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11th April 2013

## All-sky search for periodic gravitational waves in the full S5 LIGO data

J. Abadie, ${ }^{1, a}$ B. P. Abbott, ${ }^{1, a}$ R. Abbott, ${ }^{1, a}$ T. D. Abbott, ${ }^{2, a}$ M. Abernathy, ${ }^{3, a}$ T. Accadia, ${ }^{4, b}$ F. Acernese, ${ }^{5 \mathrm{a}, 5 \mathrm{c}, \mathrm{b}}$ C. Adams, ${ }^{6, b}$ R. Adhikari, ${ }^{1, a}$ C. Affeldt, ${ }^{7,8, b}$ P. Ajith, ${ }^{1, a}$ B. Allen, ${ }^{7,9,8, b}$ G. S. Allen, ${ }^{10, a}$ E. Amador Ceron, ${ }^{9, a}$ D. Amariutei, ${ }^{11, a}$ R. S. Amin, ${ }^{12, a}$ S. B. Anderson, ${ }^{1, a}$ W. G. Anderson, ${ }^{9, a}$ K. Arai, ${ }^{1, a}$ M. A. Arain, ${ }^{11, a}$ M. C. Araya, ${ }^{1, a}$ S. M. Aston, ${ }^{13, a}$ P. Astone, ${ }^{14 \mathrm{a}, \mathrm{b}}$ D. Atkinson, ${ }^{15, a}$ P. Aufmuth, ${ }^{8,7, \mathrm{a}, \mathrm{b}}$ C. Aulbert, ${ }^{7,8, \mathrm{~b}}$ B. E. Aylott, ${ }^{13, \mathrm{a}}$ S. Babak, ${ }^{16, a}$ P. Baker, ${ }^{17, \mathrm{a}}$ G. Ballardin, ${ }^{18, b}$ S. Ballmer, ${ }^{19, \mathrm{a}}$ D. Barker, ${ }^{15, \mathrm{a}}$ F. Barone, ${ }^{5 \mathrm{a}, 5 \mathrm{c}, \mathrm{b}}$ B. Barr, ${ }^{3, a}$ P. Barriga, ${ }^{20, a}$ L. Barsotti, ${ }^{21, \mathrm{a}}$ M. Barsuglia, ${ }^{22, b}$ M. A. Barton, ${ }^{15, \mathrm{a}}$ I. Bartos, ${ }^{23, a}$ R. Bassiri, ${ }^{3, \mathrm{a}}$ M. Bastarrika, ${ }^{3, \mathrm{a}}$ A. Basti, ${ }^{24 \mathrm{a}, 24 \mathrm{~b}, \mathrm{~b}}$ J. Batch, ${ }^{15, \mathrm{a}}$ J. Bauchrowitz, ${ }^{7,8, \mathrm{~b}}$ Th. S. Bauer, ${ }^{25 \mathrm{a}, \mathrm{b}}$ M. Bebronne, ${ }^{4, b}$ B. Behnke, ${ }^{16, a}$ M. G. Beker, ${ }^{25 a, b}$ A.S. Bell, ${ }^{3, a}$ A. Belletoile, ${ }^{4, b}$ I. Belopolski, ${ }^{23, a}$ M. Benacquista, ${ }^{26, a}$ J. M. Berliner, ${ }^{15, a}$ A. Bertolini, ${ }^{7,8, b}$ J. Betzwieser, ${ }^{1, a}$ N. Beveridge, ${ }^{3, a}$ P. T. Beyersdorf, ${ }^{27, a}$ I. A. Bilenko, ${ }^{28, a}$ G. Billingsley, ${ }^{1, a}$ J. Birch, ${ }^{6, a}$ R. Biswas, ${ }^{26, a}$ M. Bitossi, ${ }^{24 a, b}$ M. A. Bizouard, ${ }^{29 a, b}$ E. Black, ${ }^{1, a}$ J. K. Blackburn, ${ }^{1, a}$ L. Blackburn, ${ }^{30, a}$ D. Blair, ${ }^{20, a}$ B. Bland, ${ }^{15, \mathrm{a}}$ M. Blom, ${ }^{25 \mathrm{a}, \mathrm{b}}$ O. Bock, ${ }^{7,8, \mathrm{~b}}$ T. P. Bodiya, ${ }^{21, \mathrm{a}}$ C. Bogan, ${ }^{7,8, \mathrm{~b}}$ R. Bondarescu, ${ }^{31, \mathrm{a}}$ F. Bondu, ${ }^{32 \mathrm{~b}, \mathrm{~b}}$ L. Bonelli, ${ }^{24 a, 24 b, b}$ R. Bonnand, ${ }^{33, b}$ R. Bork, ${ }^{1, a}$ M. Born, ${ }^{7,8, b}$ V. Boschi, ${ }^{24 a, b}$ S. Bose, ${ }^{34, a}$ L. Bosi, ${ }^{35 a, b}$ B. Bouhou, ${ }^{22, b}$ S. Braccini, ${ }^{24 a, b}$ C. Bradaschia, ${ }^{24 a, b}$ P. R. Brady, ${ }^{9, a}$ V. B. Braginsky, ${ }^{28, a}$ M. Branchesi, ${ }^{36 \mathrm{a}, 36 \mathrm{~b}, \mathrm{~b}}$ J. E. Brau, ${ }^{37, a}$ J. Breyer, ${ }^{7,8, b}$ T. Briant, ${ }^{38, b}$ D. O. Bridges, ${ }^{6, a}$ A. Brillet, ${ }^{32 a, b}$ M. Brinkmann, ${ }^{7,8, b}$ V. Brisson, ${ }^{29 a, b}$ M. Britzger, ${ }^{7,8, b}$ A. F. Brooks, ${ }^{1, a}$ D. A. Brown, ${ }^{19, a}$ A. Brummit, ${ }^{39, a}$ T. Bulik, ${ }^{40 \mathrm{~b}, 40 \mathrm{c}, \mathrm{b}}$ H. J. Bulten, ${ }^{25 \mathrm{a}, 25 \mathrm{~b}, \mathrm{~b}}$ A. Buonanno, ${ }^{41, \mathrm{a}}$ J. Burguet-Castell, ${ }^{9, \mathrm{a}}$ O. Burmeister, ${ }^{7,8, b}$ D. Buskulic, ${ }^{4, \mathrm{~b}}$ C. Buy, ${ }^{22, \mathrm{~b}}$ R. L. Byer, ${ }^{10, \mathrm{a}}$ L. Cadonati, ${ }^{42, \mathrm{a}}$ G. Cagnoli, ${ }^{36 \mathrm{a}, \mathrm{b}}$ E. Calloni, ${ }^{5 \mathrm{a}, 5 \mathrm{~b}, \mathrm{~b}}$ J. B. Camp, ${ }^{30, a}$ P. Campsie, ${ }^{3, a}$ J. Cannizzo, ${ }^{30, a}$ K. Cannon, ${ }^{44, a}$ B. Canuel, ${ }^{18, b}$ J. Cao, ${ }^{45, a}$ C. D. Capano, ${ }^{19, a}$ F. Carbognani, ${ }^{18, b}$ S. Caride, ${ }^{46, a}$ S. Caudill, ${ }^{12, a}$ M. Cavaglià, ${ }^{43, a}$ F. Cavalier, ${ }^{29 a, b}$ R. Cavalieri, ${ }^{18, b}$ G. Cella, ${ }^{24 a, b}$ C. Cepeda, ${ }^{1, a}$ E. Cesarini, ${ }^{36 b, b}$ O. Chaibi, ${ }^{32 a, b}$ T. Chalermsongsak, ${ }^{1, a}$ E. Chalkley, ${ }^{13, a}$ P. Charlton, ${ }^{47, a}$ E. Chassande-Mottin, ${ }^{22, b}$ S. Chelkowski, ${ }^{13, a}$ Y. Chen, ${ }^{48, \mathrm{a}}$ A. Chincarini, ${ }^{49, \mathrm{~b}}$ A. Chiummo, ${ }^{18, \mathrm{~b}}$ H. Cho, ${ }^{50, \mathrm{a}}$ N. Christensen, ${ }^{51, \mathrm{a}}$ S. S. Y. Chua, ${ }^{52, \mathrm{a}}$ C. T. Y. Chung, ${ }^{53, \mathrm{a}}$
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Morgia, ${ }^{55 \mathrm{a}, 55 \mathrm{~b}, \mathrm{~b}}$ T. Mori, ${ }^{71, \mathrm{a}}$ S. Mosca, ${ }^{5 \mathrm{a}, 5 \mathrm{~b}, \mathrm{~b}}$ K. Mossavi, ${ }^{7,8, b}$ B. Mours, ${ }^{4, b}$ C. M. Mow-Lowry, ${ }^{52, a}$ C. L. Mueller, ${ }^{11, a}$ G. Mueller, ${ }^{11, a}$ S. Mukherjee, ${ }^{26, a}$ A. Mullavey, ${ }^{52, a}$ H. Müller-Ebhardt, ${ }^{7,8, b}$ J. Munch, ${ }^{66, a}$ D. Murphy ${ }^{23, a}$ P. G. Murray, ${ }^{3, a}$ A. Mytidis, ${ }^{11, a}$ T. Nash, ${ }^{1, a}$ L. Naticchioni, ${ }^{14 a, 14 b, b}$ R. Nawrodt, ${ }^{3, a}$ V. Necula, ${ }^{11, a}$ J. Nelson, ${ }^{3, a}$ G. Newton, ${ }^{3, a}$ A. Nishizawa, ${ }^{71, a}$ F. Nocera, ${ }^{18, b}$ D. Nolting, ${ }^{6, a}$ L. Nuttall, ${ }^{54, a}$ E. Ochsner, ${ }^{41, \mathrm{a}}$ J. O'Dell, ${ }^{39, \mathrm{a}}$ E. Oelker, ${ }^{21, \mathrm{a}}$ G. H. Ogin, ${ }^{1, \mathrm{a}}$ J. J. Oh, ${ }^{69, \mathrm{a}}$ S. H. Oh, ${ }^{69, \mathrm{a}}$ R. G. Oldenburg, ${ }^{9, \mathrm{a}}$ B. O'Reilly, ${ }^{6, \mathrm{a}}$ R. O'Shaughnessy, ${ }^{9, a}$ C. Osthelder, ${ }^{1, \mathrm{a}}$ C.D. Ott, ${ }^{48, a}$ D. J. Ottaway, ${ }^{66, a}$ R. S. Ottens, ${ }^{11, \mathrm{a}}$ H. Overmier, ${ }^{6, \mathrm{a}}$ B. J. Owen, ${ }^{31, \mathrm{a}}$ A. Page, ${ }^{13, \mathrm{a}}$ G. Pagliaroli, ${ }^{55 \mathrm{a}, 55 \mathrm{c}, \mathrm{b}}$ L. Palladino, ${ }^{55 \mathrm{a}, 55 \mathrm{c}, \mathrm{b}}$ C. Palomba, ${ }^{14 \mathrm{a}, \mathrm{b}}$ Y. Pan, ${ }^{41, \mathrm{a}}$ C. Pankow, ${ }^{11, \mathrm{a}}$ F. Paoletti, ${ }^{24 \mathrm{a}, 18, \mathrm{~b}}$ M. A. Papa, ${ }^{16,9, a}$ M. Parisi, ${ }^{5 a, 5 b, b}$ A. Pasqualetti, ${ }^{18, b}$ R. Passaquieti, ${ }^{24 a, 24 b, b}$ D. Passuello, ${ }^{24 a, b}$ P. Patel, ${ }^{1, a}$ M. Pedraza, ${ }^{1, a}$ P. Peiris, ${ }^{82, a}$ L. Pekowsky, ${ }^{19, a}$ S. Penn, ${ }^{83, a}$ C. Peralta, ${ }^{16, a}$ A. Perreca, ${ }^{19, a}$ G. Persichetti, ${ }^{5 \mathrm{a}, 5 \mathrm{~b}, \mathrm{~b}}$ M. Phelps, ${ }^{1, a}$ M. Pickenpack, ${ }^{7,8, b}$ F. Piergiovanni, ${ }^{36 a, 36 b, b}$ M. Pietka, ${ }^{40 d, b}$ L. Pinard, ${ }^{33, b}$ I. M. Pinto, ${ }^{84, a}$ M. Pitkin,,${ }^{3, a}$ H. J. Pletsch, ${ }^{7,8, b}$ M. V. Plissi, ${ }^{3, \mathrm{a}}$ R. Poggiani, ${ }^{24 \mathrm{a}, 24 \mathrm{~b}, \mathrm{~b}}$ J. Pöld, ${ }^{7,8, b}$ F. Postiglione, ${ }^{56, a}$ M. Prato, ${ }^{49, \mathrm{~b}}$ V. Predoi, ${ }^{54, \mathrm{a}}$ L. R. Price, ${ }^{1, \mathrm{a}}$ M. Prijatelj, ${ }^{7,8, b}$ M. Principe, ${ }^{84, \mathrm{a}}$ S. Privitera, ${ }^{1, \mathrm{a}}$ R. Prix, ${ }^{7,8, \mathrm{~b}}$ G. A. Prodi, ${ }^{59 \mathrm{a}, 59 \mathrm{~b}, \mathrm{~b}}$ L. Prokhorov, ${ }^{28, \mathrm{a}}$ O. Puncken, ${ }^{7,8, b}$ M. Punturo, ${ }^{35 \mathrm{a}, \mathrm{b}}$ P. Puppo, ${ }^{14 a, b}$ V. Quetschke, ${ }^{26, a}$ F. J. Raab, ${ }^{15, a}$ D. S. Rabeling, ${ }^{25 a, 25 b, b}$ I. Rácz, ${ }^{58, b}$ H. Radkins, ${ }^{15, a}$ P. Raffai, ${ }^{65, a}$ M. Rakhmanov, ${ }^{26, a}$ C. R. Ramet, ${ }^{6, a}$ B. Rankins, ${ }^{43, a}$ P. Rapagnani, ${ }^{14 a, 14 b, b}$ V. Raymond, ${ }^{63, a}$ V. Re, ${ }^{55 a, 55 b, b}$ K. Redwine, ${ }^{23, a}$
C. M. Reed, ${ }^{15, a}$ T. Reed, ${ }^{85, a}$ T. Regimbau, ${ }^{32 a, b}$ S. Reid, ${ }^{3, a}$ D. H. Reitze, ${ }^{11, a}$ F. Ricci, ${ }^{14 a, 14 b, b}$ R. Riesen, ${ }^{6, a}$ K. Riles, ${ }^{46, a}$ N. A. Robertson, ${ }^{1,3, a}$ F. Robinet, ${ }^{29 \mathrm{a}, \mathrm{b}}$ C. Robinson, ${ }^{54, \mathrm{a}}$ E. L. Robinson, ${ }^{16, \mathrm{a}}$ A. Rocchi, ${ }^{55 \mathrm{a}, \mathrm{b}}$ S. Roddy, ${ }^{6, \mathrm{a}}$ C. Rodriguez, ${ }^{63, \mathrm{a}}$ M. Rodruck, ${ }^{15, a}$ L. Rolland, ${ }^{4, b}$ J. Rollins, ${ }^{23, a}$ J. D. Romano, ${ }^{26, a}$ R. Romano, ${ }^{5 \mathrm{a}, 5 \mathrm{c}, \mathrm{b}}$ J. H. Romie, ${ }^{6, \mathrm{a}}$ D. Rosińska, ${ }^{40 \mathrm{c}, 40 f, b}$ C. Röver, ${ }^{7,8, b}$ S. Rowan, ${ }^{3, a}$ A. Rüdiger, ${ }^{7,8, b}$ P. Ruggi, ${ }^{18, b}$ K. Ryan, ${ }^{15, \mathrm{a}}$ H. Ryll, ${ }^{7,8, b}$ P. Sainathan, ${ }^{11, \mathrm{a}}$ M. Sakosky, ${ }^{15, \mathrm{a}}$ F. Salemi, ${ }^{7,8, b}$ A. Samblowski , ${ }^{7,8, a}$ L. Sammut, ${ }^{53, a}$ L. Sancho de la Jordana, ${ }^{72, a}$ V. Sandberg, ${ }^{15, a}$ S. Sankar, ${ }^{21, a}$ V. Sannibale, ${ }^{1, a}$ L. Santamaría, ${ }^{1, a}$ I. Santiago-Prieto, ${ }^{3, a}$ G. Santostasi, ${ }^{86, a}$ B. Sassolas, ${ }^{33, b}$ B. S. Sathyaprakash, ${ }^{54, a}$ S. Sato, ${ }^{71, a}$ P. R. Saulson, ${ }^{19, a}$ R. L. Savage, ${ }^{15, a}$ R. Schilling, ${ }^{7,8, b}$ S. Schlamminger, ${ }^{87, a}$ R. Schnabel, ${ }^{7,8, b}$
