

# **Global Sensitivity Analysis of Impedance Measurement Algorithms Implemented in Intelligent Electronic Devices**

by

**Nanang Rohadi**

Bachelor of Engineering,  
The University of Indonesia, Indonesia, 1998

Master of Engineering,  
Institute Technology of Bandung, Indonesia, 2005

Thesis is submitted for the degree of

**Doctor of Philosophy**

in

School of Electrical and Electronic Engineering  
Faculty of Engineering, Computer, and Mathematical Sciences  
The University of Adelaide, Australia

June 2013

©Copyright 2013

Nanang Rohadi

All Right Reserved



THE UNIVERSITY  
*of* ADELAIDE

# Abstract

A novel methodology for testing performance of impedance measurement algorithms used in transmission line protection schemes is developed. Nowadays, impedance measurement algorithms are software functions implemented in the multifunction Intelligence Electronic Devices (IEDs) responsible for overall monitoring, protection and control of transmission lines. Accurate impedance measurement during fault conditions is the key in successful performance of the line protection as well as fault location functions of an IED. This thesis investigates a typical practical situation where only short-term fault records of voltage and current measurements from one side of a transmission line are used as inputs in the impedance measurement algorithm. Current flowing into the fault from the remote terminal of transmission line as well as fault impedance can influence significantly accuracy of impedance measurement. Since these two quantities are not measured, we require a systematic tool which will assess sensitivity of impedance measurement to those factors. At present, these sensitivities are obtained in heuristic and ad hoc manner during application testing done by utilities before commissioning of new IEDs. Situation in practice can be increasingly complex and this kind of unsystematic testing approach can fail. The thesis addresses those practical complex cases in the systematic manner. In these cases we encounter the following configurations of transmission lines with new not measured factors:

- parallel closely spaced lines, where the effect of electromagnetic mutual coupling can be significant;
- series capacitive compensation of transmission line, where capacitance of the compensation device can be unknown;
- three-terminal lines, where measurements on the tapped line are not available.

The proposed systematic sensitivity testing tool comprises of a transmission line electromagnetic simulation module and a Global Sensitivity Analysis (GSA) module. The

software packages commonly used by industry are employed to implement those modules: the DIgSILENT software for the line simulation module and the SIMLAB software for the GSA module. The simulation module is used to simulate large number of fault scenarios for all samples in the factor space, while the GSA module is responsible for creating a set of specific samples in the factor space as well as for sensitivity analysis. The commercial multifunctional IED SEL-421 from the Schweitzer Engineering Laboratories has been used to demonstrate the proposed sensitivity analysis tool. The IED functions has been modelled in DIgSILENT environment and integrated into the simulation module. Test automation program has been written using the DIgSILENT Programming Language (DPL) so fully automatic and integrated performance of the simulation and the GSA modules has been achieved. The GSA module relies on the Quasi-Monte Carlo (QMC) technique with the Sobol's quasi random sampling and the Morris method is used in fast factor pre-screening in order to remove non-influential factors before applying the QMC GSA. The results of systematic tests of the impedance measurement algorithm implemented in the SEL-421 IED, for various line configuration cases, are presented in this thesis. The results verify the usefulness of the proposed testing methodology for practical applications.

# Statement of Originality

I certify that this work contains no material which has been accepted for the award of any other degree or diploma in my name, in any university or other tertiary institution and, to the best of my knowledge and belief, contains no material previously published or written by another person, except where due reference has been made in the text. In addition, I certify that no part of this work will, in the future, be used in a submission in my name, for any other degree or diploma in any university or other tertiary institution without the prior approval of the University of Adelaide and where applicable, any partner institution responsible for the joint-award of this degree.

I give consent to this copy of my thesis when deposited in the University Library, being made available for loan and photocopying, subject to the provisions of the Copyright Act 1968.

The author acknowledges that copyright of published works contained within this thesis resides with the copyright holder(s) of those works.

I also give permission for the digital version of my thesis to be made available on the web, via the University's digital research repository, the Library Search and also through web search engines, unless permission has been granted by the University to restrict access for a period of time.

Signed: .....

Date: .....

This page is blank

# Acknowledgements

This research has been carried out at the School of Electrical and Electronic Engineering, The University of Adelaide, South Australia.

