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# 3D Finite Element Modeling of Absorbing Regions for Guided Wave Scattering Problems in Composite Materials

Ching-Tai Ng

**Abstract**—This paper presents a three-dimensional (3D) finite element (FE) model of the absorbing regions for guided wave (GW) scattering in composite materials. The model is aimed at providing an efficient and practical numerical modeling technique for analyzing GW propagation and scattering in infinitely long composite structures. The reported study sought to find the optimal configuration of the absorbing regions to not only minimize the wave reflection from boundaries, but also the computational cost. The model with the optimal absorbing regions was then applied to investigate the GW scattering characteristics for different types and sizes of defects in laminated composite beams.

**Index Terms**—guided wave; absorbing region; finite element; scattering; composite material; damage detection

## I. INTRODUCTION

Infrastructure safety has received significant attention in the last decade, with a variety of damage detection methods developed by a number of researchers in an effort to ensure structural safety and reduce maintenance costs [1-3]. Their research suggests that guided wave (GW) offers outstanding detection capabilities, including large area inspection, high sensitivity to most types of damage and high efficiency in detecting small and subsurface defects [4]. The research investigations can be divided into two major areas – scattering characteristics studies [5] and developments of damage detection techniques [6-8].

The use of laminated composite materials has steadily increased in different engineering industries, such as civil, building and aerospace. However, delamination is a serious weakness in structures made with composites as it can cause a reduction of up to 60% in the residual compressive strength of structures [9] and is visually undetectable. The growing use of composite materials, however, has meant that researchers continue to develop methods for detecting hidden delamination in order to ensure structural safety.

The successful development of GW based damage detection techniques requires an understanding of GW propagation and scattering characteristics at defects. Analytical solutions of GW

scattering at defects do not exist for laminated composite materials because of their anisotropic nature and multilayer characteristics. On the other hand, a number of studies [10-15] have been carried out using FE simulations to provide improved insight into the scattering phenomena of GWs at different types of defects in laminated composite materials.

Simulations of GWs in structures are computationally expensive as they require an enough number of FE nodes per wavelength of GW to guarantee the accuracy of the simulation results. But the wavelength of GW is usually in the order of millimeters. To improve the computational efficiency of GW simulations, therefore, different FE modeling strategies have been developed for studying the scattering effects. Liu and Quek [16], for example, proposed a non-reflecting boundary for wave propagation in an infinitely long two-dimensional (2D) isotropic plate using a gradually damped artificial boundary; while Drozd *et al.* [17] suggested a method of modeling GW propagation with a FE method using frequency domain analysis and absorbing regions for isotropic materials. A technique for predicting the far-field scattering behavior of GWs at defects in anisotropic materials developed by Velichko and Wilcox [18] has proved both robust and efficient.

The current study investigates 3D FE modeling of GW propagation with different types of defects in laminated composite beams, as explained in Section II. The effect of using gradually increasing damping in the absorbing region is then discussed in detail in Section III. Section IV demonstrates how the developed 3D FE model can be employed in absorbing regions to study the scattering characteristics of the fundamental anti-symmetric mode ( $A_0$ ) GWs at different types of defects in laminated composite beams. Finally, conclusions are drawn in Section V.

## II. 3D FINITE ELEMENT SIMULATIONS

### A. Modeling of guided waves in laminated composite beams

GW propagation and scattering in laminated composite beams is described by a governing equation as a general structural dynamic problem

$$\mathbf{M}\ddot{\mathbf{u}} + \mathbf{C}\dot{\mathbf{u}} + \mathbf{K}\mathbf{u} = \mathbf{P} \quad (1)$$

where  $\ddot{\mathbf{u}}$ ,  $\dot{\mathbf{u}}$  and  $\mathbf{u}$  are acceleration, velocity and displacement vectors.  $\mathbf{M}$ ,  $\mathbf{C}$ ,  $\mathbf{K}$  and  $\mathbf{P}$  are the mass matrix, damping matrix, stiffness matrix and external force vector. Commercial FE software ABAQUS/Standard can be used to solve the

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dynamics problems. ABAQUS/Standard employs an implicit FE method using the Newmark integration scheme and the Hilber-Hughes-Taylor method [19].