R. M. S. Schofield, ${ }^{37, a}$ B. Schulz, ${ }^{7,8, b}$ B. F. Schutz, ${ }^{16,54, a}$ P. Schwinberg, ${ }^{15, a}$ J. Scott, ${ }^{3, a}$ S. M. Scott, ${ }^{52, a}$ A. C. Searle, ${ }^{1, a}$ F. Seifert, ${ }^{1, a}$ D. Sellers, ${ }^{6, a}$ A. S. Sengupta, ${ }^{1, a}$ D. Sentenac, ${ }^{18, b}$ A. Sergeev, ${ }^{75, a}$ D. A. Shaddock, ${ }^{52, a}$ M. Shaltev, ${ }^{7,8, b}$ B. Shapiro, ${ }^{21, a}$ P. Shawhan, ${ }^{41, a}$ D. H. Shoemaker, ${ }^{21, a}$ A. Sibley, ${ }^{6, a}$ X. Siemens, ${ }^{9, a}$ D. Sigg, ${ }^{15, a}$ A. Singer, ${ }^{1, a}$ L. Singer, ${ }^{1, a}$ A. M. Sintes, ${ }^{72, a}$ G. Skelton, ${ }^{9, a}$ B. J. J. Slagmolen, ${ }^{52, a}$ J. Slutsky, ${ }^{12, a}$ J. R. Smith, ${ }^{2, a}$ M. R. Smith, ${ }^{1, a}$ N. D. Smith, ${ }^{21, a}$ R. J. E. Smith, ${ }^{13, a}$ K. Somiya, ${ }^{48, a}$ B. Sorazu, ${ }^{3, a}$ J. Soto, ${ }^{21, a}$ F. C. Speirits, ${ }^{3, a}$ L. Sperandio, ${ }^{55 a, 55 b, b}$ M. Stefszky, ${ }^{52, a}$ A. J. Stein, ${ }^{21, a}$ E. Steinert, ${ }^{15, a}$ J. Steinlechner, ${ }^{7,8, b}$ S. Steinlechner, ${ }^{7,8, b}$ S. Steplewski, ${ }^{34, a}$ A. Stochino, ${ }^{1, a}$ R. Stone, ${ }^{26, a}$ K. A. Strain, ${ }^{3, a}$ S. Strigin, ${ }^{28, a}$ A. S. Stroeer, ${ }^{26, a}$ R. Sturani, ${ }^{36 a, 36 b, b}$ A. L. Stuver, ${ }^{6, a}$ T. Z. Summerscales, ${ }^{88, a}$ M. Sung, ${ }^{12, a}$ S. Susmithan, ${ }^{20, a}$ P. J. Sutton, ${ }^{54, a}$ B. Swinkels, ${ }^{18, b}$ M. Tacca, ${ }^{18, b}$ L. Taffarello, ${ }^{59 \mathrm{c}, \mathrm{b}}$ D. Talukder, ${ }^{34, \mathrm{a}}$ D. B. Tanner, ${ }^{11, \mathrm{a}}$ S. P. Tarabrin, ${ }^{7,8, b}$ J. R. Taylor, ${ }^{7,8, b}$ R. Taylor, ${ }^{1, a}$ P. Thomas, ${ }^{15, \mathrm{a}}$ K. A. Thorne,,${ }^{6, \mathrm{a}}$ K. S. Thorne, ${ }^{48, \mathrm{a}}$ E. Thrane, ${ }^{61, \mathrm{a}}$ A. Thüring, ${ }^{8,7, \mathrm{a}, \mathrm{b}} \mathrm{C}$. Titsler, ${ }^{31, \mathrm{a}}$ K. V. Tokmakov, ${ }^{79, \mathrm{a}}$ A. Toncelli, ${ }^{24 \mathrm{a}, 24 \mathrm{~b}, \mathrm{~b}}$ M. Tonelli, ${ }^{24 \mathrm{a}, 24 \mathrm{~b}, \mathrm{~b}}$ O. Torre, ${ }^{24 \mathrm{a}, 24 \mathrm{c}, \mathrm{b}}$ C. Torres, ${ }^{6, \mathrm{a}}$ C. I. Torrie, ${ }^{1,3, a}$ E. Tournefier, ${ }^{4, b}$ F. Travasso, ${ }^{35 \mathrm{a}, 35 \mathrm{~b}, \mathrm{~b}}$ G. Traylor, ${ }^{6, a}$ M. Trias, ${ }^{72, \mathrm{a}}$ K. Tseng, ${ }^{10, \mathrm{a}}$ D. Ugolini, ${ }^{89, a}$ K. Urbanek, ${ }^{10, a}$ H. Vahlbruch, ${ }^{8,7, a, b}$ G. Vajente, ${ }^{24 a, 24 b, b}$ M. Vallisneri, ${ }^{48, a}$ J. F. J. van den Brand, ${ }^{25 a, 25 b, b}$ C. Van Den Broeck, ${ }^{25 a, b}$
S. van der Putten, ${ }^{25 a, b}$ A. A. van Veggel,,${ }^{3, \mathrm{a}}$ S. Vass, ${ }^{1, \mathrm{a}}$ M. Vasuth, ${ }^{58, \mathrm{~b}}$ R. Vaulin, ${ }^{21, \mathrm{a}}$ M. Vavoulidis, ${ }^{29 \mathrm{a}, \mathrm{b}}$ A. Vecchio, ${ }^{13, \mathrm{a}}$ G. Vedovato, ${ }^{59 \mathrm{c}, \mathrm{b}}$ J. Veitch, ${ }^{54, \mathrm{a}}$ P. J. Veitch, ${ }^{66, \mathrm{a}}$ C. Veltkamp, ${ }^{7,8, \mathrm{~b}}$ D. Verkindt, ${ }^{4, \mathrm{~b}}$ F. Vetrano, ${ }^{36 \mathrm{a}, 36 \mathrm{~b}, \mathrm{~b}}$ A. Viceré, ${ }^{36 a, 36 b, b}$ A. E. Villar, ${ }^{1, \mathrm{a}}$ J.-Y. Vinet, ${ }^{32 \mathrm{a}, \mathrm{b}}$ S. Vitale, ${ }^{68, \mathrm{a}}$ S. Vitale, ${ }^{25 \mathrm{a}, \mathrm{b}}$ H. Vocca, ${ }^{35 a, b}$ C. Vorvick, ${ }^{15, a}$ S. P. Vyatchanin, ${ }^{28, a}$ A. Wade, ${ }^{52, a}$ S. J. Waldman, ${ }^{21, \mathrm{a}}$ L. Wallace, ${ }^{1, \mathrm{a}}$ Y. Wan, ${ }^{45, \mathrm{a}}$ X. Wang, ${ }^{45, \mathrm{a}}$ Z. Wang, ${ }^{45, \mathrm{a}}$ A. Wanner, ${ }^{7,8, \mathrm{~b}}$ R. L. Ward, ${ }^{22, \mathrm{~b}}$ M. Was, ${ }^{29 \mathrm{a}, \mathrm{b}}$ P. Wei, ${ }^{19, \mathrm{a}}$ M. Weinert, ${ }^{7,8, b}$ A. J. Weinstein, ${ }^{1, \mathrm{a}}$ R. Weiss, ${ }^{21, \mathrm{a}}$ L. Wen, ${ }^{48,20, \mathrm{a}}$ S. Wen, ${ }^{6, \mathrm{a}}$ P. Wessels, ${ }^{7,8, b}$ M. West, ${ }^{19, \mathrm{a}}$ T. Westphal, ${ }^{7,8, \mathrm{~b}}$ K. Wette, ${ }^{7,8, \mathrm{~b}}$ J. T. Whelan, ${ }^{82, \mathrm{a}}$ S.E. Whitcomb, ${ }^{1,20, \mathrm{a}}$ D. White, ${ }^{57, \mathrm{a}}$ B. F. Whiting, ${ }^{11, \mathrm{a}}$ C. Wilkinson, ${ }^{15, \mathrm{a}}$ P. A. Willems, ${ }^{1, \mathrm{a}}$ H. R. Williams, ${ }^{31, \mathrm{a}}$ L. Williams, ${ }^{11, \mathrm{a}}$ B. Willke, ${ }^{7,8, \mathrm{~b}}$ L. Winkelmann, ${ }^{7,8, \mathrm{~b}}$ W. Winkler, ${ }^{7,8, \mathrm{~b}}$ C. C. Wipf, ${ }^{21, \mathrm{a}}$ A. G. Wiseman, ${ }^{9, a}$ H. Wittel, ${ }^{7,8, b}$ G. Woan, ${ }^{3, a}$ R. Wooley, ${ }^{6, a}$ J. Worden, ${ }^{15, a}$ J. Yablon, ${ }^{63, a}$ I. Yakushin, ${ }^{6, a}$ H. Yamamoto, ${ }^{1, a}$ K. Yamamoto, ${ }^{7,8, b}$ H. Yang, ${ }^{48, a}$ D. Yeaton-Massey, ${ }^{1, a}$ S. Yoshida, ${ }^{90, a}$ P. Yu, ${ }^{9, a}$ M. Yvert, ${ }^{4, b}$ A. Zadroźny, ${ }^{40 e, b}$ M. Zanolin, ${ }^{68, a}$ J.-P. Zendri, ${ }^{59 \mathrm{c}, \mathrm{b}}$ F. Zhang, ${ }^{45, \mathrm{a}}$ L. Zhang, ${ }^{1, \mathrm{a}}$ W. Zhang, ${ }^{45, \mathrm{a}}$ Z. Zhang, ${ }^{20, a}$ C. Zhao, ${ }^{20, \mathrm{a}}$ N. Zotov, ${ }^{85, \mathrm{a}}$ M. E. Zucker, ${ }^{21, a}$ and J. Zweizig ${ }^{1, a}$
( ${ }^{\text {a }}$ The LIGO Scientific Collaboration)
( ${ }^{\text {b The Virgo Collaboration) }}$
${ }^{1}$ LIGO-California Institute of Technology, Pasadena, California 91125, USA
${ }^{2}$ California State University Fullerton, Fullerton, California 92831, USA
${ }^{3}$ SUPA, University of Glasgow, Glasgow, G12 8QQ, United Kingdom
${ }^{4}$ Laboratoire d'Annecy-le-Vieux de Physique des Particules (LAPP), Université de Savoie,
CNRS/IN2P3, F-74941 Annecy-Le-Vieux, France
${ }^{5 \mathrm{a}}$ INFN, Sezione di Napoli, Italy
${ }^{5 b}$ Università di Napoli 'Federico II,' Italy
${ }^{5 c}$ Complesso Universitario di Monte S. Angelo, I-80126 Napoli and Università di Salerno, Fisciano, I-84084 Salerno, Italy
${ }^{6}$ LIGO-Livingston Observatory, Livingston, Louisiana 70754, USA
${ }^{7}$ Albert-Einstein-Institut, Max-Planck-Institut für Gravitationsphysik, D-30167 Hannover, Germany
${ }^{8}$ Leibniz Universität Hannover, D-30167 Hannover, Germany
${ }^{9}$ University of Wisconsin-Milwaukee, Milwaukee, Wisconsin 53201, USA
${ }^{10}$ Stanford University, Stanford, California 94305, USA
${ }^{11}$ University of Florida, Gainesville, Florida 32611, USA
${ }^{12}$ Louisiana State University, Baton Rouge, Louisiana 70803, USA
${ }^{13}$ University of Birmingham, Birmingham, B15 2TT, United Kingdom
${ }^{14 a}$ INFN, Sezione di Roma, I-00185 Roma, Italy
${ }^{14 \mathrm{~b}}$ Università 'La Sapienza,' I-00185 Roma, Italy
${ }^{15}$ LIGO-Hanford Observatory, Richland, Washington 99352, USA
${ }^{16}$ Albert-Einstein-Institut, Max-Planck-Institut für Gravitationsphysik, D-14476 Golm, Germany
${ }^{17}$ Montana State University, Bozeman, Montana 59717, USA
${ }^{18}$ European Gravitational Observatory (EGO), I-56021 Cascina (PI), Italy
${ }^{19}$ Syracuse University, Syracuse, New York 13244, USA
${ }^{20}$ University of Western Australia, Crawley, Washington 6009, Australia
${ }^{21}$ LIGO-Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA
${ }^{22}$ Laboratoire AstroParticule et Cosmologie (APC), Université Paris Diderot, CNRS: IN2P3, CEA: DSM/IRFU, Observatoire de Paris,
10 rue A. Domon et L. Duquet, 75013 Paris, France
${ }^{23}$ Columbia University, New York, New York 10027, USA
${ }^{24 \mathrm{a}}$ INFN, Sezione di Pisa, Italy
${ }^{24 \mathrm{~b}}$ Università di Pisa, Italy
${ }^{24 \mathrm{c}}$ Università di Siena, I-53100 Siena, Italy
${ }^{25 a}$ Nikhef, Science Park, Amsterdam, The Netherlands
${ }^{25 b}$ VU University Amsterdam, De Boelelaan 1081, 1081 HV Amsterdam, The Netherlands
${ }^{26}$ The University of Texas at Brownsville and Texas Southmost College, Brownsville, Texas 78520, USA
${ }^{27}$ San Jose State University, San Jose, California 95192, USA
${ }^{28}$ Moscow State University, Moscow, 119992, Russia
${ }^{29 \mathrm{a}}$ LAL, Université Paris-Sud, IN2P3/CNRS, F-91898 Orsay, France
${ }^{29 b}$ ESPCI, CNRS, F-75005 Paris, France
${ }^{30}$ NASA/Goddard Space Flight Center, Greenbelt, Maryland 20771, USA
${ }^{31}$ The Pennsylvania State University, University Park, Pennsylvania 16802, USA
${ }^{32 a}$ Université Nice-Sophia-Antipolis, CNRS, Observatoire de la Côte d'Azur, F-06304 Nice, France
${ }^{32 \mathrm{~b}}$ Institut de Physique de Rennes, CNRS, Université de Rennes 1, 35042 Rennes, France
${ }^{33}$ Laboratoire des Matériaux Avancés (LMA), IN2P3/CNRS, F-69622 Villeurbanne, Lyon, France