I would like to express my gratitude and appreciation for Dr. Rastko Zivanovic for his supervision, encouragement, support, patience, and invaluable inputs for this research. His vision and guidance in the preparation of this thesis are gratefully acknowledged. I also wish to thank my advisory committee member, Assoc.Prof. Nesimi Ertugrul, for his suggestions and advice.

I greatly acknowledge the Directorate General of Higher Education (DIKTI), Department of National Education, for providing financial support during my studies. I also acknowledge the financial support, during the last year of this project, provided by Graduate Studies (Research Operations), and also the support from the State Polytechnique of Jakarta.

I would also like to thank Robert Moric, a Ph.D. candidate, at the School of Electrical and Electronic Engineering, University of Adelaide, for his help in editing this thesis. I also acknowledge the support provided by the IT staff, and also the staff of the School of Electrical and Electronic Engineering at the University of Adelaide.

I am also grateful for SIMLAB (2009) version 2.2.1, the software tool developed by the Joint Research Centre of the European Commission, for providing a simulation environment for sensitivity analysis.

To my wife, kind acknowledgements and special thanks are conveyed for your continued love, support and patience in the making of this thesis. To my family members: my late father, my mother, sister, and brother, thank you for your loving and constant encouragement.

To my friends, and research partners, thank you very much for your support during this research. The completion of this project would not have been possible without support from you.

Nanang Rohadi, June 2013

This page is blank



# Contents

- Abstract ..... iii**
- Statement of Originality ..... v**
- Acknowledgements ..... vii**
- Contents ..... ix**
- List of Figures ..... xiii**
- List of Tables ..... xix**
- Glossary of Symbols ..... xxi**
- Abbreviations ..... xxix**
- List of Publications ..... xxxi**
- Chapter 1 ..... 1**
- Introduction ..... 1**
  - 1.1. Uncertainty in Impedance Measurement and Performance Testing ..... 1
  - 1.2. Objectives of this Thesis ..... 4
  - 1.3. Outline of the Thesis ..... 4
- Chapter 2 ..... 6**
- Review of Distance Protection Functions ..... 6**
  - 2.1. Introduction ..... 6
  - 2.2. Distance Protection ..... 7
    - 2.2.1. Principle of Operation of the Distance Protection Function ..... 7
    - 2.2.2. Self- Polarization Mho Characteristic ..... 9
    - 2.2.3. Zone Classification and Setting ..... 12
    - 2.2.4. Fault Impedance Measurement ..... 15

Processing Signals for Fault Impedance Measurement .....	15
Fault Impedance Measurement Technique .....	16
Zero Sequence Current Compensation.....	19
Performance Evaluation.....	21
2.3. Generalized Protection Relay Structure .....	23
2.3.1. Analog Anti Aliasing and DC-Offset Removing Filter.....	25
2.3.2. Digital Filtering .....	26
2.3.3. Impedance Unit.....	28
2.4. Possible Effects on Fault Impedance Calculation .....	29
2.4.1. Effect of Combination between Fault Resistance and Power Flow Angle.....	31
2.4.2. Effect of Applying Series Compensation .....	33
2.4.3. Effect of Mutual Coupling on Distance Relay Operation .....	36
2.4.4. Effect of Tapped Line on Distance Relay Operation.....	40
<b>Chapter 3 .....</b>	<b>44</b>
<b>Transmission Network Model for Fault Impedance Calculation.....</b>	<b>44</b>
3.1. Introduction .....	44
3.2. Line Impedance Calculation.....	45
3.3. Network System Models for Protection Study.....	54
3.3.1. Two Terminal Network Representing Single-Circuit Line .....	54
3.3.2. Two Terminal Network Representing Double-Circuit Line.....	56
3.3.3. Multi-terminal Network Representing Tapped Line .....	57
3.4. Fault Impedance Calculation and Uncertainty .....	59
3.4.1. Fault Impedance Measurement for Line with Sources at Both Ends .....	59
3.4.2. Fault Impedance Measurement for Double-circuit Line .....	62
3.4.3. Fault Impedance Measurement for Three-Terminal Line .....	65
3.4.4. Fault Impedance Measurement for One Line with Series Capacitor.....	72
<b>Chapter 4 .....</b>	<b>77</b>
<b>Sensitivity Analysis for Impedance Measurement Algorithm of Distance Relay .....</b>	<b>77</b>
4.1. Introduction .....	77
4.2. Sensitivity Analysis Techniques .....	78
4.2.1. Morris Method.....	78

