frac{n(n-1)}{n!(n-1)}$ & use your table, or else cook the table myself - which again I should probably get wrong. In any case I think $\sqrt{\frac{E\sigma^2}{n(n-m)}}$ will have to be given as the estimated standard error of α , and tables of 5% & 1% limits in estimation problems & of $K = 1, \frac{1}{3}, \frac{1}{10}, \frac{1}{30}$ in significance ones in terms of α/σ_a . Do you see any reasonably compact alternative?

I suppose you don't know anybody that would like the job of working out \underline{K} for $n-m \leq 5$. It will go into a rather filthy single integral, & will I suppose be wanted some time. Anyhow I should like to see myself how it behaves. There is another bother about the tests for several degrees of freedom. Two of Wishart's lads, Finney & Lawley, had this half done when I found a nasty little correction that was liable to mount up, so it's been left pro tem. - the formulae published include the correction.

I expect to be here till next Monday. Hope you can read this - I've just smashed my spectacles & can't see comfortably unless about four feet.

Yours
Harold Jeffreys