${ }^{34}$ Washington State University, Pullman, Washington 99164, USA<br>${ }^{35}$ INFN, Sezione di Perugia, I-06123 Perugia, Italy<br>${ }^{35 \mathrm{~b}}$ Università di Perugia, I-06123 Perugia, Italy<br>${ }^{36 \mathrm{a}}$ INFN, Sezione di Firenze, I-50019 Sesto Fiorentino, Italy<br>${ }^{36 \mathrm{~b}}$ Università degli Studi di Urbino 'Carlo Bo,' I-61029 Urbino, Italy<br>${ }^{37}$ University of Oregon, Eugene, Oregon 97403, USA<br>${ }^{38}$ Laboratoire Kastler Brossel, ENS, CNRS, UPMC, Université Pierre et Marie Curie, 4 Place Jussieu, F-75005 Paris, France<br>${ }^{39}$ Rutherford Appleton Laboratory, HSIC, Chilton, Didcot, Oxon OX11 OQX, United Kingdom<br>${ }^{40 \mathrm{a}}$ IM-PAN 00-956 Warsaw, Poland<br>${ }^{40 \mathrm{~b}}$ Astronomical Observatory Warsaw University, 00-478 Warsaw, Poland<br>${ }^{40 \mathrm{c}}$ CAMK-PAN 00-716 Warsaw, Poland<br>${ }^{40 \mathrm{~d}}$ Biatystok University 15-424 Biatystok, Poland ${ }^{40 e}$ IPJ 05-400 Świerk-Otwock, Poland<br>${ }^{40 f}$ Institute of Astronomy 65-265 Zielona Góra, Poland<br>${ }^{41}$ University of Maryland, College Park, Maryland 20742, USA<br>${ }^{42}$ University of Massachusetts-Amherst, Amherst, Massachusetts 01003, USA<br>${ }^{43}$ The University of Mississippi, University, Mississippi 38677, USA<br>${ }^{44}$ Canadian Institute for Theoretical Astrophysics, University of Toronto, Toronto, Ontario, M5S 3H8, Canada<br>${ }^{45}$ Tsinghua University, Beijing 100084, China<br>${ }^{46}$ University of Michigan, Ann Arbor, Michigan 48109, USA<br>${ }^{47}$ Charles Sturt University, Wagga Wagga, NSW 2678, Australia<br>${ }^{48}$ Caltech-CaRT, Pasadena, California 91125, USA<br>${ }^{49}$ INFN, Sezione di Genova, I-16146 Genova, Italy<br>${ }^{50}$ Pusan National University, Busan 609-735, Korea<br>${ }^{51}$ Carleton College, Northfield, Minnesota 55057, USA<br>${ }^{52}$ Australian National University, Canberra, ACT 0200, Australia<br>${ }^{53}$ The University of Melbourne, Parkville, VIC 3010, Australia<br>${ }^{54}$ Cardiff University, Cardiff, CF24 3AA, United Kingdom<br>${ }^{55 a}$ INFN, Sezione di Roma Tor Vergata, Italy<br>${ }^{55 b}$ Università di Roma Tor Vergata, I-00133 Roma, Italy<br>${ }^{55 \mathrm{c}}$ Università dell'Aquila, I-67100 L'Aquila, Italy<br>${ }^{56}$ University of Salerno, I-84084 Fisciano (Salerno), Italy and INFN (Sezione di Napoli), Italy<br>${ }^{57}$ The University of Sheffield, Sheffield S10 2TN, United Kingdom<br>${ }^{58}$ RMKI, H-1121 Budapest, Konkoly Thege Miklós út 29-33, Hungary<br>${ }^{59 \mathrm{a}}$ INFN, Gruppo Collegato di Trento, Italy<br>${ }^{59 \mathrm{~b}}$ Università di Trento, I-38050 Povo, Trento, Italy<br>${ }^{59 \mathrm{c}}$ INFN, Sezione di Padova, I-35131 Padova, Italy<br>${ }^{60}$ Inter-University Centre for Astronomy and Astrophysics, Pune-411007, India<br>${ }^{61}$ University of Minnesota, Minneapolis, Minnesota 55455, USA<br>${ }^{62}$ California Institute of Technology, Pasadena, California 91125, USA<br>${ }^{63}$ Northwestern University, Evanston, Illinois 60208, USA<br>${ }^{64}$ The University of Texas at Austin, Austin, Texas 78712, USA<br>${ }^{65}$ Eötvös Loránd University, Budapest, 1117, Hungary<br>${ }^{66}$ University of Adelaide, Adelaide, SA 5005, Australia<br>${ }^{67}$ University of Szeged, 6720 Szeged, Dóm tér 9, Hungary<br>${ }^{68}$ Embry-Riddle Aeronautical University, Prescott, Arizona 86301, USA<br>${ }^{69}$ National Institute for Mathematical Sciences, Daejeon 305-390, Korea<br>${ }^{70}$ Perimeter Institute for Theoretical Physics, Ontario, Canada, N2L $2 Y 5$<br>${ }^{71}$ National Astronomical Observatory of Japan, Tokyo 181-8588, Japan<br>${ }^{72}$ Universitat de les Illes Balears, E-07122 Palma de Mallorca, Spain<br>${ }^{73}$ Korea Institute of Science and Technology Information, Daejeon 305-806, Korea<br>${ }^{74}$ University of Southampton, Southampton, SO17 1BJ, United Kingdom<br>${ }^{75}$ Institute of Applied Physics, Nizhny Novgorod, 603950, Russia<br>${ }^{76}$ Lund Observatory, Box 43, SE-221 00, Lund, Sweden<br>${ }^{77}$ Hanyang University, Seoul 133-791, Korea<br>${ }^{78}$ Seoul National University, Seoul 151-742, Korea<br>${ }^{79}$ University of Strathclyde, Glasgow, G1 1XQ, United Kingdom<br>${ }^{80}$ Southern University and A\&M College, Baton Rouge, Louisiana 70813, USA<br>${ }^{81}$ University of Rochester, Rochester, New York 14627, USA<br>${ }^{82}$ Rochester Institute of Technology, Rochester, New York 14623, USA<br>${ }^{83}$ Hobart and William Smith Colleges, Geneva, New York 14456, USA