A [-45/45/0/90]<sub>s</sub> laminated composite beam was selected as the specimen for the current study. Each lamina was assumed to be a Cycom® 970/T300 unidirectional carbon/epoxy prepreg tape. The tape was 0.2 mm thick, and the material properties were: Young's modulus  $E_1 = 128.75$  GPa,  $E_2 = E_3 = 8.35$  GPa; shear modulus  $G_{12} = G_{13} = 4.47$  GPa,  $G_{23} = 2.90$  GPa; Poisson's ratio  $\nu_{12} = \nu_{13} = 0.33$ ,  $\nu_{23} = 0.44$ . The density was  $1517$  kg/m<sup>3</sup>. The fiber volume fraction was 0.55. Each lamina was modeled by 8-noded, 3D reduced integration solid brick elements (C3D8R) with hourglass control; and orthotropic material could be assumed, given the material properties of the prepreg tape.

The key parameters of the laminated composite beam were beam length  $L = 200$  mm; width  $b = 4.0$  mm; and height  $h = 1.6$  mm (Fig. 1).

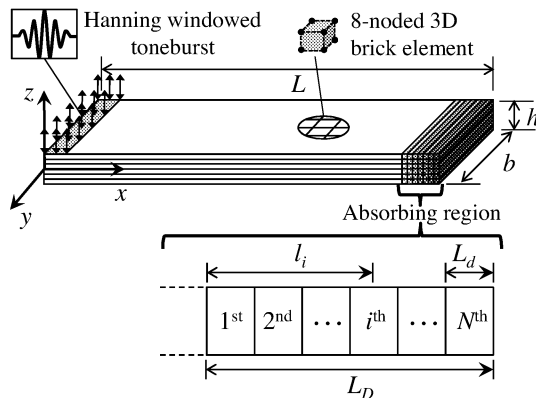


Fig. 1. Schematic diagram of the 3D FE laminated composite beam model

The excitation signal was a 200 kHz narrow-band eight-cycle sinusoidal toneburst pulse modulated by a Hanning window. The  $A_0$  GW was generated by applying the out-of-plane displacement to the nodes in the rectangular area at the beam end as shown in Fig. 1. The  $A_0$  GW at particular locations was obtained by monitoring the out-of-plane displacement of nodes located at the mid-thickness of the laminated composite beam. This ensured that only the  $A_0$  GW was detected since the  $S_0$  and fundamental shear horizontal ( $SH_0$ ) GW exhibit zero out-of-plane displacement of the nodes located at mid-thickness. The phase velocity, group velocity and wavelength of the excited  $A_0$  GW were  $1529.19$  m/s,  $1259.79$  m/s and  $6.30$  mm. The in-plane dimension of the solid brick elements was  $0.4 \times 0.4$  mm<sup>2</sup> and the thickness was  $0.2$  mm. This guaranteed that there were at least 16 FE nodes per wavelength to ensure the accuracy of the simulation results.

The out-of-plane displacements were measured at  $x = 50$  mm,  $70$  mm,  $90$  mm,  $110$  mm and  $130$  mm; with  $y = -2.0$  mm and  $z = 0$  mm. The FE calculated group velocity ( $1501.42$  m/s) was close to the velocity ( $1529.19$  m/s) calculated by the first order shear deformation theory with coupling between axial-flexural-shear motion.

Two types of damage – notches and delaminations – were considered in the current study. The notches were created by removing elements from the FE model. Delaminations across the full width of the laminated composite beams were modeled

by creating duplicate nodes at the delamination interface. Therefore, the coinciding nodes in the delaminated region had a separate identity. Similar modeling techniques were employed in [11,13] and there was good agreement between the FE simulation results and experimental measurements.