4.2.2. Variance Based Sensitivity using Sobol Method .....	79
4.3. SIMLAB Tool for Sensitivity Analysis .....	81
<b>Chapter 5.....</b>	<b>87</b>
<b>A Proposed Methodology .....</b>	<b>87</b>
5.1. Introduction .....	87
5.2. Testing Environment .....	89
5.3. Power System Protection Modelling and Simulation in DIgSILENT .....	90
5.3.1. Simulation Tool - DIgSILENT .....	91
5.3.2. Power System Protection Modelling and Data Manipulation.....	93
Power System Protection Modelling in DIgSILENT .....	93
Data Manipulation.....	96
5.3.3. Protective Distance Relay Simulation.....	98
5.4. Implementation of the Sensitivity Analysis Methodology .....	99
5.5. Conclusions .....	102
<b>Chapter 6.....</b>	<b>104</b>
<b>Case Studies .....</b>	<b>104</b>
6.1. Case study I: One Line with Two Sources .....	105
6.1.1. Description of the Case Study.....	105
6.1.2. Evaluation of Relay Algorithm Performance .....	106
6.1.3. Test Result and Discussion .....	111
6.2. Case study II: Double Lines with Two Sources Model.....	114
6.2.1. Description of the Case Study.....	114
6.2.2. Evaluation of Relay Algorithm Performance .....	115
6.2.3. Test Result and Discussion .....	119
6.3. Case study III: Three-Terminal Line .....	122
6.3.1. Description of the Case Study.....	122
6.3.2. Evaluation of Relay Algorithm Performance .....	124
6.3.3. The Test Result and Discussion.....	129
6.4. Case study IV: Two Port of Transmission Line with Series Compensation .....	132
6.4.1. Description of the Case Study.....	132
6.4.2. Evaluation of Relay Algorithm Performacne .....	134

6.4.3. Test Result and Discussion .....	141
6.5. Conclusions .....	146
<b>Chapter 7 .....</b>	<b>148</b>
<b>Conclusions .....</b>	<b>148</b>
<b>Appendix A .....</b>	<b>151</b>
<b>Transmission Data .....</b>	<b>151</b>
<b>Appendix B .....</b>	<b>154</b>
<b>DPL Implementation in DIgSILENT .....</b>	<b>154</b>
B.1. The DPL Script Program .....	154
B.2. The DPL Command Object .....	158
<b>Appendix C .....</b>	<b>159</b>
<b>Sample File.....</b>	<b>159</b>
<b>References .....</b>	<b>161</b>

# List of Figures

2.1.	Distance protection principle of measured fault impedance .....	8
2.2.	Self-Polarized Mho Characteristic with a reach of $r\underline{Z}_{1L}$ .....	11
2.3.	Voltage Diagram of Self-Polarizing Mho Characteristic .....	12
2.4.	Zone classification and stepped time of distance relay operation .....	15
2.5.	Fault input signals and fault impedance: (a) phase voltages, (b) phase current, (c) and fault impedance, at the relaying point .....	16
2.6.	AG apparent impedance plane (including fault resistance, $R_F$ ) .....	18
2.7.	Sequence network connection for SLG fault.....	18
2.8.	Steady state error of fault impedance measurement: fault at 50% of $\underline{Z}_L$ , $R_F=10 \Omega$ .....	22
2.9.	Physical model of IED (i.e., SEL-421 distance relay).....	23
2.10.	Simplified block diagram of protection scheme.....	24
2.11.	The “Measuring” type dialog with the available filtering methods.....	28
2.12.	The “Polarizing” type dialog .....	30
2.13.	Typical phases to ground fault.....	32
2.14.	Effect of Fault Resistance, $R_F$ , and Power Flow Angle, $\delta_F$ .....	33
2.15.	Schematic diagram of the series compensated line: $F_1$ , fault in front of SCs and $F_2$ , fault behind SCs .....	34
2.16.	Effect of reduced fault reactance due to series capacitor .....	35
2.17.	Voltage profile and phasor diagram for a forward fault.....	36
2.18.	Typical Parallel-Line System .....	37
2.19.	Zero-sequence component system of parallel line circuit: (a) Two lines are active, (b) One line is switched off and grounded at both ends.....	38