${ }^{84}$ University of Sannio at Benevento, I-82100 Benevento, Italy and INFN (Sezione di Napoli), Italy
${ }^{85}$ Louisiana Tech University, Ruston, Louisiana 71272, USA
${ }^{86}$ McNeese State University, Lake Charles, Louisiana 70609, USA
${ }^{87}$ University of Washington, Seattle, Washington, 98195-4290, USA
${ }^{88}$ Andrews University, Berrien Springs, Michigan 49104, USA
${ }^{89}$ Trinity University, San Antonio, Texas 78212, USA
${ }^{90}$ Southeastern Louisiana University, Hammond, Louisiana 70402, USA
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We report on an all-sky search for periodic gravitational waves in the frequency band $50-800 \mathrm{~Hz}$ and with the frequency time derivative in the range of 0 through $-6 \times 10^{-9} \mathrm{~Hz} / \mathrm{s}$. Such a signal could be produced by a nearby spinning and slightly nonaxisymmetric isolated neutron star in our Galaxy. After recent improvements in the search program that yielded a $10 \times$ increase in computational efficiency, we have searched in two years of data collected during LIGO's fifth science run and have obtained the most sensitive all-sky upper limits on gravitational-wave strain to date. Near 150 Hz our upper limit on worst-case linearly polarized strain amplitude $h_{0}$ is $1 \times 10^{-24}$, while at the high end of our frequency range we achieve a worst-case upper limit of $3.8 \times 10^{-24}$ for all polarizations and sky locations. These results constitute a factor of 2 improvement upon previously published data. A new detection pipeline utilizing a loosely coherent algorithm was able to follow up weaker outliers, increasing the volume of space where signals can be detected by a factor of 10 , but has not revealed any gravitational-wave signals. The pipeline has been tested for robustness with respect to deviations from the model of an isolated neutron star, such as caused by a low-mass or long-period binary companion.

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## I. INTRODUCTION

In this paper we report the results of an all-sky search for continuous, nearly monochromatic gravitational waves on data from LIGO's fifth science (S5) run. The search covered frequencies from 50 through 800 Hz and frequency derivatives from 0 through $-6 \times 10^{-9} \mathrm{~Hz} / \mathrm{s}$.

A number of searches have been carried out previously in LIGO data [1-8], including coherent searches for gravitational radiation from known radio and x-ray pulsars. An Einstein@Home search running on the BOINC infrastructure [9] has performed blind all-sky searches on S4 and S5 data $[10,11]$.

The results in this paper were produced with the PowerFlux search code. It was first described in [1] together with two other semicoherent search pipelines (Hough, Stackslide). The sensitivities of all three methods were compared, with PowerFlux showing better results in frequency bands lacking severe spectral artifacts. A subsequent article [2] based on the first eight months of data from the S 5 run featured improved upper limits and an opportunistic detection search.

The analysis of the full data set from the fifth science run described in this paper has several distinguishing features from previously published results:
(i) The data spanning two years of observation are the most sensitive to date. In particular, the intrinsic detector sensitivity in the low-frequency region of $100-300 \mathrm{~Hz}$ (taking into account integration time) will likely not be surpassed until advanced versions

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## operation.

of the LIGO and Virgo interferometers come into
(ii) The large data volume from the full S 5 run required a rework of the PowerFlux code, resulting in a factor of 10 improvement in speed when iterating over multiple values of possible signal frequency derivative, while reporting more detailed search results. That partially compensated for the large factor in computational cost incurred by analyzing a longer time span, allowing frequencies up to 800 Hz to be searched in a reasonable amount of time. The range of (negative) frequency derivatives considered, as large in magnitude as $-6 \times 10^{-9} \mathrm{~Hz} / \mathrm{s}$, was slightly wider than in the previous search [2]. Thus, this new search supersedes the previous search results up to 800 Hz .
(iii) The detection search has been improved to process outliers down to signal-to-noise ratio SNR $\geq 7$ using data from both the H1 and L1 interferometers. The previous search [2] rejected candidates with combined $\mathrm{SNR} \leq 8.5$. The new lower threshold is at the level of Gaussian noise, and new techniques were used to eliminate random coincidences.
(iv) The follow-up of outliers employs the new loosely coherent algorithm [12].
We have observed no evidence of gravitational radiation and have established the most sensitive upper limits to date in the frequency band $50-800 \mathrm{~Hz}$. Near 150 Hz our strain sensitivity to a neutron star with the most unfavorable sky location and orientation ("worst case") yields a 95\%
confidence level upper limit of $1 \times 10^{-24}$, while at the high end of our frequency range we achieve a worst-case upper limit of $3.8 \times 10^{-24}$.

## II. LIGO INTERFEROMETERS AND S5 SCIENCE RUN

The LIGO gravitational-wave network consists of two observatories, one in Hanford, Washington, and the other in Livingston, Louisiana, separated by a 3000 km baseline. During the S 5 run each site housed one suspended interferometer with 4 km long arms. In addition, the Washington observatory housed a less sensitive 2 km interferometer, the data from which was not used in this search.

The fifth science run spanned a nearly two-year period of data acquisition. This analysis used data from GPS 816070843 (2005 Nov 15 06:20:30 UTC) through GPS 878044141 (2007 Nov 02 13:08:47 UTC). Since interferometers sporadically fall out of operation ("lose lock") due to environmental or instrumental disturbances or for scheduled maintenance periods, the data set is not
contiguous. The Hanford interferometer H1 had a duty factor of $78 \%$, while the Livingston interferometer L1 had a duty factor of $66 \%$. The sensitivity was not uniform, exhibiting $\mathrm{a} \sim 10 \%$ daily variation from anthropogenic activity as well as gradual improvement toward the end of the run $[13,14]$.

## III. THE SEARCH FOR CONTINUOUS GRAVITATIONAL RADIATION

The search results described in this paper assume a classical model of a spinning neutron star with a fixed, asymmetric second moment that produces circularly polarized gravitational radiation along the rotation axis and linearly polarized radiation in the directions perpendicular to the rotation axis. The assumed signal model is thus

$$
\begin{align*}
h(t)= & h_{0}\left(F_{+}(t, \alpha, \delta, \psi) \frac{1+\cos ^{2}(\iota)}{2} \cos (\Phi(t))\right. \\
& \left.+F_{\times}(t, \alpha, \delta, \psi) \cos (\iota) \sin (\Phi(t))\right) \tag{1}
\end{align*}
$$



FIG. 1 (color online). Full S5 upper limits. The upper (green) curve shows worst-case upper limits in analyzed 0.25 Hz bands (see Table I for list of excluded bands). The lower (grey) curve shows upper limits assuming circularly polarized source. The values of solid points (marking non-Gaussian behavior) and circles (marking power line harmonics) are not considered reliable. They are shown to indicate contaminated bands.
where $F_{+}$and $F_{\times}$characterize the detector responses to signals with " + " and " $\times$ " quadrupolar polarizations, the sky location is described by right ascension $\alpha$ and declination $\delta, \iota$ describes the inclination of the source rotation axis to the line of sight, and the phase evolution of the signal is given by the formula

$$
\begin{equation*}
\Phi(t)=2 \pi\left(f_{\text {source }}\left(t-t_{0}\right)+f^{(1)}\left(t-t_{0}\right)^{2} / 2\right)+\phi \tag{2}
\end{equation*}
$$

with $f_{\text {source }}$ being the source frequency and $f^{(1)}$ denoting the first frequency derivative (for which we also use the shorter term spin-down). $\phi$ denotes the initial phase with respect to reference time $t_{0} . t$ is time in the solar system barycenter frame. When expressed as a function of local time of ground-based detectors it includes the sky-position-dependent Doppler shift. We use $\psi$ to denote the polarization angle of the projected source rotation axis in the sky plane.