### B. Modeling of absorbing regions using gradually increased damping

Gradually increased damping can be used to model the absorbing regions for the boundaries of GWs in laminated composite beams. Rayleigh damping, which is a combination of mass- and stiffness-proportional damping, was used in the current study to form the damping matrix  $\mathbf{C}$  in (1) as

$$\mathbf{C} = \alpha \mathbf{M} + \beta \mathbf{K} \quad (2)$$

where  $\alpha$  and  $\beta$  are Rayleigh coefficients used for damping in the lower and higher frequencies, respectively. For GW problems, damping layers with gradually increasing values of  $\beta$  are used to construct the absorbing regions. As shown in Fig. 1, the value of  $\beta_i$  at the  $i$ -th damping layer in the absorbing region can be estimated by [20] as

$$\beta_i = 2\pi f \left( \frac{l_i}{L_D} \right)^2 \quad \text{for } i = 1, \dots, N \quad (3)$$

where  $l_i$  is the distance from the centre of the  $i$ -th damping layer to the starting boundary of the absorbing region, as shown in Fig. 1.  $L_D$  is the total length of the absorbing region.  $N$  is the total number of damping layers in the absorbing region.  $f$  (in Hz) is the central frequency of the excited GWs.  $L_d = L_D / N$  is the length of each individual damping layer. As indicated in (3) the value of  $\beta_i$  is gradually increased from  $\beta_1$  to  $\beta_N$ . Assuming the total length of the absorbing region  $L_D$  is not fixed, there are fundamentally two parameters  $N$  and  $L_d$ , controlling the configuration of the absorbing region. It is obvious that the larger the values of  $N$  and  $L_d$  the larger the size of the FE model, increasing the computational cost of the simulations.

Theoretically, there is a global optimal configuration of the absorbing region that can simultaneously minimize the wave reflected from the boundaries and the computational cost of the simulations. However, the focus of the current study was not to determine the global optimal configuration of the absorbing region. In this study,  $L_d$  was assumed to be  $0.8$  mm in order to determine the optimal value of  $N$  that minimizes the wave reflected from the beam end.

## III. VALIDATION OF THE ABSORBING REGIONS

### A. Optimal value of $N$ for $L_d = 0.8$ mm

A number of simulations were carried out to determine the optimal value of  $N$ . It was assumed for 24 cases that  $N = 2$  to 25. The values of  $\beta_i$  for each case are shown in Fig. 2a, and each curve in Fig. 2a represents one FE simulation. The out-of-plane displacements were monitored at  $x = 140$  mm,  $y = -2.0$  mm and  $z = 0$  mm.

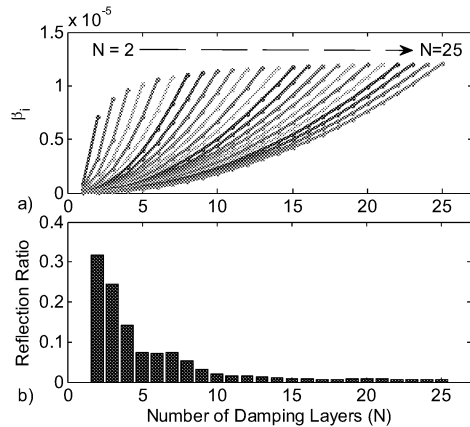


Fig. 2. (a) Values of stiffness-proportional damping and (b) corresponding reflection ratios for different  $N$

Fig. 2a shows the  $\beta_i$  for  $N$  values from 2 to 25. A series of parametric studies was conducted using  $\beta_i$  to determine the configuration of the absorbing region that could minimize the wave reflected from the boundaries. The absorbing region was then employed in the FE model developed in Section II, with the out-of-plane displacements monitored at  $x = 140$  mm,  $y = -2.0$  mm and  $z = 0$  mm, the latter of which was 60 mm from the beam end.

