

10th. March 1947.

My dear Race,

The new estimates are

	%	%	
r	56.86134	R'	0.98349 Combinations known or believed
R ₀	2.56677	R ₁	40.75499 to exist have estimates zero if
R"	1.18819	R ₂ '	1.29296 the data do not demonstrate
R ₂	<u>14.10870</u>	R ₂	.14356 their existence.
c	56.72500	C+C ^W	43.27500 R 14.54045 %
			D 58.96698 %

As a check notice that in the two series there are

cc	647
c(C+C ^W)	975
cc,cc ^W ,c ^W C ^W	<u>378</u>
	2000

so that the simple estimate

$$c = \frac{2(647) + 975}{4000} = .5672500$$

agrees with the values obtained.

The accompanying sheet gives

- (i) Frequencies per cent of 36 genotypes
- (ii) Frequencies per cent of 20 phenotypes distinguishable with the six sera used in the second series.
- (iii) Expectations and numbers observed in 26 observation classes for the two series.

Throwing together the ten classes with expectations each less than five, the seventeen classes give $\chi^2 = 8.2443$, for which the degrees of freedom are

$$17 - 8 = 9.$$

Finally

$$\begin{array}{ll} R_0 & 2.56677 \% \\ R'' + R' + R_2 & 2.41524 \% \\ \text{Difference} & .15153 \pm .52474. \end{array}$$

for errors

$$\begin{array}{lll} R''/rR_2 & .2167 & DE \\ R'/r(R_1+R_1^W) & .0602 & CD \\ R_2/R_2(R_1+R_1^W) & .0411 & CE \end{array}$$

The first is still greater than the sum of the other two.

$$2R'R_2/R_1 \quad .000114$$

giving an estimate of R more like 100 than 50 per million; this is because R_2 has gone up.

You're sincerely,

Have you thought of a title for the B.A. Anthropologist?

The matrix of the sampling covariance of those estimates is

γ	R_1	R''	R_3	R'	R_4	R'	R_5	R_6
06,98740	-1,13892	-1,18719	-1,31427	-1,13441	-4,11574	-1,12351	,02664	
	1,52562	3217	-1,13153	2828	-30927	-617	180	
	,60045	-1,39341	-1725	-1,10515	-371	-	589	
		3,24385	-1706	-1,28629	-3979	-	6149	
			,58809	-1,44257	-318	-	190	
				6,74682	-39584	-	9194	
				,57534	-112	-		
					,13389			

	Frequencies expected %	Phenotype	Exp.	Obs.		
rr	15.1020	15.1020	302.040	307	.0815	3rd series
R_0^r	1.9950					
$R_0^R_0$.0659	2.0608	41.216	42	.0149	"
$R''r$.9235	.9235	9.909	7	.8540	Second series
$R''R''$.0141	.0141	.151	0		"
			8.692	12	1.2590	First series
$R_2^R_2$	1.9906					
R_2^R''	.3353	2.3259	24.957	29	.6550	Second
$R_2^R_0$.7243					
R_2^r	10.9657	11.7510	120.088	137	.9444	Second
R_0^R''	.0610					
			130.493	113	2.3450	First
rR'	.7644	.7644	15.288	16	.0332	3rd
$R_1^R_0$	2.0922					
R_1^r	31.6759	33.8186	362.874	354	.2170	Second
R_0^R'	.0505					
$R_1^W R_0^R$.0664					
$R_1^W r$	1.0049	1.0713	11.495	9	.5415	Second
			323.429	326	.0204	First
$R''R'$.0234	.0234	.468	0		3rd
$R_1^R_2$	11.5000					
R_1^R''	.9685					
R_2^R'	.2775	12.9478	138.930	138	.0062	Second
rR_z	.1893					
$R_0^R z$.0125					
$R_2^R z$.0687					Second
$R''R_z$.0058	.0745	.799	0		
$R_1^W R_2^R$.3648					
$R_1^W R''$.0307	.3955	4.244	6		Second
			124.383	126	.0210	First
$R' R'$.0097	.0097	.194	0		3rd
$R_1^R_1$	16.6097					
R_1^R'	.8016	17.4113	186.823	178	.4167	Second
$R_1^W R_1^R$	1.0539					
$R_1^W R'$.0254	1.0793	11.581	12	.0152	Second
$R_1^W R_1^W$.0167	.0167	.179	0		Second
			171.563	183	.7624	First
$R_1^R z$.1985					
$R' R_z$.0048	.2033	2.181	4		Second
$R_1^W R_z$.0062	.0062	.067	0		Second
$R_z^R z$.0006	.0006	.006	0		Second
			1.948	1		First
		99.9999	199.998	2000		
Sum of 10 small classes		10.237	11	.0569		

$$\chi^2 = 8.2443$$

17 - 8

$$n = 9$$