2.20.	Effect of mutual coupling on impedance measurement .....	39
2.21.	Effect of changing value of zero sequence current compensation, $k_0$ , in impedance measurement .....	40
2.22.	The circuit with tapping line .....	41
2.23.	Rearrangement of the system of Figure 2.22 .....	42
2.24.	Total fault current $I_{ST}$ with varying $Z_{L3}$ .....	43
2.25.	Impedance seen by distance relay at terminal S .....	43
3.1.	Lumped parameter 3 phase Impedance Network .....	45
3.2.	The flux linkage on one conductor .....	48
3.3.	The flux linkage between 2 points outside of the line .....	48
3.4.	Three-phase transmission line .....	51
3.5.	Line conductors arranged in a bundle configuration .....	52
3.6.	Simple two-port network equivalent: a) General scheme, b) General equivalent scheme, c) Simplified scheme .....	55
3.7.	Equivalent Scheme of power network with Parallel Line .....	56
3.8.	Parallel Line Modes .....	57
3.9.	Multi-terminal with tapping line network equivalent: a) General equivalent scheme, b) Simplified scheme .....	58
3.10.	A typical single line system .....	59
3.11.	Sequence networks for the phase A to ground fault in Figure 3.10 .....	62
3.12.	Single line diagram for the phase A to ground fault on a parallel line circuits with two sources, $\underline{E}_S$ and $\underline{E}_R$ .....	63
3.13.	Sequence networks for both lines in operation in a phase A to ground fault in Figure 3.12 .....	65
3.14.	Single line diagram for the phase A to ground fault on a three-terminal line .....	66
3.15.	Sequence component circuit for the fault at $F_1$ in Figure 3.14 .....	67
3.16.	Sequence component circuit for the fault at $F_2$ in Fig 3.14 .....	70
3.17.	Single line diagram for the phase A to ground fault on a transmission line with series compensator: $F_1$ - fault location in front of SCs, $F_2$ - fault location behind SCs .....	72
3.18.	Normalized equivalent resistance and reactance vs normalized current .....	73
3.19.	Two-Source Symmetrical Component for AG fault at $F_2$ with fault resistance ...	75

4.1.	Main window of SIMLAB .....	82
4.2.	Pre-processing frame .....	83
4.3.	Morris Sampling Method.....	83
4.4.	Sobol Method Panel.....	84
4.5.	Model execution .....	85
4.6.	Statistical Post-Processor.....	86
5.1.	The proposed Structure of the Testing Environment.....	90
5.2.	Relationship between relay model and power network .....	92
5.3.	Network Model configuring using DIgSILENT .....	94
5.4.	The main measurement block of distance relay scheme .....	95
5.5.	DIgSILENT data manager window showing protection elements implemented in the relay model .....	95
5.6.	The “Polarizing” type dialog .....	96
5.7.	Simulation controlled by DPL program .....	97
5.8.	Principle of a DPL command .....	97
5.9.	Protective relay test systems based on combination between DIgSILENT and SIMLAB .....	99
5.10.	Flow chart of Testing.....	99
5.11.	The structure of the test software environment .....	102
6.1.	Circuit diagram of faulted line with sources at both ends and uncertain factors indicated in red .....	106
6.2.	Measured impedance trace against IED Mho characteristic for the phase-A to ground fault shown in Figure 6.1.....	108
6.3.	Percentage error of the $I_m(\underline{Z}_m)$ measurement as a function of $\delta_F$ for resistive faults, $R_F = 10 \Omega$ , on the line shown in Figure 6.1 at three locations.....	108
6.4.	Percentage error of the reactance measurement as a function of the ratio, $\underline{Z}_{SM}/\underline{Z}_{SN}$ , for the faults in the network in Figure 6.1 at four fault locations, and for fixed parameters, $\delta_F = 0^\circ$ and $R_F = 10 \Omega$ .....	108
6.5.	Effect of uncertainty of the setting factor $\underline{k}_0$ as a function of distance to fault location for fixed parameters, $R_F = 0 \Omega$ and $\delta_F = 0^\circ$ .....	109
6.6.	Effect of errors in the line positive-sequence impedance setting value, $\underline{Z}_{1L}$ , in function of distance to fault for the A-phase to ground faults in the system	