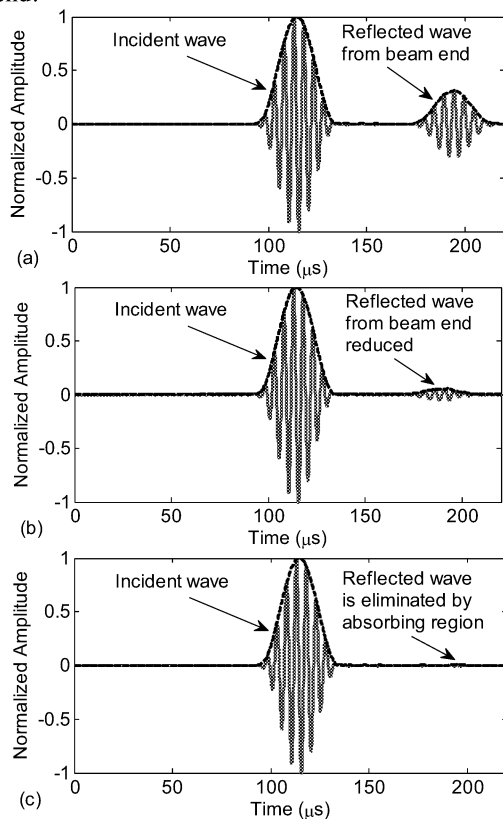


Fig. 3. Normalized amplitude of guided wave at location  $x = 140$  mm,  $y = -2.0$  mm and  $z = 0$  mm for  $L_d = 0.8$  mm, and (a)  $N = 2$ , (b)  $N = 8$  and (c)  $N = 17$ . (solid lines: normalized wave signal, dashed lines: normalized wave envelopes calculated by the Hilbert transform)

Figs. 3a, 3b and 3c show the calculated out-of-plane displacements at the monitoring locations for the models with  $N = 2$ , 8 and 17, respectively. All calculated out-of-plane displacements were normalized with respect to their maximum

displacements at the monitoring location, and hence, the maximum amplitude is equal to 1. The normalized signals and the wave envelopes calculated by the Hilbert transform [3] are indicated as solid and dashed lines, respectively, in Fig. 3.

Fig. 3a shows that the reflection ratio of the wave amplitude reflected from the beam end is reduced to 0.3172 by the absorbing region for which  $N = 2$ . The reflection ratio is the ratio of the incident wave amplitude to the reflected wave amplitude at the monitoring location. Fig. 3b shows that the reflection ratio can be further reduced to 0.0521 for the absorbing region for which  $N = 8$ . Fig. 3c shows that the reflection ratio for the absorbing region for which  $N = 17$  exhibited the best performance. The figure shows that the amplitude of the wave reflected from the beam end is almost completely eliminated by the absorbing region.

Fig. 2b shows the calculated reflection ratio of the GW from the beam end for the absorbing layer with different values of  $N$ . The figure indicates that the reflection ratio is minimized at  $N = 17$ , at which point, the reflection ratio is only 0.0066. Therefore, the absorbing region for which  $N = 17$  and  $L_d = 0.8$  mm was selected to investigate the GW scattering characteristics at defects in the laminated composite beam.

#### IV. GUIDED WAVE SCATTERING ANALYSIS

As shown in Fig. 4, the absorbing regions for which  $N = 17$  and  $L_d = 0.8$  mm are applied to both sides of the laminated composite beam in order to avoid wave reflection from the beam ends. The configuration of the efficient scattering model is shown in Fig. 4. The total length of each absorbing region at each beam end is 13.6 mm. As shown in Fig. 4, the measured out-of-plane displacements at monitoring points 1 and 2 are reflected and transmitted waves from the defects, respectively.

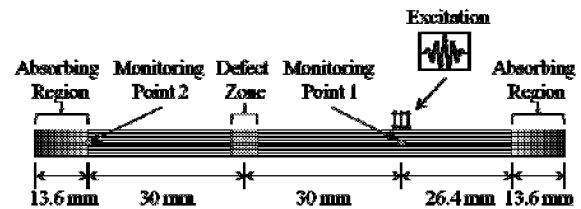


Fig. 4. Schematic of the 3D finite element scattering model

##### A. Effect of notches with different depths

Once the absorbing regions were validated, notch damage was investigated. As discussed in Section IIA, the notches are modeled by removing elements from the model. Fig. 5 shows four typical contour snapshots of the FE simulated out-of-plane displacement for  $A_0$  GW in the laminated composite beam with a notch. The first and second snapshots in Fig. 5 show that the  $A_0$  GW is generated at monitoring point 1 and then propagates to the notch at the left hand side and the absorbing region at the right beam end.