Our search algorithms calculate power for a bank of such templates and compute upper limits and signal-tonoise ratios for each template based on comparison to templates with nearby frequencies and the same sky location and spin-down.

The search proceeded in two stages. First, the main PowerFlux code was run to establish upper limits and produce lists of outliers with signal-to-noise ratio (SNR) greater than 5 . Next, the loosely coherent pipeline was used to reject or confirm collected outliers.

The upper limits are reported in terms of the worst-case value of $h_{0}$ (which applies to linear polarizations with $\iota=\pi / 2)$ and for the most sensitive circular polarization $(\iota=0$ or $\pi)$. The pipeline does retain some sensitivity, however, to more general gravitational wave polarization models, including a longitudinal component, and to slow amplitude evolution.

The $95 \%$ confidence level upper limits (see Fig. 1) produced in the first stage are based on the overall noise level and largest outlier in strain found for every template in each 0.25 Hz band in the first stage of the pipeline. A follow-up search for detection is carried out for high-SNR outliers found in the first stage. An important distinction is that we do not report upper limits for certain frequency ranges because of contamination by detector artifacts and thus unknown statistical properties. However, the detection search used all analyzed frequency bands with reduced sensitivity in contaminated regions.

From the point of view of the analysis code the contamination by detector artifacts can be roughly separated into regions of non-Gaussian noise statistics, 60 Hz harmonics, and other detector disturbances such as steeply sloped spectrum or sharp instrumental lines due to data acquisition electronics.

## IV. POWERFLUX ALGORITHM AND ESTABLISHMENT OF UPPER LIMITS

The data of the fifth LIGO science run were acquired over a period of nearly two years and comprised over 80000 1800-second Hann-windowed 50\%-overlapped short Fourier transforms (SFTs). Such a large data set posed a significant challenge to the previously described PowerFlux code $[1,15,16]$ :
(i) A 1 Hz band (a typical analysis region) needed more than a gigabyte of memory to store the input data.
(ii) The large time base necessitates particularly fine spin-down steps of $3 \times 10^{-11} \mathrm{~Hz} / \mathrm{s}$ which, in turn, requires 201 spin-down steps to cover the desired range of $\left[-6 \times 10^{-9}, 0\right] \mathrm{Hz} / \mathrm{s}$. The previous searches [1,2] had iterated over only 11 spin-down values.
(iii) The more sensitive data exposed previously unknown detector artifacts that required thorough study.
To overcome these issues, the PowerFlux analysis code was rewritten to be more memory efficient, to achieve a $10 \times$ reduction in large-run computing time, and to provide more information useful in the follow-up detection search. Changes in architecture allowed us to implement the loosely coherent statistic [12] which was invaluable in automating the detection search and pushing down the outlier noise floor. This is discussed in more detail in Sec. V.

A flow chart of the PowerFlux program is shown in Fig. 2. There are three major flows of data. The detector response involves computation of amplitude response, detector position and Doppler shifts based on knowledge of sky location searched, and timing of the input data. The data set is characterized by computing data quality statistics independent of sky position. Finally, the weighted power sums are computed from the input data, folding in information on detector response and data quality to optimize performance of the code that searches over all sky positions, establishes upper limits, and finds outliers.


FIG. 2 (color online). Flow chart of PowerFlux code.

The noise decomposition, instrumental line detection, SFT veto, and detector response components are the same as in the previous version of PowerFlux.

The power sum code has been reworked to incorporate the following improvements:
(i) Instead of computing power sums for specific polarizations for the entire data set, we compute partial power sums: terms in the polarization response that are additive functions of the data. This allows us to sample more polarizations, or to combine or omit subsets of data, at a small penalty in computing cost.
(ii) The partial power sums are cached, greatly reducing redundant computations.
(iii) The partial power sums are added hierarchically (see IVE) by a summing engine which makes it possible to produce simultaneously upper limits and outliers for different combinations of interferometers and time segments. This improvement significantly reduces the time needed for the follow-up analysis and makes possible detection of long duration signals present in only part of the data.
(iv) Instead of including the frequency evolution model in the summing engine, the engine takes a summing plan (representing a series of frequency shifts), and contains heuristics to improve cache performance by partitioning SFTs based on the summing plan. A separate module generates the summing plan for a specific frequency evolution model. This will allow us in the future to add different frequency models while still using the same caching and summing code.

## A. Input data

The input data to our analysis are a sequence of 1800second short SFTs which we view as a matrix $\left\|z_{t, f}\right\|$. Here $t$ is the GPS time of the start of a short Fourier transform, while $f$ denotes the frequency bin in units of $1 / 1800 \mathrm{~Hz}$. The SFTs are produced from the calibrated gravitational strain channel $h(t)$ sampled at 16384 Hz .

This data are subjected to noise decomposition $[1,15]$ to determine the noise levels in individual SFTs and identify sharp instrumental lines. The noise level $n_{t}$ assigned to each SFT is used to compute SFT weight as inverse square $1 / n_{t}^{2}$.

Individual SFTs with high noise levels or large spikes in the underlying data are then removed from the analysis. For a typical well-behaved frequency band, we can exclude $8 \%$ of the SFTs while losing only $4 \%$ of accumulated weight. For a band with large detector artifacts (such as instrumental lines arising from resonant vibration of mirror suspension wires), however, we can end up removing most, if not all, SFTs. As such bands are not expected to have any sensitivity of physical interest they were excluded from the upper limit analysis (Table I).

TABLE I. Frequency regions excluded from upper limit analysis. These are separated into power line harmonics, harmonics of "violin modes" (resonant vibrations of the wires which suspend the many mirrors of the interferometer), and a number of individual bands.

| Category | Description |
| :--- | :---: |
| 60 Hz harmonics | Anything within 1.25 Hz of a |
| multiple of 60 Hz |  |
| First harmonic of |  |
| violin modes |  |
| Second harmonic of <br> violin modes | From 323 to 357 Hz |
| Other low frequency | From 685 to 697 Hz |
|  |  |
|  | 0.25 Hz bands starting at $50.5,51$, |
|  | $52,54,54.25,55,57,58,58.5$, |
|  | $58.75,63,65,66,69,72,78.5$, |
|  | $79.75,80.75 \mathrm{~Hz}$ |
| Other high frequency | 0.25 Hz bands starting at 105.25, |
|  | $106,119.25,121,121.5,135.75$, |
|  | $237.75,238.25,238.5,241.5$, |
|  | 362 Hz |

## B. PowerFlux weighted sum

PowerFlux detects signals by summing power in individual SFTs weighted according to the noise levels of the individual SFTs and the time-dependent amplitude responses:

$$
\begin{equation*}
P\left[f_{t}, a_{t}\right]=\frac{\sum_{t \in \mathrm{SFTs}}\left|z_{t, f_{t}}\right|^{2}\left|a_{t}\right|^{2} / n_{t}^{4}}{\sum_{t \in \mathrm{SFTs}}\left|a_{t}\right|^{4} / n_{t}^{4}} . \tag{3}
\end{equation*}
$$

Here we use $a_{t}$ for the series of amplitude response coefficients for a particular polarization and direction on the sky, $f_{t}$ denotes the series of frequency bin shifts due to Doppler effect and spin-down, and $\left|z_{t, f_{t}}\right|^{2}$ is the power in bin $f_{t}$ from the SFT acquired at time $t$. The values $n_{t}$ describe levels of noise in individual SFTs and do not depend on sky location or polarization.

The frequency shifts $f_{t}$ are computed according to the formula

$$
\begin{equation*}
f_{t}=f_{\text {source }}+f^{(1)}\left(t-t_{\text {ref }}\right)+f_{\text {source }} \frac{\vec{e} \cdot \vec{v}_{t}}{c}+\delta f \tag{4}
\end{equation*}
$$

where $f^{(1)}$ is the spin-down, $f_{\text {source }}$ is the source frequency, $\vec{e}$ is the unit vector pointing toward the sky location of interest, and $\vec{v}_{t}$ is the precomputed detector velocity at time $t$. The offset $\delta f$ is used to sample frequencies with resolution below the resolution of a single SFT. This approximate form separating contributions from Doppler shift and spin-down ignores negligible second order terms.

For each sky location, spin-down, and polarization, we compute the statistic $P\left[f_{t}+k \Delta f, a_{t}\right]$ at 501 frequencies separated by the SFT bin size $\Delta f=1 / 1800 \mathrm{~Hz}$. The

TABLE II. Detection pipeline parameters.

| Parameter | $50-100 \mathrm{~Hz}$ | $100-400 \mathrm{~Hz}$ | $400-800 \mathrm{~Hz}$ |
| :--- | :---: | :---: | :---: |
| Main run |  |  |  |
| Frequency zoom factor | 2 | 2 | 2 |
| Sky map zoom factor | 1 | 1 | 1 |
| Spin-down step (Hz/s) | $3 \times 10^{-11}$ | $3 \times 10^{-11}$ | $3 \times 10^{-11}$ |
| First coincidence step |  |  |  |
| Maximum frequency mismatch (mHz) | 2 | 1 | 1 |
| Maximum ecliptic distance (radians) | 0.25 | 0.06 | 0.03 |
| Maximum spin-down mismatch (Hz/s) | $6 \times 10^{-11}$ | $2 \times 10^{-11}$ | $2 \times 10^{-11}$ |
| Minimum multi-interferometer SNR | 7 | 7 | 7 |
| Minimum single-interferometer SNR | 5 | 5 | 5 |
| Loosely coherent follow-up |  |  |  |
| Phase mismatch (radians) | $\pi / 2$ | $\pi / 2$ | $\pi / 2$ |
| Follow-up disk radius (radians) | $0 \times 10^{-11}$ | $2 \times 10^{-11}$ | $2 \times 10^{-11}$ |
| Follow-up spin-down mismatch (Hz/s) | 8 | 8 | 8 |
| Frequency zoom factor | 4 | 4 | 4 |
| Sky map zoom factor | $5 \times 10^{-12}$ | $5 \times 10^{-12}$ | $5 \times 10^{-12}$ |
| Spin-down step (Hz/s) |  |  |  |
| Second coincidence step | 5 | 1 | 1 |
| Maximum frequency mismatch (mHz) | 20 | 20 | 20 |
| Minimum increase in multi-interferometer SNR (\%) | 20 | 20 | 20 |
| Minimum single-interferometer SNR (\%) |  |  | 0.03 |
| Loosely coherent follow-up with coherent combination of data between interferometers |  |  |  |
| Phases sampled | 16 | 16 | 16 |
| Maximum frequency mismatch (mHz) | 5 | 1 | 1 |
| Minimum increase in multi-interferometer SNR (\%) | 7 | 7 | 7 |

historical reason for using this particular number of frequency bins is that it is large enough to yield reliable statistics while small enough that a large fraction of frequency bands avoids the frequency comb of 1 Hz harmonics that emerge in a long integration of the S4 data and arise from the data acquisition and control electronics. The relatively large stepping in frequency makes the statistical distribution of the entire set stable against changes in sky location and offsets in frequency. To obtain sub-bin resolution the initial frequency $f_{t}$ can be additionally shifted by a fraction of the SFT frequency bin. The number of sub-bin steps-"frequency zoom factor"-is documented in Table II.