	shown in Figure 6.1. Other factors are kept constant, $R_F = 0 \Omega$ and $\delta_F = 0^\circ$ ....	109
6.7.	Fault impedance measured for all samples of the input factors, $\mathbf{x} \in \mathbf{R}^{14}$ , generated according to the random sampling method (total of 500 samples) for three different fault locations.....	111
6.8.	Results of the Morris factor screening method for a single-phase short circuit at 80% of the line in Figure 6.1 .....	113
6.9.	Main effects in function of the fault position obtained by using the GSA procedure for four-dimensional factor space.....	113
6.10.	Interaction effects in function of the fault position obtained by using the GSA procedure for four-dimensional factor space.....	113
6.11.	Circuit diagram of the faulted system with uncertain factors shown in red.....	115
6.12.	Measurement error for three operational modes and different distances of fault location, $R_F = 0 \Omega$ .....	116
6.13.	Measurement error due to uncertainty of the factor, $R_F$ , and zero-sequence mutual coupling (two line are active).....	117
6.14.	Measurement error due to uncertainty of the factor, $k_o$ , and zero-sequence mutual coupling (two line are active and $R_F = 0 \Omega$ ) .....	117
6.15a.	Fault impedance measured for all samples of the input factors, $\mathbf{x} \in \mathbf{R}^{11}$ , generated according to the random sampling method (total of 500 samples) for three different fault locations ( the parallel line is loaded ).....	118
6.15b.	Fault impedance measured for all samples of the input factors, $\mathbf{x} \in \mathbf{R}^{11}$ , generated according to the random sampling method (total of 500 samples) for three different fault locations ( the parallel line is not loaded...) .....	119
6.16.	Results of the Morris method for all three operational modes of the parallel line .....	120
6.17.	Main effects in function of the fault position obtained by using the GSA procedure for three-dimensional factor space .....	121
6.18.	Interaction effects in function of the fault position obtained by using the GSA procedure for three-dimensional factor space .....	122
6.19.	Circuit of the faulted system with uncertain factors printed in red.....	124
6.20.	Impedance tracking for the fault at the border of Zone 1. The blue line is for the case where $R_F = 0$ , and the red line is for the case	



where $R_F = 10 \Omega$ .....	125
6.21. Measured fault impedance from different fault sections .....	126
6.22. Measured impedance region from different fault sections .....	127
6.23. Fault impedance measured for all samples of the input factors, $\mathbf{x} \in \mathbf{R}^{29}$ , generated according to the random sampling method (total of 500 samples) for three different fault locations .....	129
6.24. The Morris method results for a fault at 1p.u. of the line S-R in Figure 6.19 ...	130
6.25. Main effects in function of the fault position obtained by using the GSA procedure for five-dimensional factor space .....	131
6.26. Interaction effects in function of the fault position obtained by using the GSA procedure for five-dimensional factor space .....	132
6.27. Two sources of series compensation with uncertain factors printed in red:.....	134
6.28. Equivalentting and characteristic of SCs and MOVs: (a) The original device and $\underline{v-i}$ characteristic of the MOV, (b) Equivalentting .....	135
6.29. Fault Impedance tracking for the fault, $F_1$ at 0.4 p.u., $R_F = 10 \Omega$ , $\delta_F = 0^\circ$ ....	136
6.30. Phase voltage at terminal S.....	137
6.31. Phase current at terminal S .....	137
6.32. Voltage drops across SCs + MOVs .....	137
6.33. Distribution of the phase A fault current among SCs ( $I_{cap}$ ) .....	138
6.34. Fault Impedance tracking for the fault $F_2$ at 0.75 p.u., $R_F = 10 \Omega$ , $\delta_F = 0^\circ$ ....	138
6.35. Fault impedance measured for all samples of the input factors, $\mathbf{x} \in \mathbf{R}^{19}$ , generated according to the random sampling method (total of 500 samples) for three different fault locations (a) when the fault is simulated in front of the SCs, (b) when the fault is simulated behind the SCs .....	141
6.36. Results of the Morris factor screening method: (a) for a single-phase short circuit at 0.2 p.u. (in front of the SCs), (b) 0.8 p.u. (behind the SCs) .....	143
6.37. Sensitivity indices in function of the fault position obtained by using the GSA procedure for five-dimensional factor space: .....	144
6.38. Sensitivity indices in function of the fault position obtained by using the GSA procedure for three-dimensional factor space: .....	145
B2. A DPL export script.....	158