As shown in the third snapshot, the  $A_0$  GW interacts with the notch, which induces a transmitted and reflected wave in the laminated composite beam. Simultaneously, the excited  $A_0$  GW is absorbed by the absorbing region at the left beam end. The induced transmitted and reflected waves then propagate and

reach monitoring points 1 and 2, as shown in the forth snapshot in Fig. 5.

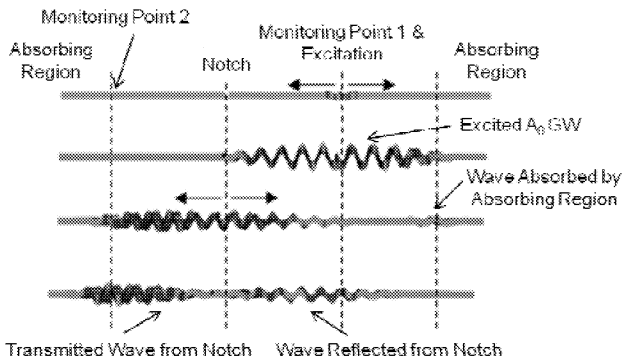


Fig. 5. Typical contour snapshots of FE simulated out-of-plane displacement for a  $A_0$  guided wave in the laminated composite beam with a notch

A series of FE simulations was performed, in which each simulation dealt with a notch of a different size. The effect of varying notch depths from 0.2 mm to 1.2 mm in 0.2 mm step increments was first investigated. The width of all the notches was 0.8 mm. Fig. 6 shows the envelopes of the reflected waves calculated at monitoring point 1. As the absorbing regions are used to eliminate the reflected waves from the beam ends, the signals in the figure only contain the incident wave and the wave reflected from the notches. In Fig. 6 the first wave peak represents the incident wave and the second represents the reflected wave from the notches.

In the present study the maximum amplitude of the reflected waves from the notches was a focus of the investigation. The reflected wave amplitude increased with the increase in notch depth. However, the reflected wave amplitude of the notch 1.4 mm in depth proved to be slightly less than that of the notch 1.2 mm deep. This phenomenon is consistent with the findings in [21], in which the reflected wave amplitude had a similar change with the increase in notch depth.

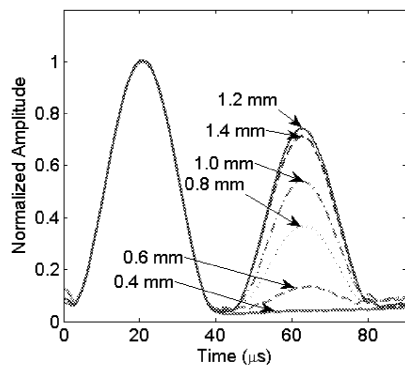


Fig. 6. Wave envelopes of the reflected waves from notches with 0.8 mm width and varying depths

Fig. 7 shows the envelopes of the transmitted waves at monitoring point 2. In contrast with Fig. 6, the signals shown in Fig. 7 only contain one wave pack because monitoring point 2 is located after the notches, causing the incident wave and the wave induced by the notch to overlap. As shown in Fig. 7, the amplitude of the transmitted wave envelopes decreases with the notch depth as a result of the scattering of energy that converts transmitted waves into reflected waves at the notches.