Except at very low frequencies (which are best analyzed using methods that take phase into account), the amplitude modulation coefficients respond much more slowly to change in sky location than do frequency shifts. Thus the spacing of sky and spin-down templates is determined from the behavior of the series $f_{t}$. The spin-down spacing depends on the inverse of the time base spanned by the entire SFT set. The sky template spacing depends on the Doppler shift, which has two main components: the Earth's rotation, which contributes a component on the order of $1 \times 10^{-6} f_{\text {source }}$ with a period of one sidereal day, and the Earth's orbital velocity, which contributes a larger component of $1 \times 10^{-4} f_{\text {source }}$ but with a longer annual period.

If not for the Earth's rotation, all the evolution components would have evolved slowly compared to the length of the analysis and the computation could proceed by subdividing the entire data set into shorter pieces which could be sampled on a coarser grid and then combined using finer steps. We can achieve a very similar result by grouping SFTs within each piece by (sidereal) time of day, which has the effect of freezing the Earth's rotation within each group.

A further speed up can be obtained by reduction in template density, which is allowed by degeneracy between contributions from spin-down mismatch and orbital velocity shift arising from mismatch in sky location.

## C. Partial power sum cache

The optimizations just described can all be made simultaneously by implementing an associative cache of previously computed power sums. This approach also has the advantage of being able to accommodate new frequency evolution models (such as emission from a binary system) with few modifications.

The cache is constructed as follows. First, we subdivide the sky into patches small enough that amplitude response coefficients can be assumed constant on each patch. Each set of templates from a single patch is
computed independently using amplitude response coefficients from a representative template of its patch.

Second, we separate the weighted power sum into the numerator and denominator sums:

$$
\begin{gather*}
P S\left[f_{t}, b_{t}\right]=\sum_{t \in \mathrm{SFTs}} \frac{b_{t}}{n_{t}^{4}}\left|z_{t, f_{t}}\right|^{2},  \tag{5}\\
W S\left[c_{t}\right]=\sum_{t \in \mathrm{SFTs}} \frac{c_{t}}{n_{t}^{4}} \tag{6}
\end{gather*}
$$

where values for a fixed set of amplitude response coefficients $b_{t}$ and $c_{t}$ (discussed in the next section) are stored in the partial power sum cache with the frequency shift series $f_{t}$ used as a key. The fact that both sums are additive functions of the set of SFTs for which they are computed allows partial power sums to be broken into several components and then recombined later.

## D. Polarization decomposition

While it is efficient to compute the partial power sums for a small number of polarizations, one can also decompose the coefficients $b_{t}$ and $c_{t}$ into products of detector-specific time-dependent parts and static coefficients that depend on polarization alone. This analysis extends [17,18].

First, we introduce quadratic and quartic detector response series,

$$
\begin{align*}
& F_{t}^{2, i}=\left(F_{t}^{+}\right)^{2-i}\left(F_{t}^{\times}\right)^{i},  \tag{7}\\
& F_{t}^{4, i}=\left(F_{t}^{+}\right)^{4-i}\left(F_{t}^{\times}\right)^{i} \tag{8}
\end{align*}
$$

(with $i=0-2$ and $i=0-4$, respectively), and the corresponding sets of polarization response coefficients:

$$
\begin{align*}
A^{2,0}(\iota, \psi)= & \frac{1}{8}\left(1+\cos ^{2}(\iota)\right)^{2}(1+\cos (4 \psi)) \\
& +\frac{1}{4} \cos ^{2}(\iota)(1-\cos (4 \psi)) \\
A^{2,1}(\iota, \psi)= & \left(\frac{1}{4}\left(1+\cos ^{2}(\iota)\right)^{2}-\frac{1}{2} \cos ^{2}(\iota)\right) \sin (4 \psi), \\
A^{2,2}(\iota, \psi)= & \frac{1}{8}\left(1+\cos ^{2}(\iota)\right)^{2}(1-\cos (4 \psi)) \\
& +\frac{1}{4} \cos ^{2}(\iota)(1+\cos (4 \psi))  \tag{9}\\
A^{4,0}= & A^{2,0} A^{2,0}, \quad A^{4,1}=2 A^{2,0} A^{2,1} \\
A^{4,2}= & 2 A^{2,0} A^{2,2}+A^{2,1} A^{2,1} \\
A^{4,3}= & 2 A^{2,2} A^{2,1}, \quad A^{4,4}=A^{2,2} A^{2,2} \tag{10}
\end{align*}
$$

Here $\iota$ and $\psi$ are the usual [19] inclination and orientation parameters of the source.

The amplitude response coefficients can be represented as

$$
\begin{align*}
& b_{t}(\iota, \psi)=\sum_{i=0}^{2} F_{t}^{2, i} A^{2, i}(\iota, \psi)  \tag{11}\\
& c_{t}(\iota, \psi)=\sum_{i=0}^{4} F_{t}^{4, i} A^{4, i}(\iota, \psi)
\end{align*}
$$

and given previously computed partial power sums, we compute the weighted power sum for an arbitrary polarization as

$$
\begin{equation*}
P\left[f_{t}, \iota, \psi\right]=\frac{\sum_{i=0}^{2} P S\left[f_{t}, F_{t}^{2, i}\right] A^{2, i}(\iota, \psi)}{\sum_{i=0}^{4} W S\left[f_{t}, F_{t}^{4, i}\right] A^{4, i}(\iota, \psi)} \tag{12}
\end{equation*}
$$

In this approach we use Eqs. (5) and (6) to compute power sums for a nonphysical but computationally convenient set of polarizations that can be combined into physical power sums in the end.

## E. SFT set partitioning

The PowerFlux weighted power sum is additive with respect to the set of SFTs it is computed with. This can be used to improve the efficiency of the cache engine, which will have a higher hit ratio for more tightly grouped SFTs. This needs to be balanced against the larger overhead from accumulating individual groups into the final weighted power sum. In addition, larger groupings could be used to analyze subsegments of the entire run, with the aim of detecting signals that were present only during a portion of the 2 years of data.

In this analysis, we have used the following summing plan: First, for each individual detector the SFT set is broken down into equally spaced chunks in time. Five chunks per detector were used in the analysis of the lowfrequency range of $50-400 \mathrm{~Hz}$, for which detector nonstationarity was more pronounced. Three chunks per detector were used for analysis of the $375-800 \mathrm{~Hz}$ range.

The partial power sums for each chunk are computed in steps of 10 days each, which are also broken down into 12 groups by the magnitude of their frequency shifts.

The individual groups have their frequency shift series rounded to the nearest integer frequency bin, and the result is passed to the associative cache.

## F. Computation of upper limits, outliers, and other statistics

Having computed partial power sums for individual chunks, we combine them into contiguous sequences, both separately by detector and as a whole, to form weighted power sums. These sums are used to establish upper limits based on the Feldman-Cousins [20] statistic, to obtain the signal-to-noise ratios and auxiliary statistics used for detector characterization and to assess the Gaussianity of underlying data.

An important caveat is that the sensitivity of the detectors improved considerably toward the end of the data
taking run, especially at low frequencies. As the SFT weight veto described earlier is performed for the entire data set, it can remove a considerable fraction of data from the first few chunks. Thus at frequencies below 400 Hz , the upper limit chosen for each frequency bin is the value obtained from analyzing the entire run, the last $4 / 5$ of the run, or the last $3 / 5$ of the run, whichever value is lowest. At frequencies above 400 Hz we use the value obtained from the entire run or the last $2 / 3$ of the run, whichever value is lowest.

The detection search was performed on outliers from any contiguous combination of the chunks, but we have not run tests to estimate pipeline efficiency on smaller subsets.

## G. Injections and validation

The analysis presented here has undergone extensive checking, including independent internal review of the code and numerous Monte Carlo injection runs. We present a small portion of this work to assure the reader that the pipeline works as described.

One of the most basic tests is correct reconstruction of hardware and software signal injections. Figure 3 shows a skymap of the signal-to-noise ratio on the sky for a sample injection, for which the maximum is found at a grid point near the injection location. As the computation of weighted sums is a fairly simple algebraic transformation, one can infer the essential correctness of the code in the general case from the correctness of the skymaps for several injections.

A Monte Carlo injection run also provides a test of realistically distributed software paths, validation of upper limits, and characterization of parameter reconstruction.

In a particular injection run we are concerned with three main issues:
(i) The upper limits established by the search should be above injected values. Figure 4 shows results of such a simulation at 400 Hz , confirming the validity of the search.
(ii) We need to determine the maximum mismatches in signal parameters the search can tolerate while still producing correct upper limits and recovering


FIG. 3 (color online). SNR skymap for hardware injection of a simulated signal. The circle is centered on the location of the injection. The high frequency of the signal ( 575 Hz ) allows good localization.


FIG. 4 (color online). Upper limit validation. Each point represents a separate injection. Established upper limit ( $y$ axis) is compared against injected strain value ( $x$ axis, red line).
injections. Figures 5-7 show results of such analysis in the 400 Hz band. The signal localization is within the bounds used by the follow-up procedure (discussed in Sec. V).


FIG. 5 (color online). Improvement of spin-down localization of injected test signals. The injected strain divided by the upper limit in this band (before injection) is shown on the $x$ axis. The difference between injection spin-down and spin-down of corresponding outlier is shown on the $y$ axis. Crosses, semicoherent; circles, loosely coherent.


FIG. 6 (color online). Improvement of position localization of injected test signals. The injected strain divided by the upper limit in this band (before injection) is shown on the $x$ axis. The distance between injection sky location and that of corresponding outlier is shown on the $y$ axis. Crosses, semicoherent; circles, loosely coherent.


FIG. 7 (color online). Improvement of frequency localization of injected test signals. The injected strain divided by the upper limit in this band (before injection) is shown on the $x$ axis. The difference between injection frequency and frequency of corresponding outlier is shown on the $y$ axis. Crosses, semicoherent; circles, loosely coherent.


FIG. 8 (color online). Injection recovery from semicoherent analysis stage (crosses), after the first loosely coherent follow-up (circles) and after the second stage of loosely coherent follow-up (diagonal crosses). The injected strain divided by the upper limit in this band (before injection) is shown on the $x$ axis. The percentage of surviving injections is shown on the $y$ axis.
(iii) The efficiency ratio of injection recovery should be high. As seen in Fig. 8 our recovery ratio for a semicoherent search is nearly $100 \%$ for injections at the upper limit level.

## V. LOOSELY COHERENT CODE AND DETECTION PIPELINE

The reduced sensitivity of a semicoherent method like PowerFlux relative to a fully coherent search comes with robustness to variation in phase of the input signal, be it from small perturbations of the source due to a companion or from imperfections in the detector.

One way to achieve higher sensitivity while preserving robustness to variations in the phase of the input signal is to use a loosely coherent search code that is sensitive to families of signals following a specific phase evolution pattern, while allowing for fairly large deviations from it. We have extended PowerFlux with a program that computes a loosely coherent power sum. The results of simulations of this program on Gaussian noise were first presented in [12].

Searches for continuous-wave signals have typically been performed using combinations of coherent and semicoherent methods. A coherent method requires a precise phase match between the signal and a model template over the entire duration of the signal, and thus requires a close
match between the signal and model parameters: each model template covers only a small region of the signal space. A semicoherent method requires phase matching over short segments of the data and discards phase information between segments, and each template therefore covers a larger region of the signal space. We use the term loosely coherent to describe a broader class of algorithms whose templates cover some arbitrarily specified region of the signal space, with sensitivity falling off outside of the template boundaries.