This page is blank

# List of Tables

2.1.	Simple Impedance Equation.....	29
6.1.	Uncertain factors and their assumed intervals of variation that are affecting fault impedance measurements for the single-phase to ground faults in Figure 6.1.....	110
6.2.	Uncertain factors and their assumed intervals of variation that are affecting fault impedance measurements for the single-phase to ground faults in Figure 6.11.....	118
6.3.	Uncertain factors and their assumed intervals of variation that are affecting fault impedance measurements for the single-phase to ground faults in Figure 6.19.....	128
6.4.	Uncertain factors and their assumed intervals of variation that are affecting fault impedance measurements for the single-phase to ground faults in Figure 6.27.....	139
A.1.	System parameters of the test one line with sources at both ends.....	151
A.2.	System parameters of the test double-circuit line with sources at both ends .....	152
A.3.	System parameters of the test three terminal line.....	152
A.4.	System parameters of the test one line with series compensation.....	153

This page is blank

# Glossary of Symbols

$\underline{E}_S, \underline{E}_R, \underline{E}_T$	source voltage behind terminal S , R, T, respectively	V
$\underline{E}_{1S}$	positive-sequence voltage behind terminal S	V
$F$	fault location	p.u.
$\underline{I}_1, \underline{I}_2, \underline{I}_0$	positive-, negative-, and zero-sequence current, respectively	A
$\underline{I}_{1S}, \underline{I}_{2S}, \underline{I}_{0S}$	positive-, negative-, zero-sequence current at terminal S, respectively	A
$\underline{I}_{AB}$	phase A-B current at the end S during the fault	A
$\underline{I}_{BC}$	phase B-C current at the end S during the fault	A
$\underline{I}_{CA}$	phase C-A current at the end S during the fault	A
$\underline{V}_{AB}$	phase A-B voltage at the end S during the fault	V
$\underline{V}_{BC}$	phase B-C voltage at the end S during the fault	V
$\underline{V}_{CA}$	phase C-A voltage at the end S during the fault	V
$\underline{I}_F$	pure-fault current flowing through the fault resistance	A
$\underline{V}_F$	voltage drop from relaying point to fault location F	V
$\underline{\Delta V}$	random errors of measured voltage distributed value	V
$\underline{\Delta I}$	random errors of measured current distributed value	I
$\underline{I}_S$	total line current at the end S during the fault	A

$\underline{I}_A, \underline{I}_B, \underline{I}_C$	phase-A, Phase-B, Phase-C current at the end S during the fault, respectively	A
$\underline{I}_S^C$	total compensated current at the end S during the fault	A
$\underline{I}_A^C$	phase-A compensated current at the end S during the fault	A
$\underline{k}_0$	zero-sequence current compensation factor	
$k_{0M}$	zero-sequence current compensation factor of mutual coupling	
$\underline{I}_{0P}$	zero-sequence current parallel line with both lines in active	A
$\underline{I}'_{0P}$	zero-sequence current parallel line with one is switched off and grounded at both sides	A
$\underline{k}_{0(mod)}$	modified of zero-sequence current compensation factor	
$p$	proportional of the total line from terminal S	p.u.
$r$	zone reach from terminal S	p.u.
$R_{1L}, R_{0L}$	positive- and zero-sequence line resistances, respectively	$\Omega$
$R_{1S}, R_{1R}$	positive -sequence source resistance at station S and R, respectively	$\Omega$
$R_F$	fault resistance	$\Omega$
$X_C$	capacitor reactance	$\Omega$
$X_L$	inductor reactance	$\Omega$
$R'_F$	resistance and capacitive/inductive reactance	$\Omega$
$\underline{V}_1, \underline{V}_2, \underline{V}_0$	positive-, negative-, and zero-sequence voltage, respectively	V
$\underline{V}_{1S}, \underline{V}_{2S}, \underline{V}_{0S}$	positive-, negative-, and zero-sequence voltage at terminal S, respectively	V