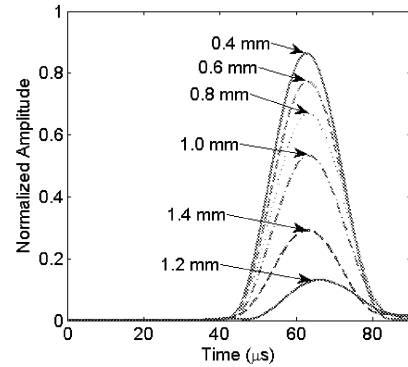


Fig. 7. Wave envelopes of the transmitted waves from notches 0.8 mm wide of varying depths

### B. Effect of notches with different widths

Notches with widths varying from 0.4 to 2.4 mm with 0.4 mm step increments were also investigated, as described in this subsection. The depth of all notches was maintained at 0.8 mm. Figs. 10 and 11 show the envelopes of the reflected and transmitted waves calculated at monitoring points 1 and 2, respectively. In contrast to the results of the notches of varying depths in Section IVA, the reflected and transmitted wave amplitude from the notches does not increase or decrease linearly in relation to notch width. The amplitude of the waves reflected and transmitted from the notches follows either a sinusoidal or cosinusoidal pattern according to the width of the notch [21].

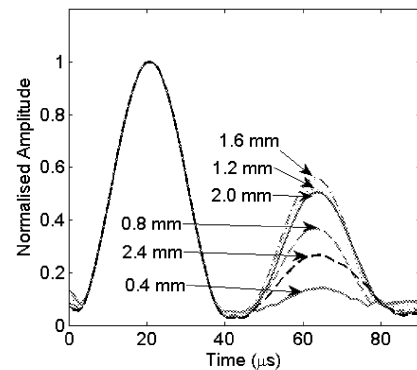


Fig. 8. Wave envelopes of the waves reflected from notches 0.8 mm deep and of varying widths

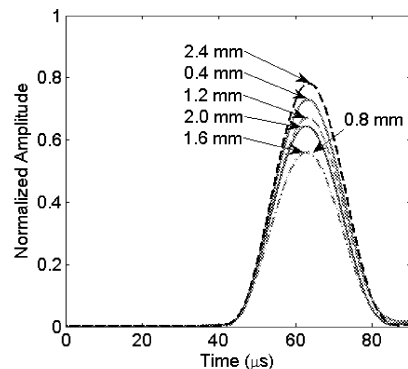


Fig. 9. Wave envelopes of the waves transmitted from notches 0.8 mm deep and of varying widths

C. Effect of delaminations with different lengths

Investigations of delaminations of different lengths are described in this subsection. Figs. 10 and 11 show the calculated envelopes of reflected and transmitted waves at monitoring points 1 and 2, respectively. The delaminations were located between the 4<sup>th</sup> and 5<sup>th</sup> lamina, which are mid-plane ( $z = 0$ ) of the laminated composite beam. The wave envelope amplitudes were normalized so that the amplitude of the incident wave at monitoring point 1 equaled 1. As shown in Fig. 10, the widths of the reflected wave envelopes for 8 and 10 mm long delaminations are wider than those for 4 and 6 mm delaminations. These results reflect the fact that the wavelength of the incident wave is shorter than the 8 and 10 mm long delaminations, and therefore, multiple wave reflections can occur, increasing the width of the reflected waves.

The amplitude of the waves reflected from the delaminations was usually smaller than the amplitude of the waves reflected from the notches. Fig. 11 shows the amplitude of the waves transmitted from the delaminations. As shown in Fig. 11, the minimum transmitted wave amplitude is 75% of the incident wave amplitude at monitoring point 1 (Fig. 10). The change in the amplitude of the transmitted wave is smaller than the change in the amplitude of the wave emanating from the notches (Figs. 8 and 9). However, the transmitted wave is still considered sensitive for damage detection.