One way to implement a loosely coherent search is by requiring the signal to match a phase model very closely over a narrow time window, but then smoothly downgrading the phase-match requirement over longer time spans by means of a weighting kernel. The mathematical expression of this is given in Eq. (13), below. The allowable phase drift, expressed as radians per unit time, is a tunable parameter of the search. Larger allowed phase drifts result in templates that cover a larger region of the signal space, but with less power to discriminate true signals from noise.

The variant of the loosely coherent statistic used in this paper is derived from the PowerFlux code base and is meant for analysis with wide phase evolution tolerance. It is not the most computationally efficient, but has wellunderstood robustness properties and suffices for follow-up of small sky areas. A dedicated program for future searches is under development. The technical description of the present implementation can be found in [16].

## A. Loosely coherent weighted sum

The loosely coherent statistic is based on the same power sum computation used in the PowerFlux computing infrastructure, but instead of a single sum over SFTs, we have a double sum:

$$
\begin{align*}
& P\left[f_{t}, \phi_{t}, a_{t}, f_{t^{\prime}}, \phi_{t^{\prime}} a_{t}^{\prime}, \delta\right] \\
& \quad=\frac{\sum_{t, t^{\prime} \in \mathrm{SFTs}} e^{i \phi_{t^{\prime}}-i \phi_{t}} K_{\delta}\left(\left|t-t^{\prime}\right|\right) \bar{z}_{t^{\prime}, f_{t^{\prime}} z_{t, f_{t}} \bar{a}_{t} a_{t^{\prime}} / n_{t}^{2} n_{t^{\prime}}^{2}}^{\sum_{t, t^{\prime} \in \mathrm{SFTs}} K_{\delta}\left(\left|t-t^{\prime}\right|\right)\left|a_{t}\right|^{2}\left|a_{t^{\prime}}\right|^{2} / n_{t}^{2} n_{t^{\prime}}^{2}} .}{} . \tag{13}
\end{align*}
$$

Here $\phi_{t}$ is the series of phase corrections needed to transition the data into the solar system barycenter frame of reference and to account for source evolution between times $t$ and $t^{\prime}$.

The formula (13) is generic for any second order statistic, a nice description is presented in [21] as a generalization of cross correlation.

In order to make a statistic (13) loosely coherent we need to make sure that it admits signals with phase deviation up to a required tolerance level and rejects signals outside of that tolerance. We achieve this by selecting a low-pass filter for the kernel $K_{\delta}\left(\left|t-t^{\prime}\right|\right)$. A
$\operatorname{sinc}=\frac{\sin (x)}{x}$ based filter provides the steepest rejection of signals with large phase deviation, but is computationally expensive. Instead, we use the Lanczos kernel with parameter 3:

$$
\tilde{K}_{\delta}(\Delta t)= \begin{cases}\operatorname{sinc}\left(\frac{\delta \Delta t}{0.5 \mathrm{hr}}\right) \operatorname{sinc}\left(\frac{\delta \Delta t}{1.5 \mathrm{hr}}\right) & \text { when } \frac{\delta \Delta t}{0.5 \mathrm{hr}}<3 \pi  \tag{14}\\ 0.0 & \text { otherwise }\end{cases}
$$

The choice of low-pass filter implies that the terms with $t=t^{\prime}$ are always included.

The parameter $\delta$ determines the amount of accumulated phase mismatch that is permitted over 30 minutes. For large values of $\delta$ the search is more tolerant to phase mismatch and closer in character to PowerFlux power sums. For smaller values the effective coherence length is longer, requiring finer template spacing and yielding higher signal-to-noise ratios.

## B. Partial power sum cache

The partial power cache is constructed similarly to the PowerFlux case. Instead of a single series of frequency shifts $f_{t}$ the partial power sums depend on both $f_{t}$ and $f_{t^{\prime}}$. The additional key component consists of a series of differential Doppler shifts, from the derivative of Doppler shift with respect to frequency, since a small change in frequency has a large effect on phases $\phi_{t}$ and $\phi_{t^{\prime}}$.

For the value of $\delta=\pi / 2$ used in this analysis the cross terms $\left(t \neq t^{\prime}\right)$ are often zero as the Lanczos kernel vanishes for widely separated SFTs. The SFT partitioning scheme takes advantage of this by forming smaller groups and only computing cross terms between groups that are close enough to produce nonzero results.

## C. Polarization decomposition

The polarization decomposition for the loosely coherent search is similar to that used by PowerFlux. The two changes required are the treatments of coefficients involving both cross and plus detector response terms and imaginary terms [16].

The implementation used in this search is obtained by the mathematical method of polarization ${ }^{1}$ of homogeneous polynomials of Eqs. (7) and (8):

$$
\begin{align*}
& F^{2,0}\left(t, t^{\prime}\right)=F_{t}^{+} F_{t^{\prime}}^{+}, \\
& F^{2,1}\left(t, t^{\prime}\right)=\frac{1}{2}\left(F_{t}^{+} F_{t^{\prime}}^{\times}+F_{t}^{\times} F_{t^{\prime}}^{+}\right),  \tag{15}\\
& F^{2,2}\left(t, t^{\prime}\right)=F_{t}^{\times} F_{t^{\prime}}^{\times},
\end{align*}
$$

[^0]\[

$$
\begin{align*}
& F^{4,0}=F^{2,0} F^{2,0}, \quad F^{4,1}=F^{2,0} F^{2,1}, \\
& F^{4,2}=\frac{1}{3} F^{2,0} F^{2,2}+\frac{2}{3} F^{2,1} F^{2,1}, \\
& F^{4,3}=F^{2,2} F^{2,1}, \quad F^{4,4}=F^{2,2} F^{2,2} . \tag{16}
\end{align*}
$$
\]

Equations (7) and (8) are obtained by setting $t^{\prime}=t$. This allows us to compute the real part of the product $\bar{a}_{t^{\prime}} a_{t}$ using the same polarization coefficients $A^{2, i}$ and $A^{4, i}$ as used by the PowerFlux search:

$$
\begin{equation*}
\operatorname{Re}\left(\bar{a}_{t^{\prime}} a_{t}\right)=\sum_{i=0}^{2} F^{2, i} A^{2, i} \tag{17}
\end{equation*}
$$

The imaginary part is equal to

$$
\begin{equation*}
\operatorname{Im}\left(\bar{a}_{t^{\prime}} a_{t}\right)=\frac{1}{8}\left(F_{t}^{+} F_{t^{\prime}}^{\times}-F_{t}^{\times} F_{t^{\prime}}^{+}\right)\left(1+\cos ^{2} \iota\right) \cos \iota \tag{18}
\end{equation*}
$$

and is neglected in the analysis. This approximation is justified for several reasons. First, the difference $F_{t}^{+} F_{t^{\prime}}^{\times}-$ $F_{t}^{\times} F_{t^{\prime}}^{+}$is small relative to other terms for closely spaced $t$ and $t^{\prime}$. Second, the part depending on $\cos (\iota)$ is large for polarizations close to circular, to which we are more sensitive anyway. The simulations have shown that discarding this term reduces the SNR by about $4 \%$ for circular polarizations.

## D. Follow-up procedure

The detection pipeline consists of three stages. The first stage is a regular PowerFlux run that produces lists of outliers with single-interferometer SNR of 5 or greater.

The outliers are subjected to a coincidence test (parameters shown in Table II), where the outliers from the multiinterferometer data with SNR of at least 7 are compared against nearby single-interferometer outliers. Frequency consistency provides the tightest constraint, with sky position and spin-down helping to eliminate loud instrumental artifacts. As the ability to localize signals depends largely on Doppler shifts from Earth orbital motion, we project outlier locations onto the ecliptic plane to compute "ecliptic distance" for a sky coincidence test. A number of 0.1 Hz regions (see Table III) had so many coincidences (due to highly disturbed local spectra) that they had to be excluded from the analysis.

The outliers at nearby frequencies and sky locations are grouped together, and only the loudest is passed to the next stage of follow-up.

During the second stage the resulting outliers are analyzed using the loosely coherent code with phase mismatch parameter $\delta=\pi / 2$, while combining data from different interferometers incoherently. The sky resolution is made finer ("zoomed") by a factor of 4 . The incoherent combination provides SNR data both for individual interferometers, as well as for their combination, while being faster to compute due to fewer terms in the double sum in Eq. (13).

The outliers in SNR passing the loosely coherent analysis are required to show at least a $20 \%$ increase in

TABLE III. Frequency regions excluded from the coincidence test because of severe noise contamination leading to numerous outliers inconsistent with a true signal.

| Center <br> frequency (Hz) | Width (Hz) | Description |
| :--- | :---: | :---: |
| 63 | 0.1 | Pulsed heating |
| 64 | 0.1 | 16 Hz harmonic from data |
|  |  | acquisition system |
| 66 | 0.1 | Pulsed heating |
| 67 | 0.1 | Unidentified strong line in L1 |
| 69 | 0.1 | Pulsed heating |
| 75 | 0.1 | Unidentified strong line in L1 |
| 96 | 0.1 | 16 Hz harmonic from data |
|  |  | acquisition system |
| 100 | 0.1 | Unidentified strong line in H1 |

multi-interferometer SNR while not shifting appreciably in frequency. The required SNR increase from the semicoherent to the loosely coherent stage is quite conservative, as can be seen in Fig. 9. In addition, we apply a minimum SNR cut: the SNR of each individual interferometer should be at least $20 \%$ of the multi-interferometer SNR. This condition is essential to eliminating coincidences from loud instrumental lines in only one interferometer.

In the third stage of follow-up the remaining outliers are reanalyzed with the loosely coherent pipeline, which now coherently combines data from both interferometers.


FIG. 9 (color online). Relative increase in SNR of injected test signals from semicoherent to loosely coherent stage. The plot is restricted to injections that passed the coincidence test. The injected strain divided by the upper limit in this band (before injection) is shown on the $x$ axis. The ratio of loosely coherent SNR to semicoherent SNR is shown on the $y$ axis.


FIG. 10 (color online). Relative increase in SNR from coherent combination of data from different interferometers. The plot is restricted to injections that passed the coincidence test. The injected strain divided by the upper limit in this band (before injection) is shown on the $x$ axis. The ratio of coherently combined loosely coherent SNR to loosely coherent SNR from the previous stage is shown on the $y$ axis.

To eliminate the possibility of a relative global phase offset we sampled 16 possible phase offsets between interferometers. This step is merely a precaution that was easy to implement-we did not expect to see a significant offset, as the relative interferometer timing was determined to be within $10 \mu s$ [13,14].

Each outlier was then required to show the expected increase in SNR of at least 7\% over the value from the second stage of follow-up, while maintaining the same frequency tolerance. The improvement in signal-to-noise ratio seen in simulations is shown in Fig. 10. Most injections have greater than $10 \%$ increase in SNR, leaving room for possible mismatch in phase of up to $\pi / 16$.

## E. Performance of the detection pipeline

Every detection pipeline can be described by two figures of merit-false alarm ratio and recovery ratio of true signals.