$\underline{V}_S$	total voltage at the line end S during the fault	V
$X_{1L}, X_{0L}$	positive- and zero-sequence line reactance, respectively	$\Omega$
$\Delta \underline{Z}_m$	error calculated in apparent fault impedance on the line at terminal S	$\Omega$
$\underline{Z}_{Ref}$	expected value of apparent fault impedance	$\Omega$
$\underline{Z}_{m(sec.)}$	secondary part of measured impedance on the line at terminal S	$\Omega$
$\underline{Z}_m$	measured fault impedance on the line at terminal S	$\Omega$
$\underline{Z}_{1S}, \underline{Z}_{1R}$	positive-sequence source impedance behind bus S and R, respectively	$\Omega$
$\underline{Z}_{0S}, \underline{Z}_{0R}$	zero-sequence source impedance behind bus S and R, respectively	$\Omega$
$\underline{Z}_{1L}, \underline{Z}_{0L}$	positive- and zero- sequence line impedance, respectively	$\Omega$
$\underline{Z}_S, \underline{Z}_R, \underline{Z}_T$	source impedance behind bus S, R, and T respectively	$\Omega$
$\underline{Z}_L$	total line impedance	$\Omega$
$\underline{Z}_{OM}$	mutual impedance of line for the zero-sequence network	$\Omega$
$\underline{Z}_{est}$	estimated impedance of line	$\Omega$
$\underline{Z}_{act}$	actual impedance of line	$\Omega$
$\underline{Z}_{tot}$	total impedance of line (total protected line impedance)	$\Omega$
$\underline{Z}_{012}$	sequence impedance matrix	$\Omega$
$\underline{Z}_{E1}, \underline{Z}_{E2}, \underline{Z}_{E3}$	equivalent of external line impedance	$\Omega$
$\theta_L$	the angle of maximum reach	deg
$\underline{S}_{Pol}$	polarizing quantity	$\Omega$

$\underline{S}_{op}$	operating quantity	$\Omega$
$\underline{V}^*_{pol}$	polarising voltage	V
$\theta$	impedance relay operation angle	deg
$\phi_i$	angle of the measured current	deg
$\phi_V$	angle of the measured voltage	deg
$error_{ss}$	error steady state	%
$\delta_F$	pre-fault power flow angle	deg
$\underline{Z}_{1L1}, \underline{Z}_{1L2},$ $\underline{Z}_{1L3}$	positive- sequence line impedance, Line-1, Line-2, and Line-3, respectively	$\Omega$
$x_i$	a number of factors	
$\underline{v}_s(t)$	time varying of measured voltage from terminal S of transmission line	V
$\underline{i}_s(t)$	time varying of measured line current	A
$\Delta t$	sampling interval	s
$\tau$	time constant	s
$N$	number of samples per period	
$\Delta$	difference	
$H(s)$	transfer function	
$s_i$	poles of transfer function	
$\pi$	mathematical constant	3.14
$A$	constant value	
$\delta_S, \delta_R, \delta_T$	power flow angle of source impedance in bus S, R, T respectively	deg



$x_k$	sample of signal with dc-offset	
$\varphi$	phase angle	deg
$\underline{V}_{peak}$	maksimum voltage	V
$\omega$	machine angular speed	rad/s
$t$	time	s
$\rho$	conductivity of material	$\Omega \cdot m$
$l$	length of the conductor	m
$A$	cross sectional area	$m^2$
$R_{dc}$	dc-resistance	$\Omega$
$L_{int}$	internal inductance	H
$L_{ext}$	external inductance	H
$L_{tot}$	total inductance	H
$R_{t1}$	dc-resistance at temperature $t_1$	$\Omega$
$R_{t2}$	dc-resistance at temperature $t_2$	$\Omega$
$t_1, t_2$	first temperature, second temperature	$^{\circ}C$
$M$	temperature constant	
$H$	magnetic intencity	A/m
$B$	magnetic dencity	T
$\lambda$	flux linkage	Wb- turn/m
$d\Phi$	differential flux	Wb/m
$X_A$	inductive reactance of phase A	$\Omega$
$\Phi_{AB}, \Phi_{AC}$	flux due to $I_B$ and $I_C$	Wb

$\underline{Z}_{xy}$	line impedance, $xx$ for self impedance and $xy$ mutual impedance, where $xy = a, b, c$	$\Omega$
$\underline{V}_{AS}, \underline{V}_{BS}, \underline{V}_{CS},$	phase to ground voltage measured from terminal S of	V
$\underline{V}_{AR}, \underline{V}_{BR}, \underline{V}_{CR},$	phase to ground voltage measured from terminal R of	V
$\underline{V}_{C1}, \underline{V}_{C2}, \underline{V}_{C0},$	sequence voltage of series capacitor	V
$\emptyset_{AA,self},$	self flux in phase A	Wb
$\emptyset_{AA,self}$	another self-flux of phase A	Wb
$\underline{V}_{real}$	real voltage value	V
$\underline{V}_{imag}$	imaginary voltage value	V
$\underline{V}_{mag}$	magnitude voltage	V
$\underline{V}_{angle}$	voltage angle	deg
$\underline{S}_k.$	sampled value	
$E_i$	‘elementary effect’ calculation for Morris method	
$d$	number of discretization grid levels	
$\mu$	mean	
$\sigma$	Standard deviation	
$E\{*\}$	expected operator	
$V(f(\mathbf{x}))$	Total variance	
$S_i$	sensitivity indice	
$x_i, x_j$	two independence factors	