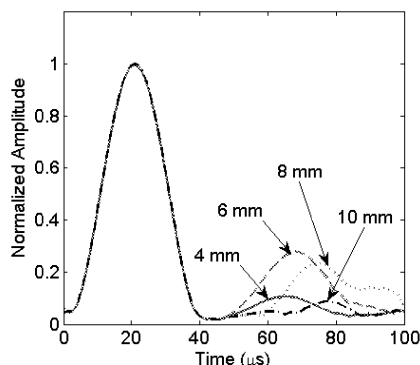


Fig. 10. Wave envelopes of the reflected waves from delaminations of varying lengths

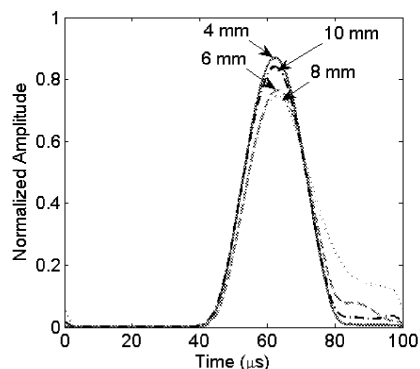


Fig. 11. Wave envelopes of the transmitted waves from delaminations of varying lengths

D. Effect of delaminations at different through-thickness locations

It is obvious that the delaminations at different through-thickness locations have different effects on the  $A_0$  GW

scattering characteristics. This subsection further investigates this phenomenon by considering 8 mm long delaminations located between the 4<sup>th</sup> and 5<sup>th</sup>, 3<sup>rd</sup> and 4<sup>th</sup>, 2<sup>nd</sup> and 3<sup>rd</sup>, and 1<sup>st</sup> and 2<sup>nd</sup> lamina of the composite beam. The results of the reflected and transmitted wave amplitudes are shown in Figs. 12 and 13, respectively. These results are labeled L4-5, L3-4, L2-3 and L1-2. Although all the delaminations have the same length, the reflected and transmitted wave amplitudes are different for the delaminations located between the 4<sup>th</sup> and 5<sup>th</sup>, 3<sup>rd</sup> and 4<sup>th</sup>, 2<sup>nd</sup> and 3<sup>rd</sup>, and 1<sup>st</sup> and 2<sup>nd</sup> lamina. This is mainly due to the mode conversion effect, in which part of the reflected and transmitted  $A_0$  wave energy is converted to other GW modes.

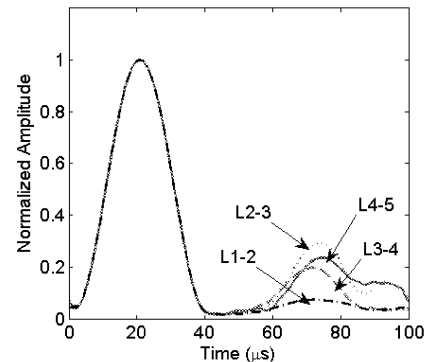


Fig. 12. Wave envelopes of the reflected waves from 8 mm long delaminations at different through-locations

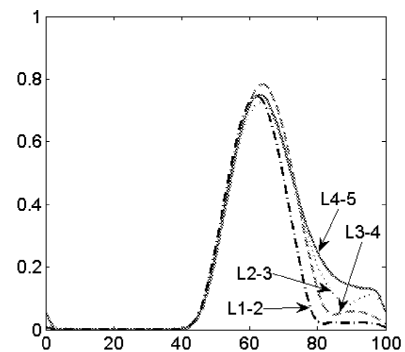


Fig. 13. Wave envelopes of the transmitted waves from 8 mm long delaminations at different through-thickness locations

V. CONCLUSION

The current study has demonstrated the use of gradually increasing damping to construct the absorbing regions for boundaries of GW problems in composite materials, thereby reducing the size of the FE models and the computational cost of the simulations. The 3D FE method together with the developed absorbing regions were employed in an investigation of the scattering characteristics of the  $A_0$  GW at notches and delaminations in laminated composite beams. A series of case studies was used to investigate the characteristics of the waves reflected and transmitted from these defects. Notches with different depths and widths, and delaminations of varying length and at different through-thickness locations were also investigated. The results of this study provide improved insight into the scattering phenomena of  $A_0$  GW at defects in composite materials, insight which is essential to further advance the development of GW damage detection techniques.

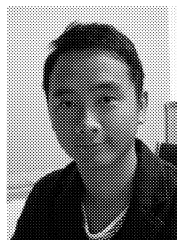
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