Since our analysis is computationally limited, we can use a more sensitive code to confirm or reject outliers. Thus, our main objective in optimizing each pipeline stage was to have as high a recovery ratio as possible, while generating a small enough false alarm ratio to make the subsequent step computationally feasible.

The recovery ratios found in a Monte Carlo simulation of first, second, and third follow-up stages are shown in

Fig. 8. The graph shows that the loosely coherent stages have less than a $5 \%$ loss ratio of injections, and the overall pipeline performance approaches $100 \%$ right at the upper limit threshold.

While it is possible to compute the false alarm ratio for Gaussian noise, this number is not very informative, since most outliers are the result of instrumental artifacts, as discussed in Sec. VI.

## F. Injections and validation

The loosely coherent search code has undergone the same extensive review as the regular semicoherent PowerFlux discussed earlier. In addition to strain reconstruction tests, mismatch determination, and injection recovery, we verified that the passing of reconstructed injections to the next stage of the detection pipeline does not undermine detection efficiency.

The results of such analysis in a narrow band near 400 Hz can be seen in Fig. 8. The injection recovery ratio after the first semicoherent pass is shown with a " + " symbol. The circles show the recovery ratio after the first loosely coherent pass, while the crosses " $\times$ " show recovery after the second loosely coherent stage. The improvement in parameter determination is shown in Figs. 5-7.

We have also run a simulation to determine whether the loosely coherent follow-up preserves the robustness to deviations from the ideal signal model that we obtain with a regular semicoherent code. Figure 11 shows the


FIG. 11 (color online). Upper limit reconstruction versus depth of periodic frequency modulation for semicoherent search. The frequency modulation depth is shown on the $x$ axis. The red line marks the $280 \mu \mathrm{~Hz}$ boundary to the right of which we expect injections to start losing power. The $y$ axis shows the ratio between the upper limit and injected strain.


FIG. 12 (color online). Upper limit reconstruction versus depth of periodic frequency modulation for loosely coherent search with parameter $\delta=\pi / 2$. The frequency modulation depth is shown on the $x$ axis. The red line marks the $70 \mu \mathrm{~Hz}$ boundary to the right of which we expect injections to start losing power. The $y$ axis shows the ratio between the upper limit and injected strain.
results of a simulation where we applied an additional sinusoidal frequency modulation to the signal. We considered frequency modulations with periods above 2 months. Figure 12 shows results for the loosely coherent pipeline. The red line marks the amplitude of frequency modulation where we had predicted we would start to see significant signal loss, based on rough estimates of how much power is expected to "leak" into adjacent frequency bins. For the semicoherent search the tolerance is $280 \mu \mathrm{~Hz}$, while for the loosely coherent search it is $70 \mu \mathrm{~Hz}$.

## VI. RESULTS

PowerFlux produces 95\% confidence level upper limits for individual templates, where each template represents a particular value of frequency, spin-down, sky location, and polarization. The results are maximized over several parameters, and a correction factor is applied to account for possible mismatches of real signal with sampled parameters. Figure 1 shows the resulting upper limits maximized over the analyzed spin-down range, over the sky and, for the upper set of curves, over all sampled polarizations. The lower set of curves shows the upper limit for circular polarization alone. The uncertainty of these values is below $15 \%$ [14], dominated by systematic and statistical calibration errors. The numerical data for this plot can be obtained separately [22].

The solid blue points denote values for which we found evidence of non-Gaussian behavior in the underlying data. For these, we do not claim a specific confidence bound. The regions near harmonics of the 60 Hz power line frequency are shown as circles. In addition, a small portion of the sky near each ecliptic pole has been excluded from the search, as these regions are susceptible to contamination from stationary instrumental spectral lines. The excluded portion consists of sky templates where frequency shifts due to Doppler modulation and spin-down are close to each other for a significant fraction of input data [2]. This is similar to the $S$ parameter veto described in [1], but takes into account varying noise level in input SFTs. The fraction of excluded sky starts as about $1 \%$ at 50 Hz and decreases at $f^{-2.15}$ with deviations due to wideband instrumental artifacts.

Figure 13 provides an easy way to judge the astrophysical range of the search. We have computed the implied spin-down solely due to gravitational emission at various distances, as well as corresponding ellipticity curves. This follows formulas in paper [1]. For example, at the highest frequency sampled, assuming ellipticity of $3.3 \times 10^{-6}$ (which is well under the maximum limit in [23]), we can see as far as 425 parsecs.

In each search band, including regions with detector artifacts and without restrictions on sky position, the


FIG. 13 (color online). Range of the PowerFlux search for neutron stars spinning down solely due to gravitational radiation. This is a superposition of two contour plots. The green solid lines are contours of the maximum distance at which a neutron star could be detected as a function of gravitational-wave frequency $f$ and its derivative $\dot{f}$. The dashed lines are contours of the corresponding ellipticity $\epsilon(f, \dot{f})$. The fine dotted line marks the maximum spin-down searched. Together these quantities tell us the maximum range of the search in terms of various populations (see text for details).

TABLE IV. Outliers that passed the detection pipeline. Only the highest-SNR outlier is shown for each hardware injection and 60 Hz harmonic.

| Frequency (Hz) | Spin-down (Hz/s) | RA (J2000) (degrees) | $\begin{gathered} \text { DEC (J2000) } \\ \text { (degrees) } \end{gathered}$ | Description |
| :---: | :---: | :---: | :---: | :---: |
| 63.391111 | $-9.15 \times 10^{-10}$ | 53.96 | 20.60 | Electromagnetic interference in L1 |
| 70.883403 | $-9.10 \times 10^{-10}$ | 34.99 | -13.06 | Line in L1 from controls/data acquisition system |
| 70.884306 | $-7.65 \times 10^{-10}$ | 22.46 | -9.55 | Line in L1 from controls/data acquisition system |
| 80.006389 | $-2.80 \times 10^{-10}$ | 247.89 | -19.86 | 16 Hz harmonic from data acquisition system |
| 97.772778 | $-1.85 \times 10^{-09}$ | 59.39 | 1.12 | Line in L1 from controls/data acquisition system |
| 97.787569 | $-2.25 \times 10^{-10}$ | 355.08 | -1.94 | Line in L1 from controls/data acquisition system |
| 108.857569 | $-2.00 \times 10^{-11}$ | 177.90 | -32.84 | Hardware injection of simulated signal (ip3) |
| 128.057083 | $-1.81 \times 10^{-09}$ | 229.39 | 15.47 | 16 Hz harmonic from data acquisition system |
| 180.178056 | $-2.68 \times 10^{-09}$ | 319.38 | 29.16 | 60 Hz harmonic |
| 193.323333 | $-2.08 \times 10^{-09}$ | 345.78 | -27.19 | Hardware injection of simulated signal (ip8) |
| 566.049375 | $1.50 \times 10^{-11}$ | 81.27 | 42.29 | Suspension wire resonance in H1 |
| 568.077708 | $-1.84 \times 10^{-09}$ | 283.47 | -61.01 | Suspension wire resonance in H1 |
| 575.163542 | 0 | 215.24 | 3.47 | Hardware injection of simulated signal (ip2) |

TABLE V. Parameters of hardware-injected simulated signals detected by PowerFlux (epoch GPS 846885755).

| Name | Frequency (Hz) | Spin-down (Hz/s) | RA (J2000) (degrees) | DEC (J2000) (degrees) |
| :--- | :---: | :---: | :---: | :---: |
| ip2 | 575.16356 | $-1.37 \times 10^{-13}$ | 215.26 | 3.44 |
| ip3 | 108.85716 | $-1.46 \times 10^{-17}$ | 178.37 | -33.44 |
| ip8 | 193.48479 | $-8.65 \times 10^{-09}$ | 351.39 | -33.42 |

follow-up pipeline described in Sec. V was applied to outliers satisfying the initial coincidence criteria. The statistics are as follows: the second stage received 9855 outliers, out of which only 619 survived to the third stage of follow-up, which reduced them to 47 outliers. They are summarized in Table IV which lists only one outlier for each frequency of interest. The frequency is specified relative to GPS time 846885755, which corresponds to the middle of the S 5 run.

Most of the 47 remaining outliers are caused by three simulated pulsar signals injected into the instrument as test signals. Their parameters are shown in Table V. The signal ip8 lay outside the sampled spin-down range, but was loud enough to generate an outlier at an offset from the true location and frequency. The spin-down values of ip2 and ip3 are very close to 0 and were detected in the first few templates.

Several techniques were used to identify outlier causes. During S5 there was a general effort to identify problematic areas of frequency space and instrumental sources of the contamination. Noise lines were identified by previously performed searches $[2,11,24]$ as well as the search described in this paper. In addition, a dedicated analysis code "FScan" [25] was created specifically for identification of instrumental artifacts. Problematic noise lines were recorded, and monitored throughout S5. Another technique
used was the calculation of the coherence between the interferometers' output channel and physical environment monitoring channels. In S5 the coherence was calculated as monthly averages; the coherence output was then mined for statistically significant peaks.

In addition to data analysis techniques, investigations in the laboratory at the observatories provided further evidence as to the origin of noise lines. Portable magnetometers were used to find electrical sources of noise. Measurements of the noise coming from power supplies and cooling fans in electronics racks also helped to identify a number of noise lines.

The 47 remaining outliers were investigated and were all traced to known instrumental artifacts or hardware injections. Hence the search has not revealed a true continuous gravitational-wave signal.

## VII. CONCLUSIONS

We have performed the most sensitive all-sky search to date for continuous gravitational waves in the range $50-800 \mathrm{~Hz}$. At the highest frequencies we are sensitive to neutron stars with an equatorial ellipticity as small as $3.3 \times 10^{-6}$ as far away as 425 pc for unfavorable spin orientations. For favorable orientations (spin axis aligned with line of sight), we are sensitive to ellipticities as small
as $1.2 \times 10^{-6}$ for the same distance and frequencies. A detection pipeline based on a loosely coherent algorithm was applied to outliers from our search. This pipeline was demonstrated to be able to detect simulated signals at the upper limit level. However, no true pulsar signals were found.

The analysis of the next set of data produced by the LIGO and Virgo interferometers (science runs S6, VSR2, and VSR3) is under way. This science run has an improved strain sensitivity by a factor of 2 at high frequencies, but spans a shorter observation time than S 5 , and its data at lower frequencies are characterized by larger contaminations of non-Gaussian noise than for S5. Therefore, we do not expect to produce improved upper limits in the $100-300 \mathrm{~Hz}$ range without changes to the underlying algorithm until the Advanced LIGO and Advanced Virgo interferometers begin operation.

The improved sensitivity of the S 6 run coupled with its smaller data volume will make it easier to investigate higher frequencies and larger spin-down ranges, goals of the forthcoming S6 searches. We also look forward to results from the Virgo interferometer, in particular, in the frequency range below $\sim 40 \mathrm{~Hz}$ which so far has been inaccessible to LIGO interferometers.

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[^0]:    ${ }^{1}$ This has nothing to do with polarization of gravitational-wave signals, but refers to the fact that the map between symmetric multilinear forms $L(x, y, z, \ldots)$ with $k$ arguments and homogeneous polynomials $P$ of degree $k$ given by $P(x)=L(x, x, x, \ldots)$ is a bijection.