$Re\{\underline{Z}_{0S}\},$ $Re\{\underline{Z}_{0R}\}$	real value of zero-sequence of source impedance in terminal S and terminal R	$\Omega$
$Im\{\underline{Z}_{0S}\},$ $Im\{\underline{Z}_{0R}\}$	imaginary value of zero-sequence of source impedance in terminal S and terminal R	$\Omega$
$Re\{\underline{Z}_{1S}\},$ $Re\{\underline{Z}_{1R}\}$	real value of positive-sequence of source impedance in terminal S and terminal R	$\Omega$
$Im\{\underline{Z}_{1S}\},$ $Im\{\underline{Z}_{1R}\}$	imaginary value of positive-sequence of source impedance in terminal S and terminal R	$\Omega$
$Re\{\underline{Z}_{1L}\},$ $Re\{\underline{Z}_{0L}\}$	real value of positive- and zero-sequence of line impedance	$\Omega$
$Im\{\underline{Z}_{1L}\},$ $Im\{\underline{Z}_{0L}\}$	imaginary value of positive- and zero-sequence of line impedance	$\Omega$
$f$	non linear complex function	
$\underline{P}_S$	group of positive- and zero-sequence sources impedance	
$\underline{P}_E$	group of sources of voltage	
$\underline{P}_L$	group of positive- and zero-sequence line impedance	
$\underline{V}_{REF}$	reference voltage	V
$\underline{V}_V$	voltage drop across the capacitor	V
$q$	exponent	
$P$	reference current	A
$R'_c$	equivalent series resistance	$\Omega$
$X'_c$	equivalent series reactance	$\Omega$
$X_{CO}$	capacitor bank reactance	$\Omega$

This page is blank

# Abbreviations

A/D	Analogue to Digital converter
ANOVA	Analysis of Variance
CT	Current Transformer
CVT	Capacitor Voltage Transformer
EMT	Electromagnetic Transient
GSA	Global Sensitivity Analysis
IEDs	Intelligent Electronic Devices
DPL	DIgSILENT Programming Language
QMC	Quasi-Monte Carlo
MCF	Modified Compensation Factor
GMR	Geometric Mean Radius
CB	Circuit Breaker

SCs	Series Capacitors
DFT	Discrete Fourier Transform
MOVs	Metal Oxide Varistors
SA	Sensitivity Analysis
GUI	Graphical User Interface
DSL	Dynamic Simulation Language

# List of Publications

- [P1] M.N. Ibrahim, **N. Rohadi** and R. Zivanovic, “Methodology for Automated Testing of Transmission Line Fault Locator Algorithms”, Australasian Universities Power Engineering Conference (AUPEC 2009), 27-30 September 2009, Adelaide-Australia.
- [P2] **N. Rohadi** and R. Zivanovic, “Sensitivity Analysis of Impedance Measurement Algorithms Used in Distance Protection”, IEEE TENCON 2011, Bali, Indonesia, November 22-24, 2011.
- [P3] **N. Rohadi** and R. Zivanovic, “Sensitivity Analysis of Fault Impedance Measurement Algorithm Used in Protection of Three-Terminal Lines”, Australasian Universities Power Engineering Conference (AUPEC 2012), 26-29 September 2012, Bali-Indonesia.
- [P4] **N. Rohadi** and R. Zivanovic, ” Sensitivity Analysis of a Fault Impedance Measurement Algorithm Applied in Protection of Parallel Transmission Lines”, The 9<sup>th</sup> IET International Conference on Advances in Power System Control, Operation and Management (APSCOM 2012), 18-21 November 2012, Hong Kong
- [P5] **N. Rohadi**, R. Zivanovic, “A Method for Sensitivity Analysis of Impedance Measurement Algorithm”, Journal of Electrical Engineering, Springer, 2013 (under reviewed).
- [P6] **N. Rohadi**, R. Zivanovic, “Sensitivity Analysis of Impedance Measurement Algorithms Used in Series-Compensated Power Transmission Line”, Journal of IET Generation, Transmission & Distribution, 2013 (under reviewed)